# High resolution absorption cross-section measurements of the Schumann-Runge bands of $\mathrm{O}_{2}$ by VUV Fourier transform spectroscopy 

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#### Abstract

The photoabsorption spectrum of the $\mathrm{O}_{2}$ Schumann-Runge bands was measured with resolution comparable to the Doppler widths by using the VUV Fourier transform spectrometer from Imperial College, London, combined with synchrotron radiation as a continuum light source at the Photon Factory, KEK, Japan. The analysis of the $(12,0)-(17,0)$ bands of the Schumann-Runge system provides accurate rotational line positions as well as the line intensities from 185 to 175 nm . Molecular constants of the $v^{\prime}=12$ to 17 levels of the $B^{3} \Sigma_{u}^{-}$state have been determined. The $\left(v^{\prime}, 0\right)$ band oscillator strengths were determined as $2.38,2.62,2.70$, 2.66, 2.40, and $2.12 \times 10^{-5}$ for the bands from $v^{\prime}=12$ to 17 , respectively. © 2003 Elsevier Science (USA). All rights reserved.


## 1. Introduction

The Schumann-Runge (S-R) band system, which can be found in the photoabsorption spectrum of $\mathrm{O}_{2}$ in the wavelength region $175-205 \mathrm{~nm}$, is ascribed to the transition from the ground state $X^{3} \Sigma_{g}^{-}$to the excited state $B^{3} \Sigma_{u}^{-}$. The S-R bands contain many relatively narrow $\left(0.2-4 \mathrm{~cm}^{-1}\right)$ rotational lines belonging to 14 branches ( 6 principal, 6 satellite, and 2 forbidden branches) of this triplet-triplet transition. Although the upper state $B^{3} \Sigma_{u}^{-}$ is a bound state, it is dissociated by interaction with repulsive states to produce two oxygen atoms in the ground state [1]. This predissociation is the major source of oxygen atoms in the stratosphere (height of 11-

[^0]48 km ) and especially in the mesosphere (height of 48 90 km ). Because atomic oxygen plays an important role in the photochemistry of these atmospheric regions, it is necessary to obtain the wavelengths, the oscillator strengths and the linewidths of rovibrational lines in the S-R band for atmospheric photochemical modeling [2].

Spectroscopic aspects of the S-R bands have been extensively reviewed by Krupenie [3], Creek and Nicholls [4], and Huber and Herzberg [5]. The analyses of the S-R bands were initiated by Curray and Herzberg [6], Knauss and Ballard [7], and Brix and Herzberg [8]. Yoshino et al. [9] reviewed and presented the vibronic assignments of the S-R bands. The molecular constants of the $B^{3} \Sigma_{u}^{-}$ state were determined from the experimental data [9] by Cheung et al. [10]. Recently the rotational perturbations in the $B^{3} \Sigma_{u}^{-}$state were studied by high resolution laser absorption spectroscopy for the $(16,0)-(18,0)$ bands by Lewis et al. [11]. The same group extended the assignments of the S-R bands up to $v^{\prime}=22$ [12].

Earlier, Bethke determined the band oscillator strengths of the S-R bands by lower resolution photoelectric measurements using the technique of pressure broadening [13]. In 1975, Huebner et al. also determined band oscillator strengths by electron energy loss measurements [14]. More recent determinations of the band oscillator strengths of the S-R bands were made by Frederick and Hudson [15] and Lewis and co-workers [16-20]. The Harvard-Smithsonian Center for Astrophysics (CfA) group measured absorption cross-sections for the $(1,0)$ through $(12,0)$ S-R bands at $300 \mathrm{~K}[21,22]$ and 79 K [23] with a resolution of $\simeq 0.40 \mathrm{~cm}^{-1}$ and determined the band oscillator strengths for these bands directly from the measured cross-sections.

In the present paper, we report experimental crosssection data at 295 K throughout the wavelength region $175-182.5 \mathrm{~nm}$ containing the ( $v^{\prime}, 0$ ) bands from $v^{\prime}=12$ to the dissociation limit. The linewidths in the S-R bands above $v^{\prime}=12$ suddenly become narrower, especially in the $(13,0)$ and the $(14,0)$ bands. Almost all linewidths observed at room temperature for the vibrational bands above $v^{\prime}=12$ are less than $0.4 \mathrm{~cm}^{-1}$. The highest resolution of conventional spectrometers using gratings is about $0.4 \mathrm{~cm}^{-1}$ in the $\mathrm{S}-\mathrm{R}$ wavelength region. Therefore, as discussed by Stark et al. [24], it is difficult to obtain precise oscillator strengths of the rovibrational lines of the bands for $v^{\prime}>12$ with a conventional spectrometer. For this reason we used a new method for the measurement of these bands: Fourier transform (FT) spectroscopy, with synchrotron radiation as a background light source.

Although FT spectroscopy is generally regarded as a technique for the infrared, where the multiplex advantage can be exploited, the FT spectrometer at Imperial College London (IC) is designed for the ultraviolet and operates from the visible region to 140 nm with a resolution limit down to $0.03 \mathrm{~cm}^{-1}$ [25,26]. Using this instrument and a White cell, Yoshino et al. measured the absorption cross-sections of the Herzberg I, II, and III bands of $\mathrm{O}_{2}$ at a resolution of $0.06 \mathrm{~cm}^{-1}$ (resolving power 750000 ) (e.g. [27,28]). However, in order to obtain good signal-to-noise ( $S / N$ ) ratios in an absorption spectrum in the VUV, it is necessary to use a background continuum source of high photon flux in that region, preferably in conjunction with a predisperser to limit the spectral bandwidth. We therefore moved the FT spectrometer to the Photon Factory synchrotron source in Japan.

## 2. Experimental

The present experiment was carried out at the Photon Factory (PF), High Energy Accelerator Research Organization (KEK), Japan. PF synchrotron radiation is provided by the storage ring $(2.5 \mathrm{GeV})$. Full details of
the experimental setup were described in a previous paper [29]. The FT spectrometer was connected to beam line 12B [30,31] in PF. Synchrotron radiation from the predisperser system in the beam line was reflected by a cylindrical mirror and focused onto the entrance aperture of the FT spectrometer. To ensure full coverage from the $(12,0)$ band to the dissociation limits of $\mathrm{O}_{2}$, the predisperser was set to produce center wavelengths of 177.5 and 180.0 nm , with a bandwidth of 2.5 nm . The diameter of the entrance aperture was set at 1.5 mm . The spectral resolution was either 0.06 or $0.12 \mathrm{~cm}^{-1}$ by using the maximum optical path difference for the scan of 8.33 or 4.16 cm , respectively. The absorption cell, with an optical path length of 7.82 cm , was placed between the predisperser and the FT spectrometer, and $\mathrm{O}_{2}$ gas was introduced at pressures of 2.00, 4.00, and 10.00 Torr at room temperature ( 295 K ), corresponding to column densities of $0.51,1.02$, and $2.56 \times 10^{18} \mathrm{~cm}^{-2}$. The $\mathrm{O}_{2}$ pressure was measured with a capacitance manometer (MKS Baratron). For the measurements at $0.12 \mathrm{~cm}^{-1}$ resolution, a total integration time of about 20 h , obtained from around 400 coadded scans, yielded $S / N$ ratios in the continuum background of about 100. The $S / N$ ratios for the spectra observed with a resolution of $0.06 \mathrm{~cm}^{-1}$ were about 50 or less.

## 3. Analysis of the spectrum

### 3.1. Fitting of the FT data

The measured absorption spectra were converted to optical depth by taking the logarithms of the intensity $(I)$ and fitting a smooth continuum to the regions between the lines $\left(I_{0}\right)$. The absorption lines were fitted to Voigt profiles using the spectral reduction routine GREMLIN [32]. Line parameters (position, width, intensity, and Gaussian and Lorentzian contributions to the Voigt profile) are determined through a nonlinear least-squares iterative procedure. The spectra used for the analysis have a $S / N$ ratio for $I_{0}$ of about 100 . There are many seriously blended lines in the SchumannRunge spectrum, particularly the low rotational $R_{2}, R_{3}$ and $P_{2}, P_{3}$ lines for $N=3$ to 11 . These blended lines could be separated by taking care to keep the combination rule of line positions for blended $R_{2,3}(N)$ and $P_{2,3}(N+2)$ lines, and to constrain the intensity ratios between these $R$ and $P$ lines to be almost the same, according to the calculated Hönl-London factors discussed by Tatum and Watson [33]. We obtained temporary line parameters from the first fitting results and determined provisional line positions for $R_{2,3}(N)$ and $P_{2,3}(N+2)$ and then we refitted the lines with these new positions. If the line strengths obtained in the second fitting were satisfactory, the line positions should be correct; otherwise the line positions were further
adjusted until the relative line strengths were in good agreement with the intensity ratio estimated from the Hönl-London factors. This procedure is also effective to deconvolute blends between lines in different branches.

The Lorentzian component of the Voigt profile is due to the predissociation of the $B^{3} \Sigma_{u}^{-}$state, and the Gaussian component is due to Doppler broadening, with a full-width at half maximum (FWHM) of $0.12 \mathrm{~cm}^{-1}$. The instrumental function of the spectrometer can be approximated by a Gaussian function of width $0.12 \mathrm{~cm}^{-1}$, and the convolution of this with the Doppler width should give an effective Gaussian width of $0.17 \mathrm{~cm}^{-1}$. However, the best fit Gaussian component is significantly wider than this, ranging from 0.26 to $0.30 \mathrm{~cm}^{-1}$. These anomalous Gaussian widths are considered to be due to drifts in alignment causing very small wave number shifts over the long observation periods [34]. In our fitting procedure, the Gaussian contribution for each spectrum is kept constant for all lines at the mean value found for that spectrum (i.e., between 0.26 and $0.30 \mathrm{~cm}^{-1}$ ).

### 3.2. Line positions and molecular constants

Fig. 1a shows the spectrum of the Schumann-Runge $\left(v^{\prime}, 0\right)$ bands in the region from 55450 to $57500 \mathrm{~cm}^{-1}$, in which the bands for $v^{\prime}=12$ to 17 are included. We assigned about 650 lines in the present analysis according to the results of Yoshino et al. [9]. An expanded portion of the $(14,0)$ band spectrum is shown in Fig. 1b with details of the rotational structure, which includes the high $J$ lines of the $(15,0)$ and $(16,0)$ bands. The line positions for the $(12,0)-(17,0)$ bands of the $S-R$ system were obtained by averaging over the lines with different experimental conditions. The results are presented in Tables 1a and 1b for the six principal branches and for the satellite and forbidden branches, respectively. About one-fourth of all assigned lines are blended with other lines. In general, the $P_{1}$ and $R_{1}$ lines are well separated from the $P_{2,3}$ and $R_{2,3}$ lines. However, some of them are blended closely with lines from other bands, for example $R_{1}(3)$ of the $(15,0)$ band with $R_{2}(13)$ of the $(16,0)$ band. In Tables 1a and 1 b , the partly resolved complexes are labeled with "b." Several high $J$ lines are entirely blended with other strong lines and could not be deconvoluted by the least-square fitting. Such blended lines are analyzed as a single line. Table 1a presents also calculated wavenumbers for the blended high $J$ lines in italic, which are derived from the term values.

The perturbation in the $(16,0)$ band, observed by Brix and Herzberg [8] and Yoshino et al. [9], was assigned to the interaction with the $C^{\prime 3} \Pi_{u}$ state by Lewis et al. [11]. For the $(16,0)$ band, they observed 4.5 pairs of the $R_{2}(N)+P_{2}(N+2)$ lines with $N=3$ to 11 , and we confirmed 3.5 pairs with $N=5$ to 11 . Those extra lines are presented in Table 1a with E. The limited number of


Fig. 1. (a) Absorption cross-section spectrum of the Schumann-Runge bands $\left(55300-57400 \mathrm{~cm}^{-1}\right)$ from $(12,0)$ to $(17,0)$ obtained with 4 Torr of oxygen. (b) An expanded portion of the spectrum of the $(14,0)$ band in the region of $56250-56310 \mathrm{~cm}^{-1}$.
observations of these weak extra lines is due to the low column density of our absorption measurements. For the $(17,0)$ band, the line at $56448.523 \mathrm{~cm}^{-1}$ was assigned to $R_{3}(19)$, but Lewis et al. [11] designated it as an extra line of $R_{2}(19)$ without making any assignment to the $R_{3}(19)$ line. The assignments of the $R_{2,3}$ lines are kept the same as those of Brix and Herzberg [8] and Yoshino et al. [9], and their intensities will be discussed in the following subsection. The extra lines observed for the $(17,0)$ band are also presented in Table 1a with E. The perturbation related with the $F_{3}$ level of $v^{\prime}=16,17$ was also discussed by Lewis et al. [11], but we could not confirm any of those lines in the expected places.

The wavenumber scale in an FT spectrum is strictly linear, and therefore only one reference line is needed to fix the scale absolutely. In previous work we have used as reference the Hg I line at 184.8 nm (having fitted the isotope and hyperfine structure). This line appears in the $(8,0)$ band of the Schumann-Runge system, outside the range of the present measurements, but we have carried the wavenumber calibration through to the

Table 1a
Observed wavenumbers of the principal branch lines of the Schumann-Runge bands of $\mathrm{O}_{2}{ }^{\mathrm{a}}$

| $N$ | $R_{1}$ | $R_{2}$ | $R_{3}$ | $P_{1}$ | $P_{2}$ | $P_{3}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $(12,0)$ band |  |  |  |  |  |  |
| 1 | 55784.253 | 55785.083b |  | 55780.703 |  |  |
| 3 | 55777.781 | 55778.593b | 55778.922b | 55769.950 | 55770.707b | 55771.260 b |
| 5 | 55764.225 | 55765.063b | 55765.380b | 55751.945 | 55752.719b | 55752.975b |
| 7 | 55743.605 | 55744.525b | 55744.892b | 55726.883 | 55727.694b | 55727.973 b |
| 9 | 55715.943 | 55716.954b | 55717.387b | 55694.790 | 55695.668b | 55696.007b |
| 11 | 55681.214b | 55682.348b | 55682.846b | 55655.627 | 55656.617b | 55657.026b |
| 13 | 55639.420 b | 55640.661b | 55641.264b | 55609.433 | 55610.540b | 55611.017b |
| 15 | 55590.502 | 55591.869 b | 55592.604 b | 55556.173b | 55557.394b | 55557.977 b |
| 17 | 55534.482 | 55536.000 b | 55536.804b | 55495.809 | 55497.156b | 55497.872b |
| 19 | 55471.235 | 55472.921b | 55473.839b | 55428.351 | 55429.857 | 55430.643 |
| 21 | 55400.804 b | 55402.590 b | 55403.556 b |  |  |  |
| $(13,0)$ band |  |  |  |  |  |  |
| 1 | 56084.434b | 56085.701 |  | 56081.080 |  |  |
| 3 | 56077.440 | 56078.674b | 56079.008b | 56070.131b | 56071.324 b | 56071.898b |
| 5 | 56063.009 | 56064.326b | 56064.611b | 56051.607 | 56052.800 b | 56053.06 |
| 7 | 56041.204 | 56042.622b | 56042.979b | 56025.667 | 56026.958b | 56027.204b |
| 9 | 56012.031 | 56013.576 b | 56014.051b | 55992.373 | 55993.765b | 55994.094b |
| 11 | 55975.464 | 55977.15 | 55977.769 | 55951.708 | 55953.239 | 55953.690 |
| 13 | 55931.497 | 55933.336 | 55934.110 | 55903.672 | 55905.344 | 55905.943 |
| 15 | 55880.079 | 55882.104 | 55883.036 | 55848.246 | 55850.063 | 55850.820 |
| 17 | 55821.193 | 55823.391 | 55824.518 | 55785.385b | 55787.394b | 55788.308 |
| 19 | 55754.798 | 55757.168 | 55758.519 | 55715.072 | 55717.249b | 55718.357 |
| 21 | 55680.820 b | 55683.432b | 55684.950 | 55637.264 | 55639.613b | 55640.946b |
| 23 | 55599.217 | 55602.089 | 55603.795 | 55551.889 | 55554.483 | 55555.982b |
| 25 | 55509.913 | 55512.995 | 55514.907 | 55458.980 | 55461.821 | 55463.433 |
| (14,0) band |  |  |  |  |  |  |
| 1 | 56338.537 | 56340.393 |  | 56335.367 |  |  |
| 3 | 56330.945 | 56332.776 b | 56333.115b | 56324.239 | 56326.017b | 56326.614 b |
| 5 | 56315.553 | 56317.51 | 56317.806 b | 56305.110 b | 56306.901 b | 56307.167 b |
| 7 | 56292.443 b | 56294.571b | 56294.960b | 56278.209 | 56280.144 b | 56280.400 b |
| 9 | 56261.606 | 56263.928 b | 56264.492b | 56243.609 | 56245.715 b | 56246.076b |
| 11 | 56223.033 | 56225.572 | 56226.332 | 56201.296 | 56203.590 | 56204.131 |
| 13 | 56176.682 | 56179.474b | 56180.439 | 56151.254 | 56153.764 | 56154.502b |
| 15 | 56122.533 | 56125.569 | 56126.772 | 56093.438 | 56096.217 | 56097.157b |
| 17 | 56060.495 | 56063.845 | 56065.284 | 56027.831 | 56030.849 | 56032.051 |
| 19 | 55990.537 | 55994.210 b | 55995.881 | 55954.354 | 55957.669 | 55959.122 |
| 21 | 55912.606 | 55916.564 | 55918.552b | 55872.97 | 55876.618 | 55878.314 |
| 23 | 55826.598 | 55830.895 | 55833.244 | 55783.675b | 55787.615 b | 55789.564 |
| 25 | 55732.448 | 55737.195 | 55739.752 | 55686.284 | 55690.561 | 55692.814 |
| $(15,0)$ band |  |  |  |  |  |  |
| 1 | 56547.488 | 56550.287 |  | 56544.549 |  |  |
| 3 | 56539.264 b | 56542.043b | 56542.387b | 56533.184b | 56535.911 | 56536.599 |
| 5 | 56522.841 | 56525.779b | 56526.140b | 56513.433 | 56516.168b | 56516.440b |
| 7 | 56498.308 | 56501.528b | 56502.032b | 56485.490 | 56488.416b | 56488.734b |
| 9 | 56465.665 | 56469.172 | 56469.911 | 56449.479b | 56452.673b | 56453.149b |
| 11 | 56424.894b | 56428.744 | 56429.757 | 56405.354 | 56408.835 | 56409.550 |
| 13 | 56375.966 | 56380.168 | 56381.505 | 56353.104 | 56356.936b | 56357.928 |
| 15 | 56318.811 | 56323.419 | 56325.092b | 56292.719b | 56296.904 | 56298.222 |
| 17 | 56253.380 | 56258.404 | 56260.451 | 56224.126 | 56228.706 | 56230.343 |
| 19 | 56179.576b | 56185.091 | 56187.525 | 56147.271 | 56152.265 | 56154.290b |
| 21 | 56097.376 b | 56103.366 | 56106.251 | 56062.091 | 56067.523 | 56069.952 b |
| 23 | 56006.557 | 56013.310b | 56016.536 | 55968.439 | 55974.405 | 55977.284 |
| 25 | 55907.147 | 55914.312 | 55918.320 b | 55866.272 | 55872.988 | 55876.161 |
| (16,0) band |  |  |  |  |  |  |
| 1 | 56714.654 | 56718.974 | $56721.726 ?$ | 56711.922 |  |  |
| 3 | 56705.765b | 56710.046b | 56710.497b | 56700.350b | 56704.601 | 56705.429b |
| 5 | 56688.254 | $\begin{aligned} & 56692.735 \mathrm{~b} \\ & 56693.671 \mathrm{E} \end{aligned}$ | 56693.248b | 56679.929 | 56684.171b | 56684.549b |
| 7 | 56662.217 b | $\begin{aligned} & 56666.791 \mathrm{~b} \\ & 56667.595 \mathrm{E} \end{aligned}$ | 56667.797b | 56650.912 | $\begin{aligned} & 56655.366 \mathrm{~b} \\ & 56656.332 \mathrm{E} \end{aligned}$ | 56655.841 b |

Table 1a (continued)

| $N$ | $R_{1}$ | $R_{2}$ | $R_{3}$ | $P_{1}$ | $P_{2}$ | $P_{3}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 9 | 56627.670 | 56633.217 b | 56633.999 | 56613.384 | 56617.933 | 56618.911b |
|  |  | 56632.049 E |  |  | 56618.738 E |  |
| 11 | 56584.587 | 56590.564 | 56591.800 | 56567.358 | 56572.881 | 56573.639 |
|  |  | 56588.623 E |  |  | 56571.713 E |  |
| 13 | 56532.932b | 56539.377 b | 56541.112 | 56512.789 | 56518.738 | 56519.969 |
| 15 | 56472.566 | 56479.625 | 56481.854 | 56449.731 b | 56456.115 | 56457.820 |
| 17 | 56403.545 | 56411.163 | 56414.003 | 56377.881 | 56384.909 | 56387.132 |
| 19 | 56325.680 | 56333.893 | 56337.347b | 56297.424 | 56305.009 b | 56307.839 |
| 21 | 56238.905 | 56247.667 | 56251.952 | 56208.142 | 56216.360 | 56219.790 |
| 23 | 56143.083 |  | 56157.341 | 56110.010 | 56118.764 | 56123.055 |
| 25 | 56038.115 | 56047.130 |  | 56002.776 |  | 56016.962 |
| $(17,0)$ band |  |  |  |  |  |  |
| 1 | 56844.985 | 56851.566 |  | 56842.461 b |  |  |
| 3 | 56835.424 | 56842.048b | 56842.585b | 56830.693 | 56837.190b | 56838.137 |
| 5 | 56816.843b | 56823.719b | 56824.240 | 56809.611 | 56816.171 b | 56816.637b |
| 7 | 56789.311 b | 56796.591 | 56797.400 | 56779.502 | 56786.351 b | 56786.833b |
| 9 | 56752.827 | 56760.620 | 56761.876 | 56740.478 | 56747.734 | 56748.519 |
| 11 | 56707.384 | 56715.719 | 56717.581b | 56692.511 b | 56700.283b | 56701.513 |
| 13 | 56652.945 | 56661.830 | 56664.403 | 56635.591 | 56643.923 | 56645.754 |
| 15 | 56589.411 | 56598.679 | 56602.206 | 56569.686 | 56578.547 | 56581.094 |
|  |  | 56606.869 E |  |  |  |  |
| 17 | 56516.705b | 56526.050 b | 56530.835 | 56494.689 | 56503.998 | 56507.454 |
|  |  | 56531.874 E |  |  |  |  |
| 19 | 56434.713 | 56443.080 | 56448.523b | 56410.594 | 56419.940 | 56424.631b |
|  |  | 56448.523 E |  |  | 56425.705 E |  |
| 21 | 56343.320 | 56356.987 b | 56361.743 | 56317.176 | 56325.525 | 56330.949 |
|  |  | 56349.451 E |  |  |  |  |
| 23 | 56242.458 | 56256.545 |  | 56214.398 | 56228.038 | 56232.742 |

b: Incompletely resolved complex.
E: Extra lines resulting from the perturbation.
?: A line is observed at the correct position from the term values, but its intensity is too strong for this assignment. A line might be overlapped with others.
${ }^{\text {a }}$ Absolute values of the wavenumbers are subject to the calibration uncertainty of $0.03 \mathrm{~cm}^{-1}$. Lines for which the position is affected by an overlapping line or for which the term values are inconsistent are given to two places of decimals only. Values in italic are calculated from the combination rule.

Table 1b
Observed wavenumbers of the satellite and forbidden branch lines of the Schumann-Runge bands of $\mathrm{O}_{2}$

| $N$ | ${ }^{P} R_{13}$ | ${ }^{P} Q_{12}$ | ${ }^{P} Q_{23}$ | ${ }^{R} Q_{21}$ | ${ }^{R} Q_{32}$ | ${ }^{R} P_{31}$ | ${ }^{T} R_{31}$ | ${ }^{N} P_{13}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $(12,0)$ band |  |  |  |  |  |  |  |  |
| 1 | 55782.787 |  |  | 55786.960b | 55783.552b |  |  |  |
|  | 55782.787 | 55778.826 |  | 55786.960 | 55783.552 | 55785.429 | 55793.091 |  |
| 3 |  |  | 55772.768 |  | 55776.843 |  |  | 55766.534 |
|  | 55770.084 | 55768.000 | 55772.791 | 55780.543 | 55776.838 | 55778.787 | 55791.193 | 55766.534 |
| $(13,0)$ band |  |  |  |  |  |  |  |  |
| 1 | 56083.170 | 56079.203 b |  | 56087.591 | 56084.190b | 56086.066 |  |  |
|  | 56083.164 | 56079.203 |  | 56087.577 | 56084.190 | 56086.066 | 56093.176 |  |
| 3 |  | 56068.181 | 56073.408 | 56080.643 | 56076.930 |  |  | 56066.911 |
|  | 56070.265 | 56068.181 | 56073.409 | 56080.624 | 56076.924 | 56078.873 | 56090.423 | 56066.911 |
| 5 |  | 56049.624 | 56054.822 |  |  |  |  | 56044.330 |
|  | 56051.629 | 56049.618 | 56054.811 | 56066.314 | 56062.599 | 56064.587 | 56080.362 | 56044.318 |
| (14,0) band |  |  |  |  |  |  |  |  |
| 1 | 56337.452b |  |  | 56342.271 | 56338.905 |  | 56347.316 |  |
|  | 56337.451 | 56333.490 |  | 56342.270 | 56338.905 | 56340.782 | 56347.283 |  |
| 3 |  |  | 56328.095 |  |  |  |  | 56321.197 |
|  | 56324.371 | 56322.287 | 56328.101 | 56334.725 | 56331.030 | 56332.980 | 56343.619 | 56321.199 |
| $(15,0)$ band |  |  |  |  |  |  |  |  |
| 1 | 56546.634 |  |  | 56552.164 | 56548.881 | 56550.764 | 56556.546 |  |
|  | 56546.634 | 56542.673 |  | 56552.164 | 56548.891 | 56550.767 | 56556.556 |  |

Table 1b (continued)

| $N$ | ${ }^{P} R_{13}$ | ${ }^{P} Q_{12}$ | ${ }^{P} Q_{23}$ | ${ }^{R} Q_{21}$ | ${ }^{R} Q_{32}$ | ${ }^{R} P_{31}$ | ${ }^{T} R_{31}$ | ${ }^{N} P_{13}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3 |  |  | 56537.996 |  |  |  |  | 56530.381 |
|  | 56533.319 | 56531.235 | 56537.996 | 56543.992 | 56540.303 | 56542.253 | 56551.954 | 56530.381 |
| 5 |  |  |  |  |  |  |  | 56507.367 |
|  | 56513.454 | 56511.443 | 56518.180 | 56527.773 | 56524.129 | 56526.117 | 56539.417 | 56507.372 |
| $(16,0)$ band |  |  |  |  |  |  |  |  |
| 1 | 56714.006 |  |  | 56720.810 | 56717.721 b | 56719.598 | 56724.665b |  |
|  | 56714.006 | 56710.045 |  | 56720.852 | 56717.721 | 56719.598 | 56724.662 |  |
| 3 |  | 56698.313 | 56706.684 |  | 56708.412 |  |  | 56697.753 |
|  | 56700.479 | 56698.394 | 56706.684 | 56711.996 | 56708.409 | 56710.359 | 56719.061 | 56697.753 |
| 5 |  | $56677.880$ |  |  |  |  |  | $56674.731$ |
|  | 56679.953 | $56677.941$ | 56686.183 | 56694.723 | 56691.237 | 56693.225 | 56705.180 | $56674.531$ |
| $(17,0)$ band |  |  |  |  |  |  |  |  |
| 1 | $56844.555$ | $56840.417$ |  | $56853.443$ | $56850.474 \mathrm{~b}$ | $56852.306$ | $56856.758 \mathrm{~b}$ |  |
|  | $56844.545$ | $56840.584$ |  | $56853.443$ | $56850.429$ | $56852.306$ | $56856.753$ |  |
| 3 |  |  | 56839.367 |  |  |  | 56850.084b | 56828.302 |
|  | 56830.822 | 56828.738 | 56839.274 | 56844.000 | 56840.500 | 56842.450 | 56850.052 | 56828.292 |
| 5 |  |  |  |  |  |  | 56834.829b | 56804.875 b |
|  | 56809.623 | 56807.612 | 56818.187 | 56825.708 | 56822.228 | 56824.216 | 56834.787 | 56804.875 |
| 7 |  |  |  |  |  |  |  | 56772.257 |
|  | 56779.459 | 56777.486 | 56788.325 | 56798.607 | 56795.430 | 56797.446 | 56810.802 | 56772.216 |
| 9 |  |  |  |  |  |  |  | 56730.577 |
|  | 56740.384 | 56738.438 | 56749.679 | 56762.660 | 56759.929 | 56761.969 | 56778.034 | 56730.574 |

Absolute values of the wavenumbers are subject to the calibration uncertainty of $0.03 \mathrm{~cm}^{-1}$. Values in italic are calculated from the term values. b: Incompletely resolved complex.
$(13,0)$ band by using lines from another of our recorded spectra that overlaps both bands. This step-by-step calibration is a well-known technique. Its accuracy in this case is limited by the large widths of the rotational lines in the $(8,0)$ band $\left(1.5-2.0 \mathrm{~cm}^{-1}\right.$ FWHM) [35] that are used for the transfer, which make it difficult to deconvolute their fine structure splitting accurately. The uncertainty in the absolute wavenumber derived in this way is estimated to be $0.03 \mathrm{~cm}^{-1}$. However, uncertainties of the relative positions for the strong unblended $P_{1}$


Fig. 2. Differences in the observed line positions between present results and Yosino et al. [9]. The differences of $P_{1}$ and $R_{1}$ lines are presented by solid circles, $P_{2}, R_{2}$ and $P_{3}, R_{3}$ are presented by open squares and open triangles, respectively. The solid horizontal line represents the average shift of $0.007 \mathrm{~cm}^{-1}$.
and $R_{1}$ lines are better than $0.01 \mathrm{~cm}^{-1}$. Fig. 2 shows the differences in the observed line positions between the results of the present FT spectroscopic measurement and the previous measurements of Yoshino et al. [9]. The positions of the unblended strong lines are in good agreement of $<0.1 \mathrm{~cm}^{-1}$. The differences are larger for some $F_{2}$ and $F_{3}$ lines because of insufficient resolution for these blended lines in the previous measurements, and they are also larger for the weak lines, where the discrepancies may be due to the uncertainties arising from the lower $S / N$ ratios in the FT spectra.

The rotational term values of the $B(v)$ levels can be obtained by adding the term values of the $X(0)$ level to the wavenumbers of the observed lines. The rotational term values of the ground state for each of three sublevels designated $F_{1}, F_{2}$, and $F_{3}$ were provided by Amiot and Verges [36]. The energy origin of these term values is taken for the hypothetical level $F_{2}, N=J=0$ of the $X(0)$ level. The rotational term values of the levels with $v=12$ to 17 obtained in the present work are listed in Table 2 with the estimated uncertainty of the average in $1 \sigma$ limits. The term values obtained from the extra lines for the $v=16$ and 17 levels are also shown in italic in Table 2. The uncertainties in the term values of high $J$ levels increases because of the decreasing $S / N$ ratios for the lines. For the levels with $v=16$ and 17 , the blended lines in the band head region have influence on the uncertainties of the term values. Note that the absolute values of all terms have a possible systematic error of up to $0.03 \mathrm{~cm}^{-1}$ arising from the uncertainty in the calibration.

Table 2
The term values of the $B^{3} \Sigma_{u}^{-}$state of $\mathrm{O}_{2}{ }^{\text {a }}$

| $N$ | $v=12$ |  |  | $v=13$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $F_{1}$ | $F_{2}$ | $F_{3}$ | $F_{1}$ | $F_{2}$ | $F_{3}$ |
| 0 | 55781.701(5) |  |  | 56082.078(2) |  |  |
| 2 | 55785.252(6) | $55787.958(50)$ | 55786.427(5) | 56085.432(4) | 56088.576(5) | 56087.065(22) |
| 4 | 55793.083(10) | $55795.845(18)$ | 55794.089(13) | 56092.744(3) | 56095.926(3) | 56094.175(8) |
| 6 | 55805.365(8) | 55808.189(9) | 55806.495(2) | 56104.146(6) | 56107.452(3) | 56105.725(3) |
| 8 | 55822.094(19) | 55825.020(6) | 55823.413(12) | 56119.684(5) | 56123.117(14) | 56121.500(10) |
| 10 | 55843.254(3) | 55846.306(12) | 55844.794(3) | 56139.340(4) | 56142.928(4) | 56141.458(10) |
| 12 | 55868.843(10) | 55872.037(7) | 55870.614(21) | 56163.090(7) | 56166.841(4) | 56165.539(2) |
| 14 | 55898.836(21) | $55902.158(5)$ | 55900.861(12) | 56190.910(3) | 56194.830(4) | 56193.705(8) |
| 16 | $55933.165(13)$ | 55936.633(5) | 55935.488 (17) | 56222.741(2) | 56226.869(2) | 56225.922(2) |
| 18 | $55971.835(13)$ | 55975.476(2) | 55974.420 (8) | 56258.550(5) | 56262.868(6) | 56262.134(19) |
| 20 | 56014.715(49) | 56018.540(3) | 56017.616(34) | 56298.279(14) | 56302.787(31) | $56302.296(62)$ |
| 22 | 56061.820 | 56065.764 | 56064.906 | 56341.837(11) | 56346.607(14) | 56346.300(51) |
| 24 |  |  | 56389.199(76) | 56394.229(66) | 56394.102(51) |  |
| 26 |  |  | 56440.165 | 56445.440 | 56445.564 |  |
|  | $v=14$ |  |  | $v=15$ |  |  |
| 0 | 56336.366(8) |  | 56545.548(11) |  |  |  |
| 2 | $56339.538(6)$ | 56343.268(7) | 56341.781(29) | 56548.486(5) | 56553.163(10) | 56551.766(14) |
| 4 | 56346.247(7) | 56350.027(4) | 56348.282(2) | 56554.569(4) | 56559.294(6) | $56557.555(7)$ |
| 6 | 56356.690(9) | 56360.639(7) | 56358.921(9) | 56563.971(13) | 56568.911(19) | $56567.255(14)$ |
| 8 | 56370.923(5) | 56375.067(6) | 56373.482(7) | 56576.791(7) | 56582.025(13) | 56580.555(8) |
| 10 | 56388.921(6) | 56393.280(7) | 56391.898(7) | 56592.980(4) | 56598.524(4) | 56597.318(6) |
| 12 | 56410.665(6) | 56415.261(3) | 56414.099(8) | 56612.520(11) | 56618.434(5) | 56617.525(4) |
| 14 | 56436.099(5) | 56440.985(32) | 56440.038(4) | 56635.381(6) | 56641.666 (6) | 56641.104(11) |
| 16 | 56465.192(15) | $56470.330(11)$ | 56469.661(14) | $56661.478(6)$ | 56668.183(11) | 56667.968(16) |
| 18 | 56497.843(13) | 56503.304(20) | 56502.899(10) | 56690.743(10) | 56697.882(10) | 56698.067(5) |
| 20 | 56534.003(16) | $56539.799(53)$ | 56539.661(7) | 56723.069(54) | 56730.704(13) | 56731.302(13) |
| 22 | 56573.623(15) | 56579.738(18) | 56579.892(45) | 56758.392(9) | 56766.535(26) | 56767.602(26) |
| 24 | 56616.541(12) | 56623.015(29) | 56623.517(75) | 56796.511(18) | 56805.434(94) | 56806.854(49) |
| 26 | 56662.700 | 56669.641 | 56670.409 | 56837.399(18) | 56846.758(23) | 56848.978(00) |
|  | $v=16$ |  |  | $v=17$ |  |  |
| 0 | 56712.920(14) |  | 56843.459(37) |  |  |  |
| 2 | 56715.646(22) | 56721.851(20) | 56720.597(8) | 56845.989(14) | 56854.442(33) | 56853.304(6) |
| 4 | 56721.067(18) | 56727.297(11) | 56725.661(12) | 56850.738(20) | $56859.302(11)$ | $56857.752(15)$ |
| 6 | 56729.392(15) | 56735.861(21) | 56734.363(14) | 56857.981(24) | 56866.846(30) | 56865.354(1) |
|  |  | 56736.812(18) |  |  |  |  |
| 8 | 56740.693(11) | 56747.291(18) | 56746.318(11) | 56867.790(7) | 56877.086(18) | 56875.925(8) |
|  |  | 56748.090 (30) |  |  |  |  |
| 10 | 56754.984(10) | 56762.574(17) | 56761.409(10) | 56880.139(26) | 56889.972(27) | 56889.281(14) |
|  |  | 56761.406(19) |  |  |  |  |
| 12 | 56772.215(15) | 56780.247(16) | $56779.566(6)$ | 56895.009(16) | 56905.414(14) | 56905.346(14) |
|  |  | $56778.313(10)$ |  |  |  |  |
| 14 | 56792.393(40) | 56800.879(14) | 56800.704(5) | 56912.354(20) | 56923.318(16) | 56923.989(17) |
| 16 | 56815.233(15) | 56824.387(8) | 56824.743(8) | 56932.059(18) | 56943.459(28) | 56945.080(18) |
|  |  |  |  |  | 56951.633(18) |  |
| 18 | 56840.903(6) | 56850.633(16) | 56851.617(16) | 56954.074(11) | 56965.551(20) | 56968.408(37) |
|  |  |  |  |  | 56971.330(9) |  |
| 20 | 56869.159(24) | 56879.523(21) | 56881.142(37) | 56978.193(10) | 56988.699(8) | 56992.300(35) |
| 22 | 56899.939(29) | 56910.865(28) | 56913.338(53) | 57004.341(16) | 57020.161(29) | 57023.085(26) |
|  |  |  |  |  | 57012.625(78) |  |
| 24 | 56933.030(13) | 56947.650(45) | 57032.406(24) | 57048.668(14) |  |  |
| 26 | 56968.366(20) | 56979.575(60) |  |  |  |  |

${ }^{\text {a }}$ Absolute values of the wavenumbers are subject to the calibration uncertainty of $0.03 \mathrm{~cm}^{-1}$. Errors of $1 \sigma$ limits are given in the parentheses. The term values without errors were determined by only one observed line. Italic figures are the term values from the extra lines.

The molecular constants of the $B^{3} \Sigma_{u}^{-}$state of $\mathrm{O}_{2}$ from $v=1$ to 17 were derived by Cheung et al. [10] from the experimental data of Yoshino et al. [9]. They performed nonlinear least-square fitting for the matrix elements of
the Hamiltonian for a ${ }^{3} \Sigma$ electronic state in Hund case (a) basis, and determined the band origin $T_{v}$; the rotational parameters $B_{v}$ (rotational coefficient) and $D_{v}$ (rotational distortion coefficient); $\lambda$ (spin-rotational
interaction coefficient) and $\lambda_{D}$ (coefficient of the rotational distortion for the spin-rotational interaction); $\gamma$ (spin-spin interaction coefficient) and $\gamma_{D}$ (coefficient of the rotational distortion for the spin-spin interaction). We performed the same fitting analysis with the present new term values, except for $F_{2}(8)$ and $F_{2}(10)$ of the $v=16$ level and $F_{2}(N), N \geqslant 16$ and $F_{3}(N), N \geqslant 18$ of the $v=17$ level, because these rotational levels are perturbed as mentioned before. Fig. 3 shows the differences between measured and calculated term values for $v=14$ and 16. The two values are in good agreement for $v=14$. Even for the high rotational levels, which have large error bars because of the weak line intensities, the discrepancies are less than $0.07 \mathrm{~cm}^{-1}$, and this is true for all of the term values of $v=12$ to 15 . On the other hand, shifts in the term values are observed around $N=8$ of the $v=16$ level, as shown in Fig. 3. A large shifts in the $F_{2}$ and $F_{3}$ components of the $v=17$ level are also observed above $N=16$. The shifts of the $F_{2}$ component due to the perturbation with $C^{3} \Pi_{u}$ level occur between $N=18$ and $N=20$ [11]. The reason for the shifts of the $F_{3}$ component are not clear at present. For the $v=17$ level, we did not present values of $\lambda_{D}$ and $\gamma_{D}$, because the high rotational levels are not used in the least-square fitting. The molecular constants obtained in the present analysis are shown in Table 3, together with the values of Cheung et al. [10].

### 3.3. The integrated cross-sections of the lines and band oscillator strengths

The integrated optical depth of each rotational line is obtained along with the line position by the Voigt fitting procedure and is converted to an integrated cross-section by dividing by the column densities given in Section


Fig. 3. Differences between measured rotational term values and calculated term values for the $v^{\prime}=14$ (a) and $v^{\prime}=16$ (b). The differences of $T_{1}, T_{2}$, and $T_{3}$ are presented by solid circles, open squares, and crosses, respectively.
2. The results are presented in Tables 4 a and 4 b for the six principal branches and for the satellite and forbidden branches, respectively. For the $(13,0)-(15,0)$ bands, the

Table 3
Molecular spectroscopic constants $\left(\mathrm{cm}^{-1}\right)$ of the $B^{3} \Sigma_{u}^{-}$state $v=12$ to 17 of $\mathrm{O}_{2}$. ${ }^{\text {a }}$

| $v$ | $T(v)^{\text {b }}$ | B | $10^{5} \mathrm{D}$ | $\lambda$ | $-\gamma$ | $10^{3} \lambda_{\mathrm{D}}$ | $-10^{4} \gamma_{\mathrm{D}}$ | RMS ${ }^{\text {c }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 12 | 55783.011(7) | 0.56283(9) | 1.42(2) | 2.24(1) | 0.0632(9) | 0.24(5) | 0.09(3) | 0.02 |
|  | 55782.95(2) | 0.5626 (2) | 1.37(2) | 2.37(2) | 0.054(2) |  | 0.24(4) |  |
| 13 | 56083.695(3) | 0.52436(3) | $1.635(7)$ | 2.488(4) | 0.0848(4) | 0.02(2) | 0.21(1) | 0.03 |
|  | 56083.68(1) | 0.5242 (1) | 1.63(1) | 2.51(1) | 0.084(1) |  | 0.26 (2) |  |
| 14 | 56338.380(4) | $0.48320(4)$ | 2.041(8) | 2.793(5) | 0.1174(5) | 0.24(3) | $0.35(1)$ | 0.02 |
|  | 56338.43(1) | 0.48319 (8) | 2.084(9) | 2.81(2) | $0.116(1)$ | 0.19(4) | 0.39(2) |  |
| 15 | 56548.168(5) | $0.43885(5)$ | 2.42(1) | 3.269(6) | 0.1672(6) | 0.40(3) | 0.60(2) | 0.04 |
|  | 56548.26(1) | 0.4391 (1) | 2.54(2) | $3.30(2)$ | 0.164(2) | 0.31 (7) | 0.66 (4) |  |
| 16 | 56716.53(2) | 0.3931(2) | 2.98 (3) | 4.05(2) | 0.242(2) | $0.58(11)$ | 0.80(6) | 0.06 |
|  | 56716.64(2) | 0.3934 (2) | 3.08(3) | 4.11(3) | $0.241(3)$ | $0.33(1)$ | 0.81(6) |  |
| 17 | 56848.56(2) | 0.3463(2) | 3.70(5) | 5.14(2) | 0.352(2) |  |  | 0.05 |
|  | 56848.65(4) | 0.3457(8) | 3.34(31) | $5.18(3)$ | $0.348(3)$ |  |  |  |

[^1]Table 4a
Integrated cross-sections of the main branch lines of the Schumann-Runge bands of $\mathrm{O}_{2}$ in units of $10^{-19} \mathrm{~cm}^{2} \mathrm{~cm}^{-1}$ a

| $N$ | $R_{1}$ | $R_{2}$ | $R_{3}$ | $P_{1}$ | $P_{2}$ | $P_{3}$ | $R_{1}$ | $R_{2}$ | $R_{3}$ | $P_{1}$ | $P_{2}$ | $P_{3}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $(12,0)$ band |  |  |  |  |  | $(13,0)$ band |  |  |  |  |  |
| 1 | 2.90 | 1.67 b |  | 2.14 |  |  | 3.17 b | 1.74 |  | 2.03 |  |  |
| 3 | 4.77 | 3.82b | 2.89b | 4.25 | 2.27 b | 1.54 b | 4.85 | 4.22 b | 2.46 b | 5.04b | 2.68 b | 1.54 b |
| 5 | 6.02 | 5.03b | 3.89b | 5.17 | 4.20b | 2.97 b | 5.89 | 5.31 b | 4.52b | 5.11 | 4.31 b | 3.49 |
| 7 | 6.24 | 5.52b | 4.83 b | 5.41 | 4.68b | 4.29b | 5.91 | 5.55b | 5.29b | 5.44 | 5.39b | 4.54b |
| 9 | 5.71 | 5.25b | 4.53 b | 5.58 | 4.76b | 4.24b | 5.93 | 5.00b | 5.12b | 5.30 | 5.46b | 4.55b |
| 11 | 5.20 b | 4.32b | 3.82 b | 4.68 | 4.46b | 4.14b | 5.10 | 5.74 | 4.30 | 4.90 | 4.80 | 3.89 |
| 13 | 4.19b | 3.81 b | 3.25 b | 3.55 | 3.71 b | 3.33 b | 3.91 | 3.94 | 4.02 | 4.10 | 3.91 | 3.79 |
| 15 | 2.82 | 2.67 b | 2.48 b | 2.53 b | 2.66 b | 2.55 b | 3.37 | 3.03 | 2.93 | 3.28 | 3.37 | 2.58 |
| 17 | 2.10 | 1.68 b | 1.68 b | 1.95 | 1.83 b | 1.78 b | 2.07 | 2.45 | 2.13 | 2.43 b | 2.53 b | 2.05 |
| 19 | 1.19 | 1.57 b | 1.08 b | 1.42 | 0.88 | 0.80 | 1.80 | 1.46 | 1.61 | 1.45 | 1.78 b | 1.34 |
| 21 | 0.89b | 0.61 b | 0.75 b |  |  |  | 0.72b | 1.26 b | 0.85 | 0.76 | 0.89 b | 0.53 b |
| 23 |  |  |  |  |  |  | 0.42 | 0.33 | 0.45 | 0.27 | 0.44 | 0.67 b |
| 25 |  |  |  |  |  |  | 0.16 | 0.13 | 0.30 | 0.29 | 0.30 | 0.24 |
| Total | 42.03 | 35.95 | 29.19 | 36.69 | 29.46 | 25.64 | 43.30 | 40.14 | 34.00 | 40.40 | 35.87 | 29.22 |
| Ext. | 42.62 | 36.65 | 29.91 | 37.89 | 31.12 | 27.56 | 43.45 | 40.41 | 34.30 | 40.59 | 36.26 | 29.56 |
|  | $(14,0)$ band |  |  |  |  |  | $(15,0)$ band |  |  |  |  |  |
| 1 | 3.08 | 2.05 |  | 2.47 |  |  | 3.06 | 1.68 |  | 1.99 |  |  |
| 3 | 5.76 | 4.16b | 2.94b | 4.24 | 2.99b | 1.49 b | 4.35b | 3.77 b | 3.46b | 3.90b | 2.95 | 1.52 |
| 5 | 6.13 | 6.16 | 4.91b | 4.80 b | 4.86b | 3.82b | 5.91 | 5.28b | 4.02b | 5.49 | 4.72b | 3.25 b |
| 7 | 6.26 b | 6.31 b | 5.16b | 5.85 | 5.44b | 4.84b | 6.20 | 6.15 b | 4.98 b | 6.41 | 5.57 b | 4.58 b |
| 9 | 6.04 | 6.41b | 5.37 b | 5.86 | 5.63 b | 5.20 b | 5.94 | 5.59 | 5.36 | 6.62b | 5.86b | 4.84b |
| 11 | 4.93 | 5.33 | 4.36 | 4.88 | 4.88 | 4.64 | 5.87 b | 4.92 | 4.56 | 5.01 | 4.55 | 4.81 |
| 13 | 4.18 | 3.94b | 3.80 | 4.25 | 3.88 | 3.99b | 4.16 | 4.05 | 3.53 | 3.83 | 4.83b | 3.34 |
| 15 | 3.03 | 2.97 | 2.80 | 3.26 | 2.96 | 2.81b | 2.97 | 2.97 | 2.89b | 3.55 b | 3.02 | 3.36 |
| 17 | 2.23 | 2.28 | 1.73 | 2.13 | 2.06 | 1.92 | 2.41 | 2.27 | 2.43 | 2.42 | 2.36 | 2.80 |
| 19 | 1.55 | 1.36 b | 1.62 | 1.78 | 1.42 | 1.41 | 1.37 b | 1.42 | 1.37 | 1.21 | 1.57 | 1.35 b |
| 21 | 0.77 | 0.72 | 0.56 b | 1.44 | 1.01 | 0.87 | 0.66 b | 0.73 | 1.00 | 1.28 | 0.79 | 0.38 b |
| 23 | 0.59 | 0.66 | 0.36 | 0.39 b | 0.45 b | 0.79 | 0.48 | 0.74 b | 0.81 | 0.60 | 0.54 |  |
| 25 | 0.57 | 0.33 | 0.33 | 0.25 | 0.23 | 0.13 | 0.22 | 0.14 | 0.16 b | 0.16 |  | 0.35 |
| Total | 45.11 | 42.69 | 33.96 | 41.60 | 35.82 | 31.92 | 43.60 | 39.72 | 34.57 | 42.47 | 36.66 | 30.57 |
| Ext. | 45.21 | 42.84 | 34.16 | 41.86 | 36.07 | 32.32 | 43.76 | 39.92 | 34.88 | 42.56 | 37.40 | 31.72 |
|  | $(16,0)$ band |  |  |  |  |  | $(17,0)$ band |  |  |  |  |  |
| 1 | 2.40 | 2.20 | 1.08 ? | 1.53 |  |  | 2.39 | 1.45 |  | 1.73 b |  |  |
| 3 | 4.49b | 4.43b | 3.01 b | 4.08 b | 3.27 | 0.92b | 3.47 | 3.68 b | 1.65 b | 3.17 | 2.26b | 0.91 |
| 5 | 5.45 | 4.91 b | 4.16b | 5.26 | 4.25 b | 3.08 b | 4.44b | 5.09b | 4.94 | 3.98 | 4.13 b | 2.77b |
|  |  | 0.39 |  |  |  |  |  |  |  |  |  |  |
| 7 | 5.22 b | 2.14 | 4.11 b | 5.26 | 4.76b | 3.67 b | 3.94b | 4.98 | 3.86 | 4.66 | 4.85 b | 2.98b |
|  |  | 2.80 |  |  | 0.75 |  |  |  |  |  |  |  |
| 9 | 5.28 | 4.28 | 4.67 | 5.30 | 2.54 | 4.59b | 4.69 | 4.67 | 3.74 | 6.83 | 6.07 | 2.94 |
|  |  | 1.03 |  |  | 2.65 |  |  |  |  |  |  |  |
| 11 | 4.58 | $4.07$ | 4.43 | 4.43 | 3.76 | 3.81 | 3.83 | 4.08 | 4.00 b | 3.52 b | 3.24 b | 3.12 |
|  |  | $0.21$ |  |  | 0.59 |  |  |  |  |  |  |  |
| 13 | 4.33 b | 3.73 b | 4.01 | 4.98 | 3.51 | 3.40 | 3.17 | 3.29 | 2.80 | 2.99 | 2.86 | 2.55 |
| 15 | 2.57 | 2.43 | 2.25 | 2.42 b | 2.52 | 2.39 | 2.14 | 2.94 | 2.49 | 2.30 | 2.24 | 2.19 |
|  |  |  |  |  |  |  |  | 0.20 |  |  |  |  |
| 17 | 1.63 | 1.72 | 1.69 | 1.76 | 1.75 | 1.70 | 1.53 b | 1.84 b | 1.44 | 1.44 | 2.04 | 1.59 |
|  |  |  |  |  |  |  |  | 0.19 |  |  |  |  |
| 19 | 1.51 | 1.20 | 0.99 b | 1.18 | 1.39 b | 0.92 | 0.90 | 0.45 | 0.98 | 0.90 | 0.74 | 0.72b |
|  |  |  |  |  |  |  |  |  |  |  | 0.17 |  |
| 21 | 0.81 | 0.86 | 0.79 | 0.81 | 0.85 | 0.81 | 0.76 | 0.68 b | 0.49 |  |  |  |
|  |  |  |  |  |  |  |  | 0.12 |  |  |  |  |
| 23 | 0.34 |  | 0.30 | 0.31 | 0.28 | 0.22 | 0.52 | 0.32 |  | 0.62 | 0.39 | 0.48 |
| 25 | 0.16 | 0.08 |  | 0.26 |  | 0.11 |  |  |  |  |  |  |
| Total | 38.77 | 36.48 | 30.42 | 37.58 | 32.87 | 25.62 | 31.78 | 33.98 | 26.39 | 32.12 | 29.00 | 20.24 |
| Ext. | 38.90 | 36.88 | 30.76 | 37.70 | 33.25 | 25.90 | 32.03 | 34.22 | 27.33 | 32.97 | 29.95 | 21.57 |

b: Incompletely resolved complex.
${ }^{\text {a }}$ Extra lines resulting from the perturbation presented in italic.

Table 4b
Integrated cross-sections of the satellite and forbidden branch lines of the Schumann-Runge bands of $\mathrm{O}_{2}$ in units of $10^{-19} \mathrm{~cm}^{2} \mathrm{~cm}^{-1}$

| Band | $N$ | ${ }^{P} R_{13}$ | ${ }^{P} Q_{12}$ | ${ }^{P} Q_{23}$ | ${ }^{R} Q_{21}$ | ${ }^{R} Q_{32}$ | ${ }^{R} P_{31}$ | ${ }^{T} R_{31}$ | ${ }^{N} P_{13}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $(12,0)$ | 1 | 1.01 |  |  | 0.44 b | 1.39 b |  |  |  |
|  | 3 |  |  | 0.59 |  | 0.51 |  |  | 0.71 |
|  | Total | 1.01 |  | 0.59 | 0.44 | 1.90 |  |  | 0.71 |
| $(13,0)$ | 1 | 1.03 | 0.39 b |  | 0.60 | 1.65 b | 0.08 |  |  |
|  | 3 |  | 0.24 | 0.44 | 0.13 | 0.41 |  |  | 0.57 |
|  | 5 |  | 0.14 | 0.52 |  |  |  |  | 0.74 |
|  | Total | 1.03 | 0.77 | 0.96 | 0.73 | 2.06 | 0.08 |  | 1.31 |
| $(14,0)$ | 1 | 1.92 b |  |  | 0.98 | 1.91 |  | 0.05 |  |
|  | 3 |  |  | 0.92 |  |  |  |  | 0.73 |
|  | Total | 1.92 |  | 0.92 | 0.98 | 1.91 |  | 0.05 | 0.73 |
| $(15,0)$ | 1 | 1.11 |  |  | 0.98 | 1.57 | 0.39 | 0.31 |  |
|  | 3 |  |  | 0.54 |  |  |  |  | 0.42 |
|  | 5 |  |  |  |  |  |  |  | 0.53 |
|  | Total | 1.11 |  | 0.54 | 0.98 | 1.57 | 0.39 | 0.31 | 0.95 |
| $(16,0)$ | 1 | 1.46 |  |  |  | 0.75 b | 0.42 | 0.58b |  |
|  | 3 |  | 0.25 | 0.74 |  | 0.53 |  |  | 0.91 |
|  | 5 |  | 0.61 |  |  |  |  |  | 1.99 |
|  | Total | 1.46 | 0.86 | 0.74 |  | 1.28 | 0.42 | 0.58 | 2.90 |
| $(17,0)$ | 1 | 0.84 | 0.69 |  | 0.39 | 2.34 b | 1.17 | 0.46b |  |
|  | 3 |  |  |  |  |  |  | 1.21 b | 1.02 |
|  | 5 |  |  |  |  |  |  | 0.62b | 0.70b |
|  | 7 |  |  |  |  |  |  |  | 1.26 |
|  | 9 |  |  |  |  |  |  |  | 0.34 |
|  | Total | 0.84 | 0.69 |  | 0.39 | 2.34 | 1.17 | 2.28 | 3.32 |

b: Incompletely resolved complex.
present results were determined from the measurements with 2.00 Torr pressure of oxygen. The integrated crosssections of the strong lines ( $N=7$ to 13 ) obtained from the measurements with 4.00 Torr of oxygen are systematically lower than those at 2.00 Torr. These lines are very narrow, and it is possible that our resolution is not high enough to avoid errors from saturation. Therefore the cross-sections from the 4.00 Torr pressure were not included in the present results. The spectrum at 10 Torr pressure was not used at all for the integrated crosssections because of intensity saturation. The integrated cross-sections of the $R_{1}, R_{2}$, and $R_{3}$ branch lines of the $(14,0)$ band are plotted against $N$ in Fig. 4a, represented by the solid squares, circles, and triangles, respectively. The values listed in Tables 4 a and 4 b can be divided by the fractional populations of the rotational levels to obtain values proportional to the line oscillator strengths.

The extra lines observed in the $(16,0)$ and $(17,0)$ bands are results of the heterogeneous perturbation between $B^{3} \Sigma_{u}^{-}$and $C^{\prime 3} \Pi_{u}$ states discussed by Lewis et al. [11]. The almost equal intensities observed for the main and extra $P_{2}(9)$ and $R_{2}(7)$ lines of the $(16,0)$ band results from the maximum interaction at the $v^{\prime}=8$ level as shown in Fig. 4 of [11]. The strengths of the extra lines are borrowed from the perturbed levels of the $B^{3} \Sigma_{u}^{-}$
state. The results of the perturbation on their intensity are demonstrated in Fig. 4b for the $P_{2}$ branch of the $(16,0)$ band. The sum of the integrated cross-sections of the main and extra lines is used for the total and extended values, because the band oscillator strength of the $C^{\prime 3} \Pi_{u}-X^{3} \Sigma_{g}^{-}$system is negligible compared to that of the S-R band system. As mentioned in the previous section for the $(17,0)$ band, Lewis et al. [11] reassigned a line at $56448.523 \mathrm{~cm}^{-1}$ from $R_{3}(19)$ to an extra line of $R_{2}(19)$. However, then the total strength of $R_{2}(19)$ line (the main and extra) will be $1.43 \times 10^{-19} \mathrm{~cm}^{2} \mathrm{~cm}^{-1}$, which is too large compared with that of the $R_{1}(19)$ line. On the other hand, the strength of $R_{2}(19)$ is too weak by itself. Therefore we propose that the line at $56448.523 \mathrm{~cm}^{-1}$ is a blend of two lines, $R_{3}(19)$ and the extra line of $R_{2}(19)$.

The strengths of the branches are obtained by adding the integrated cross-sections of all rotational lines in the branch. These are listed in Tables 4a and 4b as 'Total.' The high rotational lines of $N>25$ are not observed in the present measurements because they are too weak with respect to the photon noise level. However, these higher $N$ lines should be taken into account for the total branch cross-sections. The extended total cross-section of each branch up to $N^{\prime \prime}=41$ was obtained by the extrapolation method using the Boltzmann distribution as


Fig. 4. (a) The integrated cross-sections of the $R_{1}, R_{2}$, and $R_{3}$ branch lines of $(14,0)$ band against $N$. The results of the measurements are shown by solid squares, circles, and triangles, respectively. Fitted curves of the Boltzmann distribution are shown by broken, dotted, and chain lines, respectively. (b) The integrated cross-sections of the $P_{2}$ branch lines of $(16,0)$ band. The total, main, and extra lines are shown by solid circles, open circles, and crosses, respectively.
discussed by Yoshino et al. [28], and it is given in the bottom line in Table 4a. The total integrated cross-sections of the satellite and the forbidden branches were
not extended because the fractional intensity distribution of these branches decreases rapidly with $J$. Table 5 gives the total observed integrated cross-section for each band, obtained by summing over all branches, together with the total extended integrated cross-section obtained by using the extended integrated cross-sections for the principal branches.

The uncertainties in the integrated cross-sections are due to noise in the spectra and errors in the measurement of the $\mathrm{O}_{2}$ pressure and optical path length. The small errors in the pressure ( $\pm 0.02$ Torr), temperature ( $295 \pm 2 \mathrm{~K}$ ), and path length ( $7.82 \pm 0.01 \mathrm{~cm}$ ) give a random error of less than $2 \%$. The error from the noise of the background is almost constant at $\pm 3 \times 10^{-20} \mathrm{~cm}^{2}$ over the whole spectrum. For the unblended strong lines of $5-6 \times 10^{-19} \mathrm{~cm}^{2} \mathrm{~cm}^{-1}$, the uncertainties due to noise are estimated to be $3-4 \%$. For weak lines of integrated cross-section $2.5 \times 10^{-19} \mathrm{~cm}^{2} \mathrm{~cm}^{-1}$ the uncertainty is $10 \%$, and for $1.0 \times 10^{-19} \mathrm{~cm}^{2} \mathrm{~cm}^{-1}$ it is $17 \%$. The large uncertainties of the weak peaks do not significantly affect the integrated cross-sections of the bands because these are determined predominantly by the strong lines. Therefore, total errors on the integrated cross-sections are estimated to be less than $5 \%$.

The band oscillator strength of the $\left(v^{\prime}, v^{\prime \prime}\right)$ band is given by
$f\left(v^{\prime}, v^{\prime \prime}\right)=\frac{m c^{2}}{\pi \mathrm{e}^{2}} \frac{1}{\tilde{N}\left(v^{\prime \prime}\right)} \int \sigma(v) \mathrm{d} v$
in which $\tilde{N}\left(v^{\prime \prime}\right)$ is the fractional Boltzmann population of the absorbing vibrational level, and integration of the cross-section $\sigma(v)$ is performed over all of the rotational lines belonging to the ( $v^{\prime}, v^{\prime \prime}$ ) band. Table 5 shows the oscillator strengths of the bands $v^{\prime}=12$ to 17 obtained in the present work from the extended total cross-sections of principal branches and the observed total crosssections of satellite and forbidden branches. Table 5 also shows the results obtained in earlier measurements. The

Table 5
Total and extended integrated cross-sections $\left(10^{-17} \mathrm{~cm}^{2} \mathrm{~cm}^{-1}\right)$, and band oscillator strengths $\left(10^{-5}\right)$ of the Schumann-Runge bands of $\mathrm{O}_{2}$

| Band | Integrated cross-sections |  | Band oscillator strengths, $f$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Total ${ }^{\text {a }}$ | Ext. ${ }^{\text {b }}$ | Present | $\mathrm{LBC}^{\text {c }}$ | YFEP ${ }^{\text {d }}$ | GGMBL ${ }^{\text {e }}$ | $\mathrm{HCMK}^{\text {f }}$ | Bethke ${ }^{\text {g }}$ |
| $(12,0)$ | 2.04 | 2.10 | 2.38 | 2.44 | 2.43 | 2.74 | 2.88 | 2.81 |
| $(13,0)$ | 2.30 | 2.32 | 2.62 | 2.73 |  | 2.87 | 3.41 | 3.17 |
| $(14,0)$ | 2.38 | 2.39 | 2.70 | 2.82 |  | 3.21 | 3.77 | 3.24 |
| $(15,0)$ | 2.33 | 2.36 | 2.66 | 2.73 |  | 2.95 | 3.73 | 3.26 |
| $(16,0)$ | 2.10 | 2.12 | 2.40 | 2.63 |  | 2.63 | 3.53 | 3.16 |
| $(17,0)$ | 1.83 | 1.88 | 2.12 |  |  | 2.64 | 3.03 | 2.95 |

${ }^{\mathrm{a}}$ Total integrated cross-sections from Tables 4a and 4b.
${ }^{\mathrm{b}}$ Extended integrated cross-sections from Tables 4a and 4b.
${ }^{\mathrm{c}}$ LBC: Lewis et al. [20].
${ }^{\mathrm{d}}$ YFEP: Yoshino et al. [21]
${ }^{\mathrm{e}}$ GGMBL: Gies et al. [19].
${ }^{\mathrm{f}}$ HCMK: Huebner et al. [14].
${ }^{\mathrm{g}}$ Bethke [13].


Fig. 5. Band oscillator strengths with $v^{\prime}=1$ to 17 . The oscillator strengths of $v^{\prime}=1$ to 12 derived from the measurement of Yoshino et al. [21] are shown in the open circles. Present results of $v^{\prime}=12$ to 17 are marked by solid circles.
present band oscillator strength of the $(12,0)$ band agrees with the result of Yoshino et al. [21] obtained by line-by-line photoabsorption cross-section measurement with a resolution of $0.40 \mathrm{~cm}^{-1}$. The oscillator strengths of the present work are smaller than those of Bethke [13] and Gies et al. [19] and much smaller than that of Huebner [14] obtained by electron energy loss measurement. The results of Lewis et al. [20], obtained by measurement without pressure broadening with a resolution of $1.4 \mathrm{~cm}^{-1}$ are near the present results, but still a little larger. Our value is the only one derived from line-by-line measurements with a resolution comparable to the rotational linewidths for the bands of $v^{\prime} \geqslant 13$. Moreover, we were able to separate the lines of one vibrational band from those of overlapping higher vibrational bands. Because this could not be done in the previous (low resolution) measurements, it is possible that the blending may have led to overestimates of the band oscillator strengths by those authors. Fig. 5 shows a plot of band oscillator strengths against $v^{\prime}$ for $v^{\prime}=1$ to 17 , using the results of the present work and those of Yoshino et al. [21].

## 4. Summary

This work provides the first absorption measurements of the Schumann-Runge $(13,0)-(17,0)$ bands of $\mathrm{O}_{2}$ free of problems arising from inadequate spectral resolution. In addition, this is the first measurements of the Schumann-Runge bands performed by the combination of a VUV FT spectrometer and a synchrotron radiation source. The present measurements provide accurate rotational line positions, term values and oscillator strengths of the $(12.0)-(17,0)$ bands.

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[^1]:    ${ }^{\text {a }}$ Estimated errors, which are $1 \sigma$ limits, are given in parentheses following the last figure of the molecular parameters. Italic parameters below the present results are determined by the previous work of Cheung et al. [10].
    ${ }^{\mathrm{b}}$ Absolute values of $T(v)$ are subject to the calibration uncertainty of $0.03 \mathrm{~cm}^{-1}$.
    ${ }^{\mathrm{c}}$ RMS is the root-mean-square deviation between calculated and observed term values.

