

# Atmospheric and oceanic circulations

PG Lectures, Autumn 2017  
Mike Byrne & Arnaud Czaja

# Aim and learning outcomes

Provide new PhD students in SPAT with an overview of why and how the atmosphere and ocean circulate and the implications for Earth's climate

# Aim and learning outcomes

Provide new PhD students in SPAT with an overview of why and how the atmosphere and ocean circulate and the implications for Earth's climate

1. Describe the **radiative drivers** of atmospheric and oceanic circulations
2. Describe the **structure of Earth's winds** (vs latitude and height)
3. Understand angular momentum conservation and implications for the **tropical Hadley cell**
4. Physical origins of **Ekman layers** and ocean gyres
5. Baroclinic instability in atmosphere and oceans, **Rossby number**, geostrophic balance
6. Atmospheric moisture transport: Influence on Earth's **water cycle** and thermohaline circulation

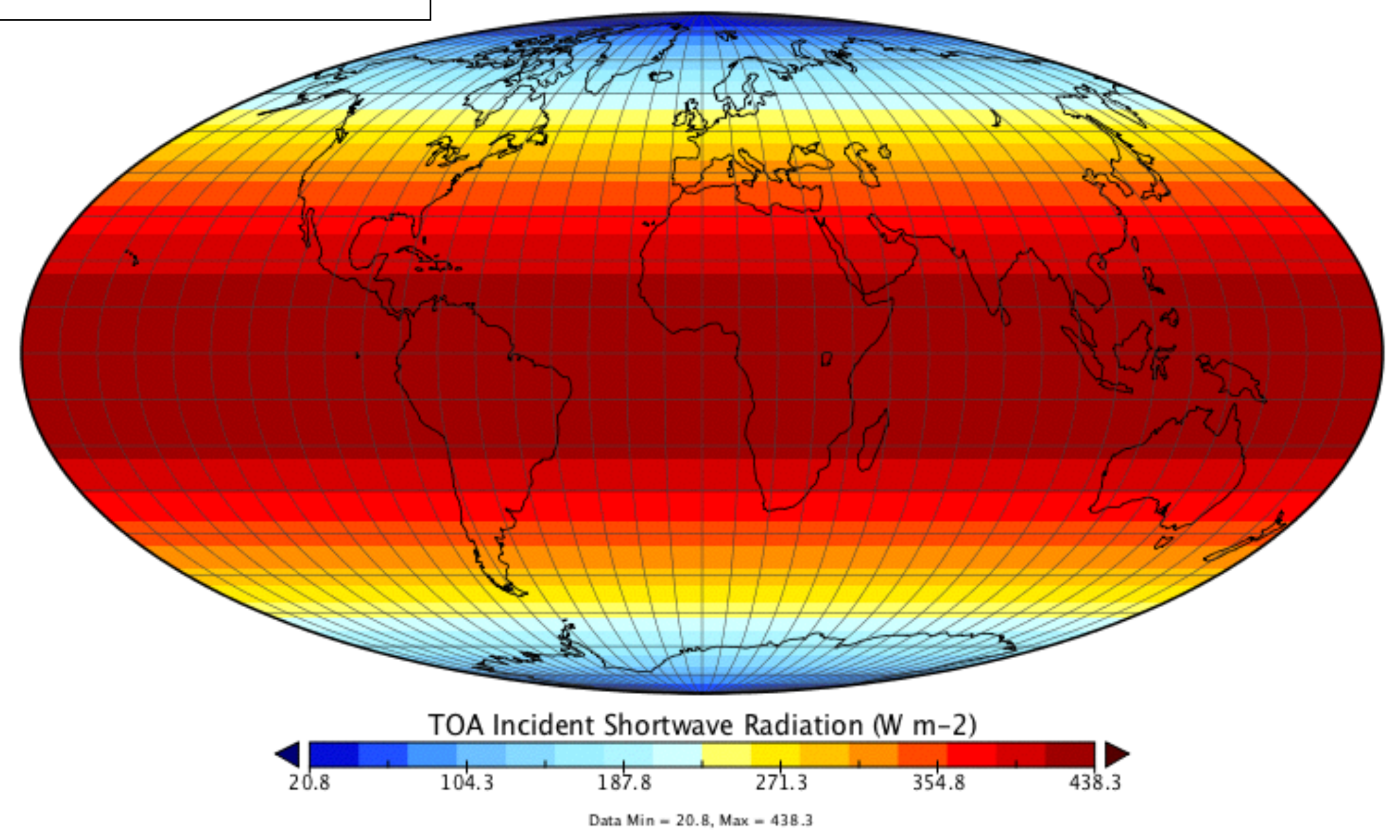
# Structure of the week

- **Monday:**
  - \*attendance register\*
  - Earth's radiative budget
  - Observed climate: temperature and winds
  - Atmosphere: Hadley cell and angular momentum
  - Ocean: Ekman layers, gyres
- **Tuesday:**
  - Baroclinic instability in the atmosphere, ocean, and classroom (tank experiment)
  - Rossby number, geostrophic balance
  - Impact of atmospheric circulation: Earth's water cycle
- **Friday:** 3 groups present & discuss problem-set solutions

# Phenomena: Earth's radiative balance — the circulation driver

NASA's CERES satellite

Top of Atmosphere Insolation  
March 2003

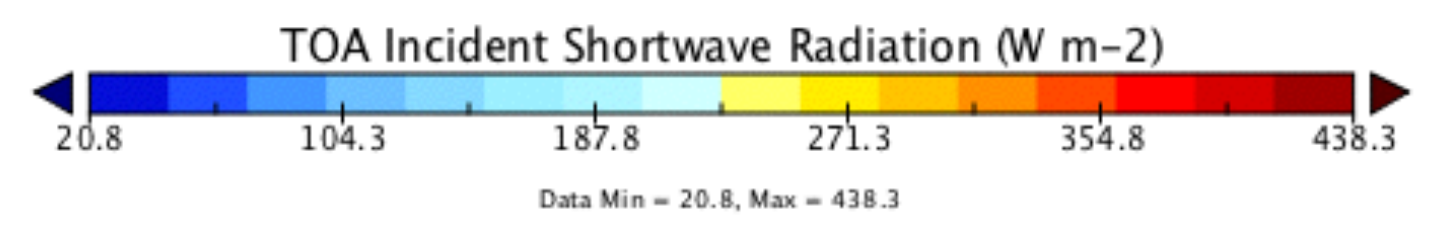
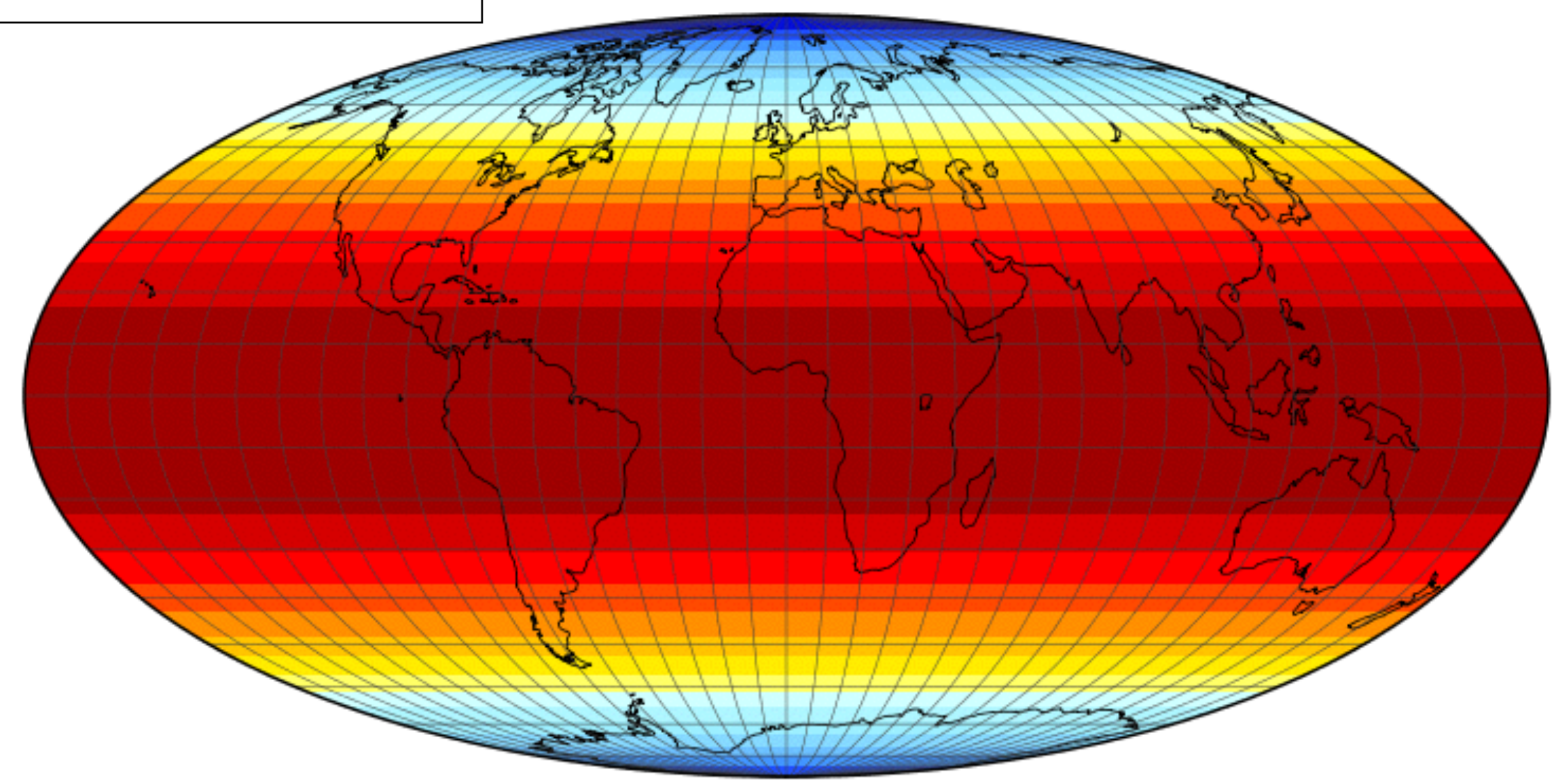


**solar energy received**

# Phenomena: Earth's radiative balance — the circulation driver

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Top of Atmosphere Insolation  
March 2003

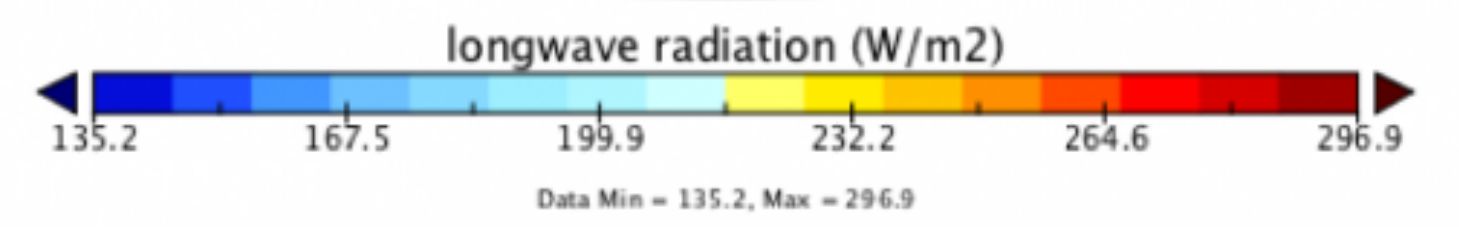
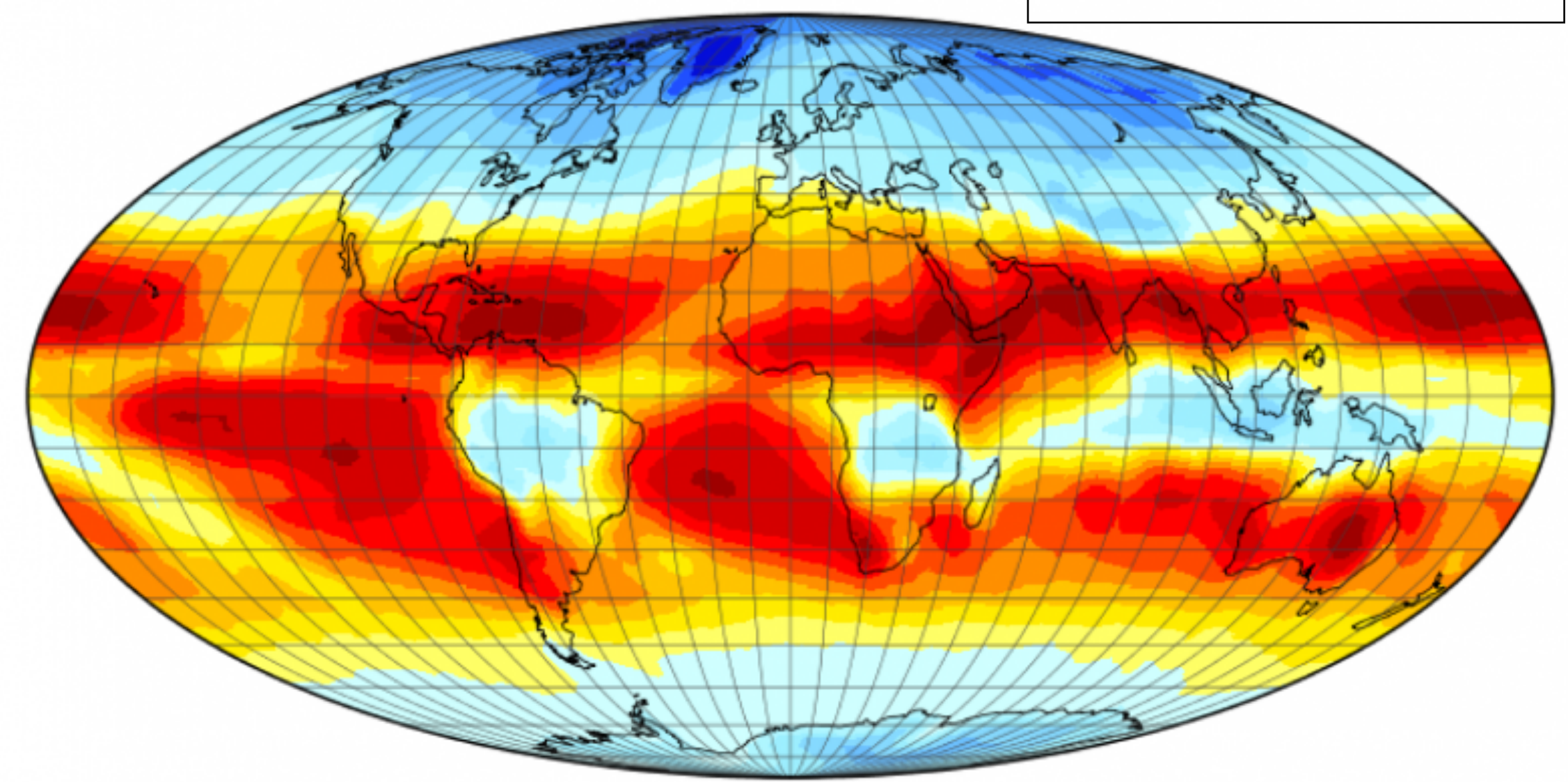


**solar energy received**

Stefan-Boltzmann Law:  
 $B(T) = \sigma T_e^4$

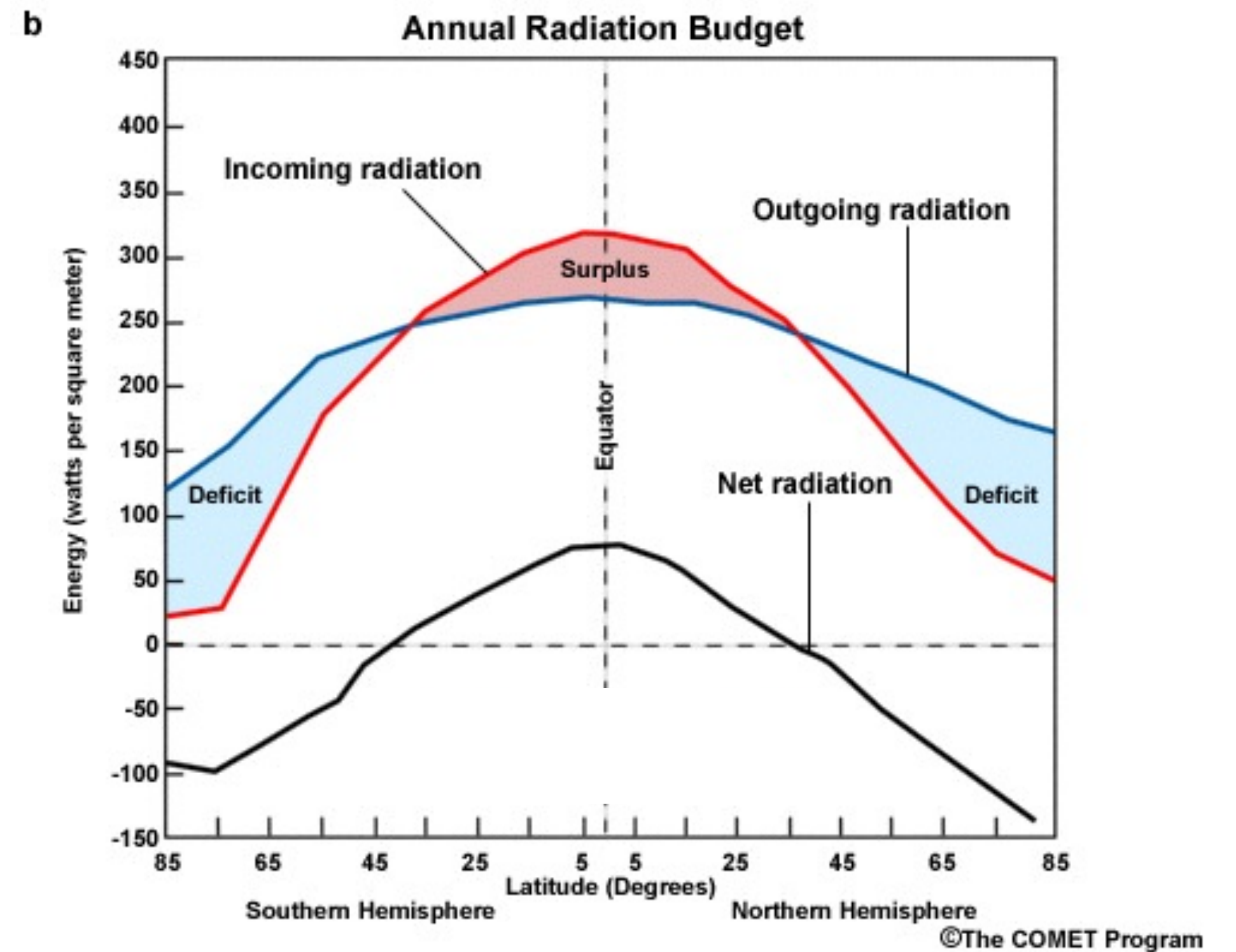
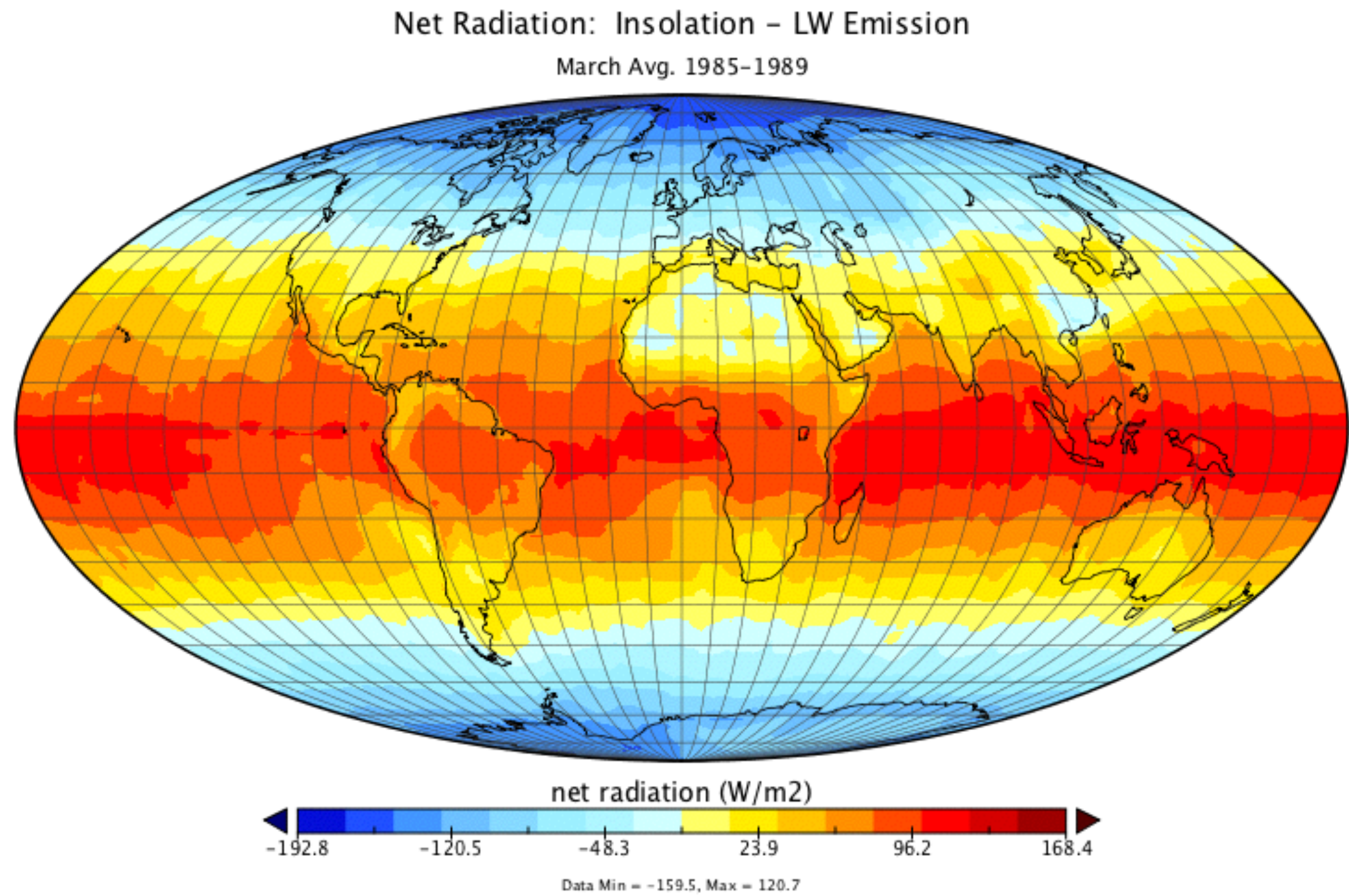
LW Energy Emitted  
March average for 1985-1989

NASA's ERBE satellite



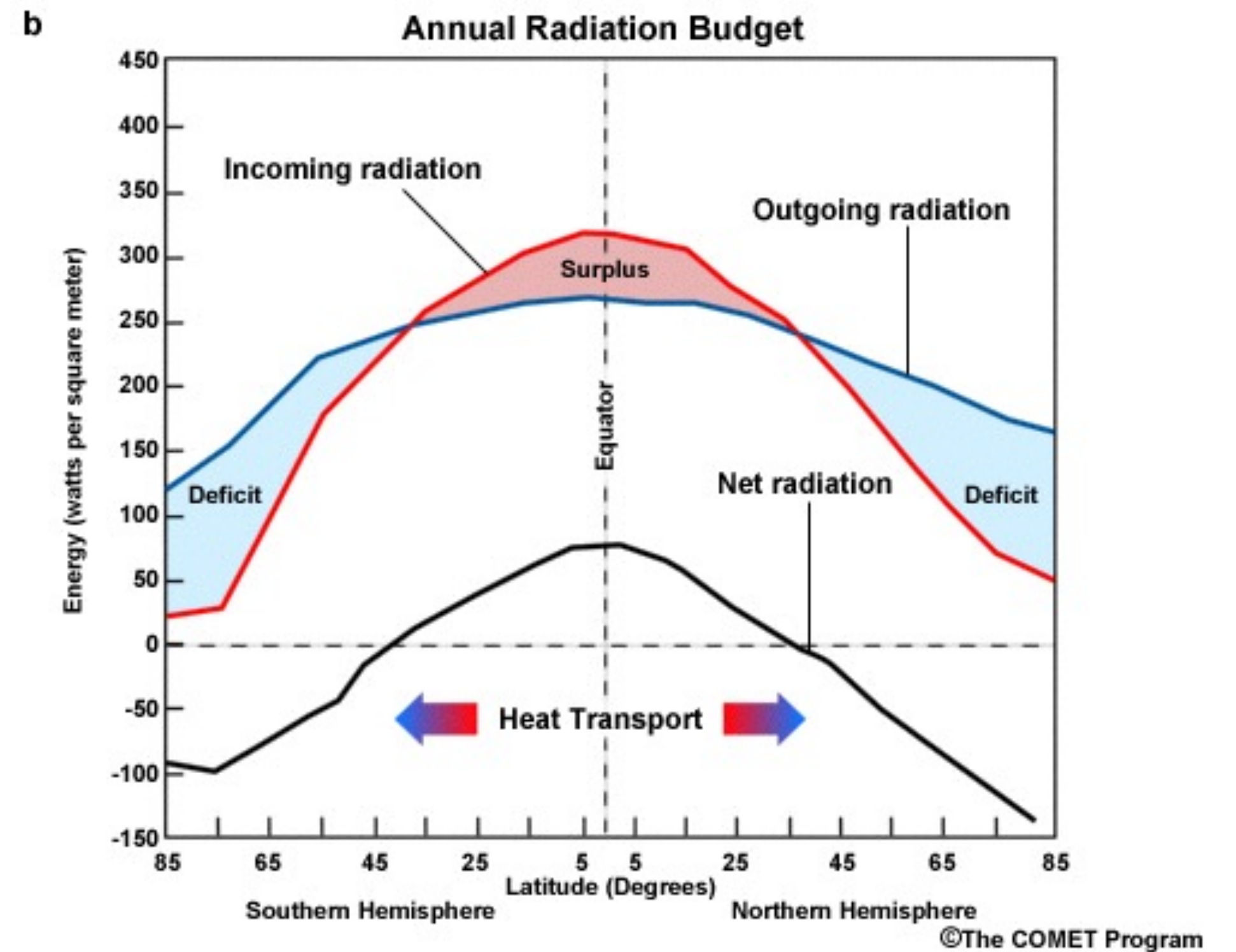
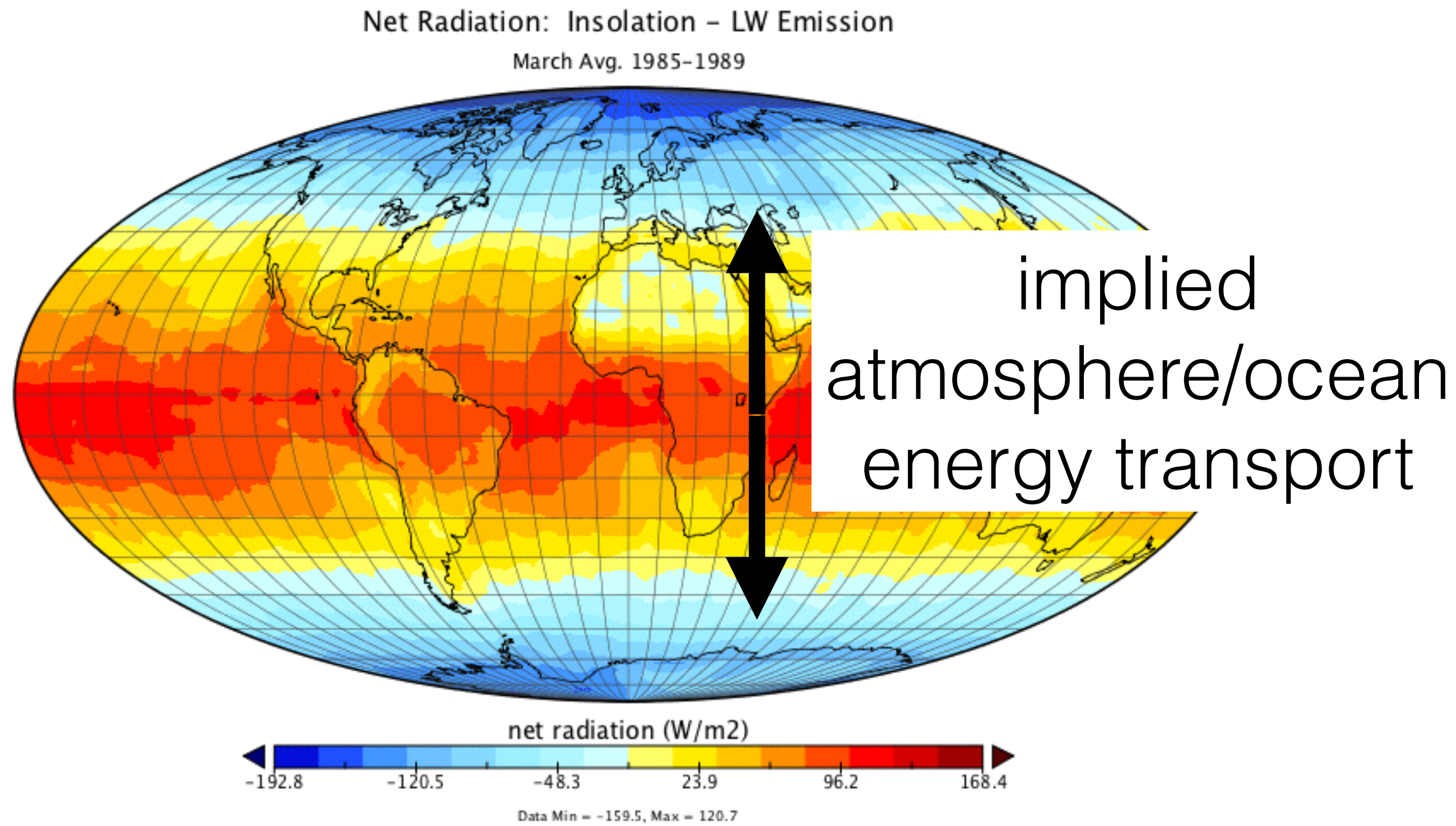
**terrestrial energy emitted**

# Phenomena: Earth's radiative balance — the circulation driver



**solar (SW) received minus terrestrial (LW) emitted**

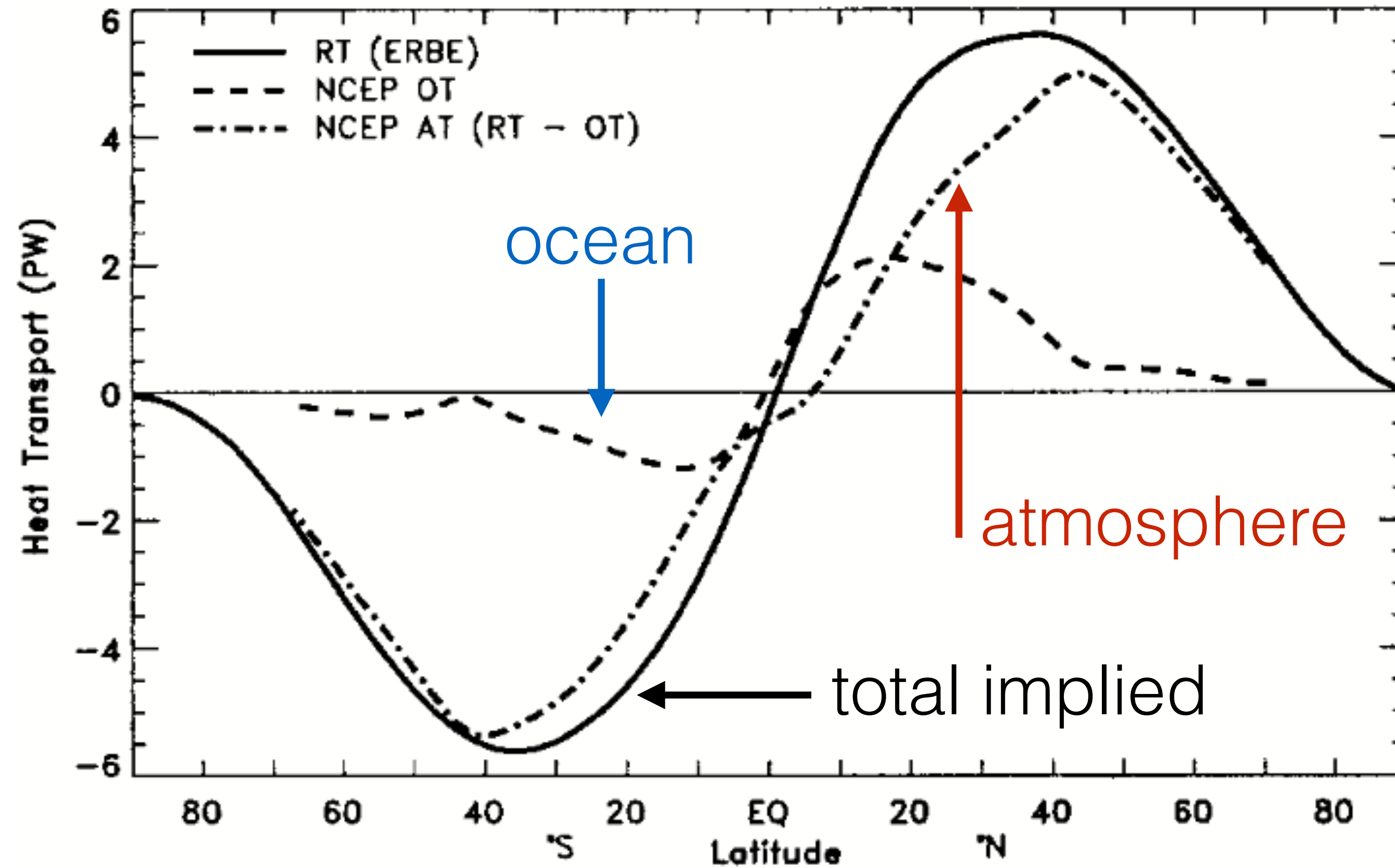
# Phenomena: Earth's radiative balance — the circulation driver



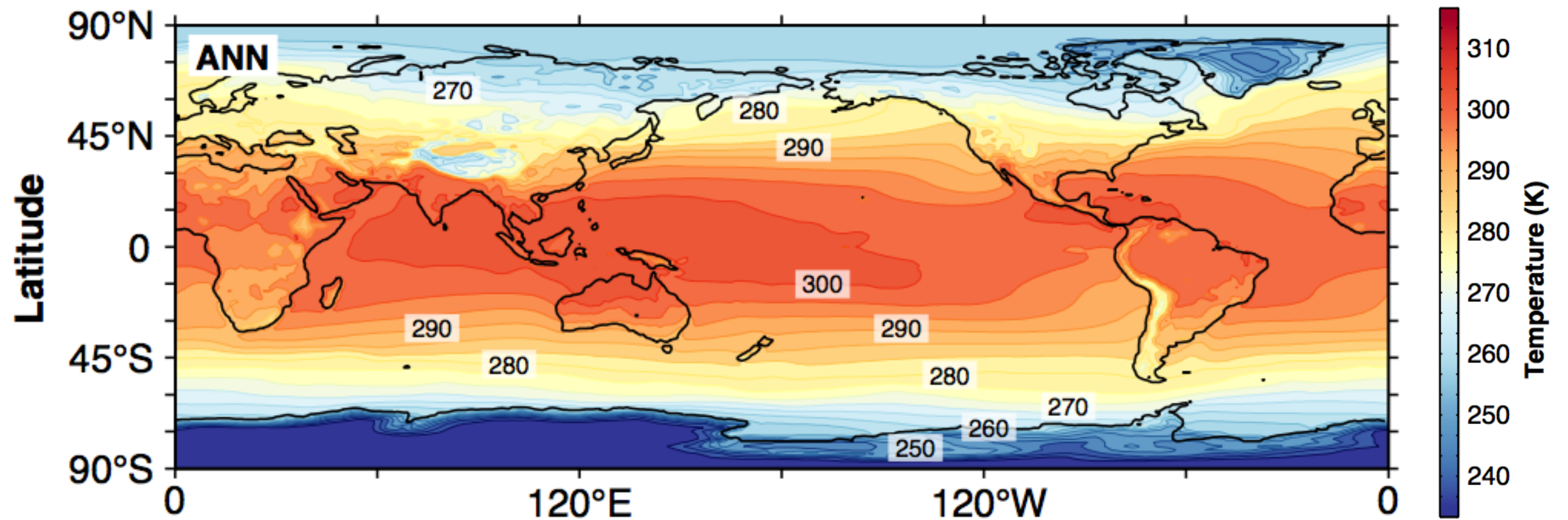
**solar (SW) received minus terrestrial (LW) emitted**



# Phenomena: Poleward energy transport by atmosphere and oceans

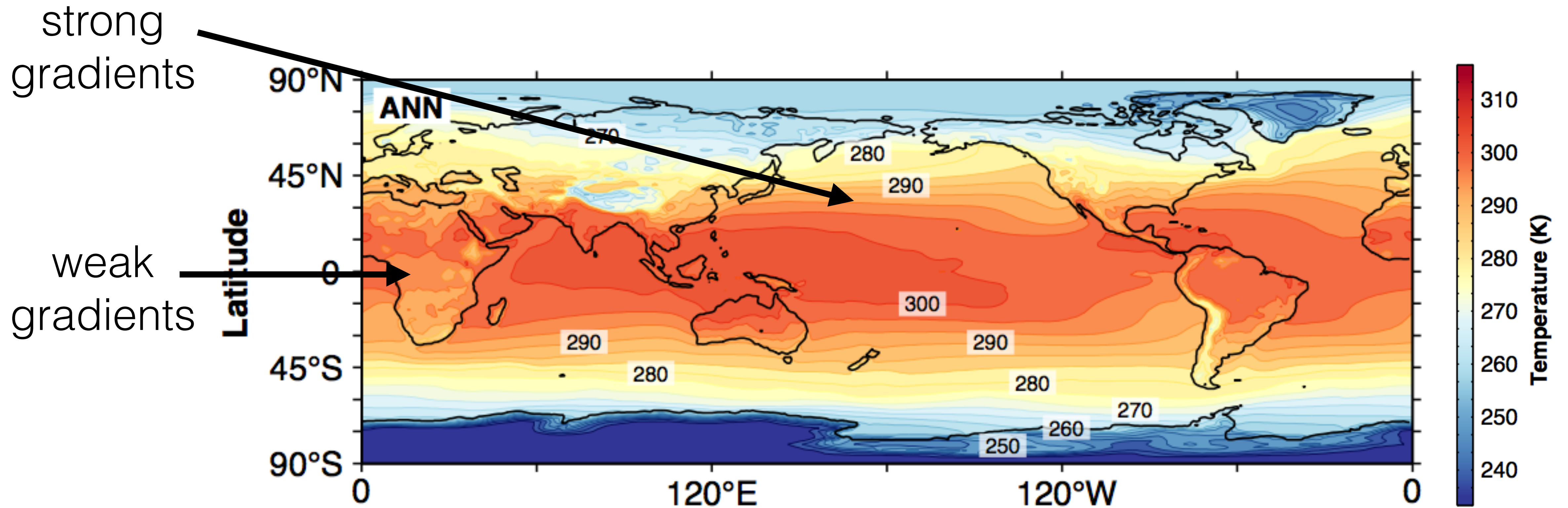


# Phenomena: Surface temperature $\leftrightarrow$ pressure gradients $\rightarrow$ circulations



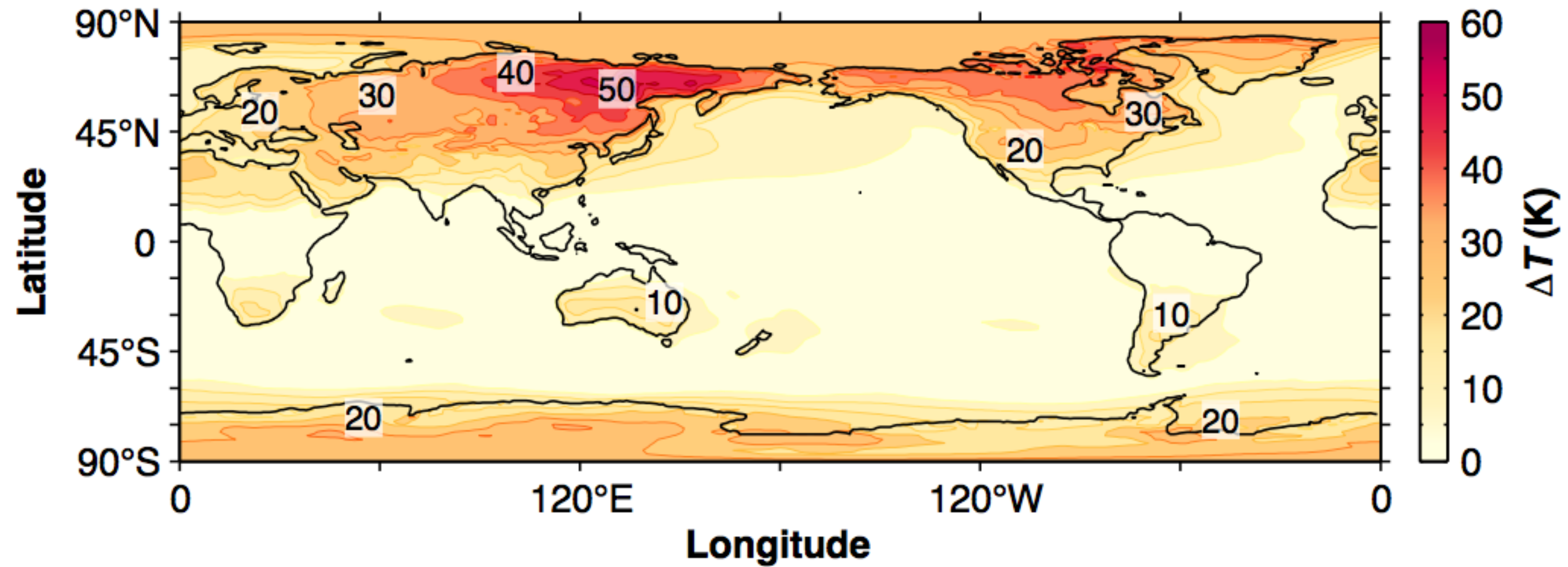
from Schneider's "Physics of Earth's Climate"

# Phenomena: Surface temperature $\leftrightarrow$ pressure gradients $\rightarrow$ circulations



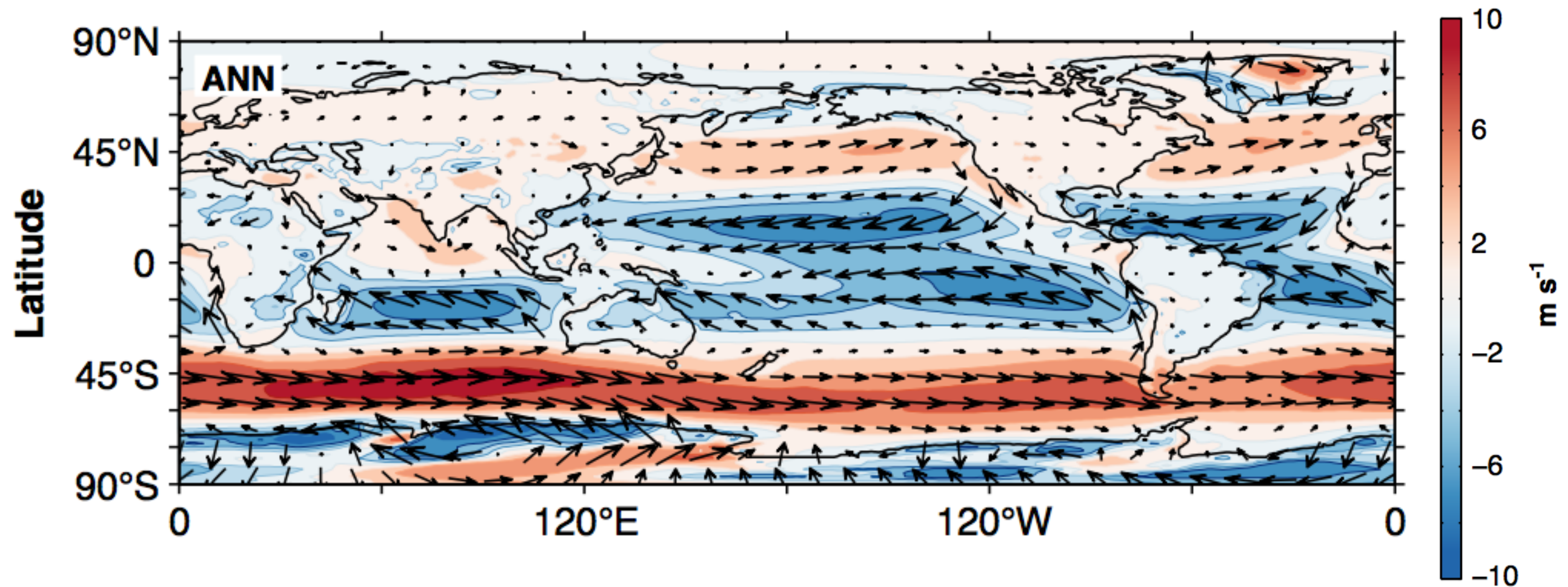
from Schneider's "Physics of Earth's Climate"

# Phenomena: Surface temperature (annual range)



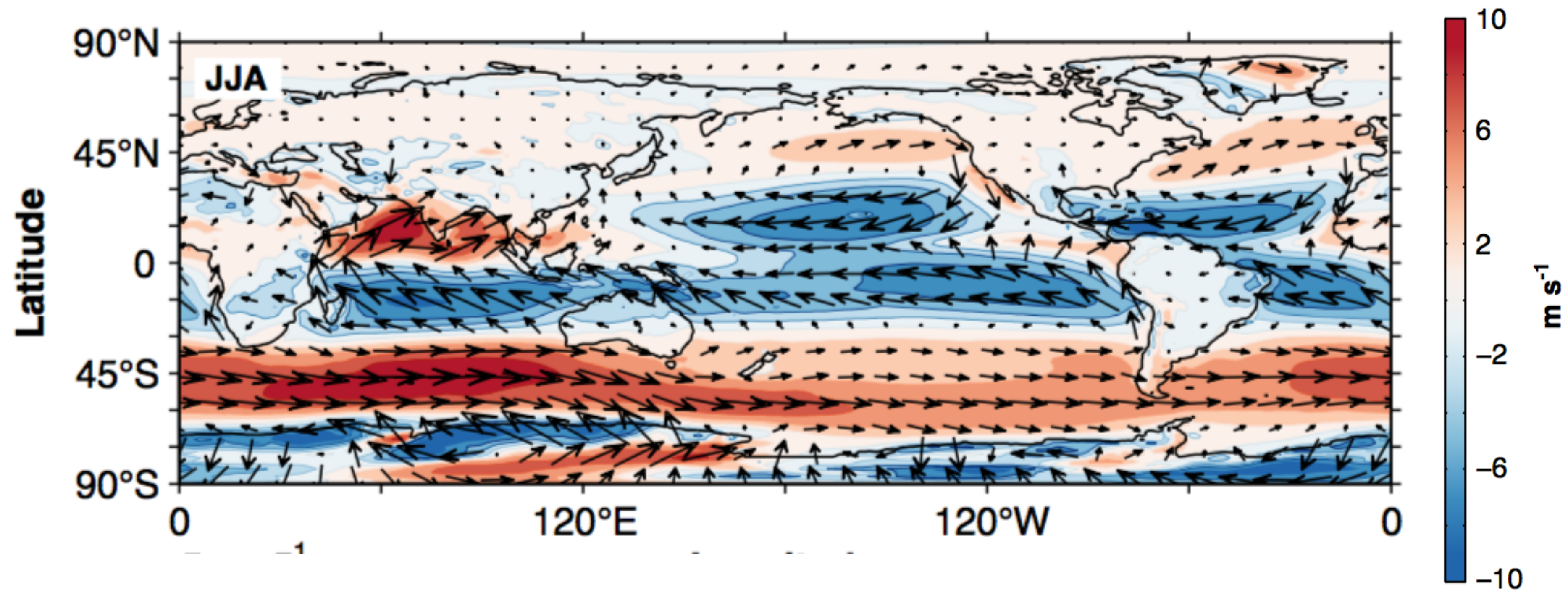
from Schneider's "Physics of Earth's Climate"

Phenomena: Annual-mean surface winds — much stronger in zonal direction because of Earth's rotation

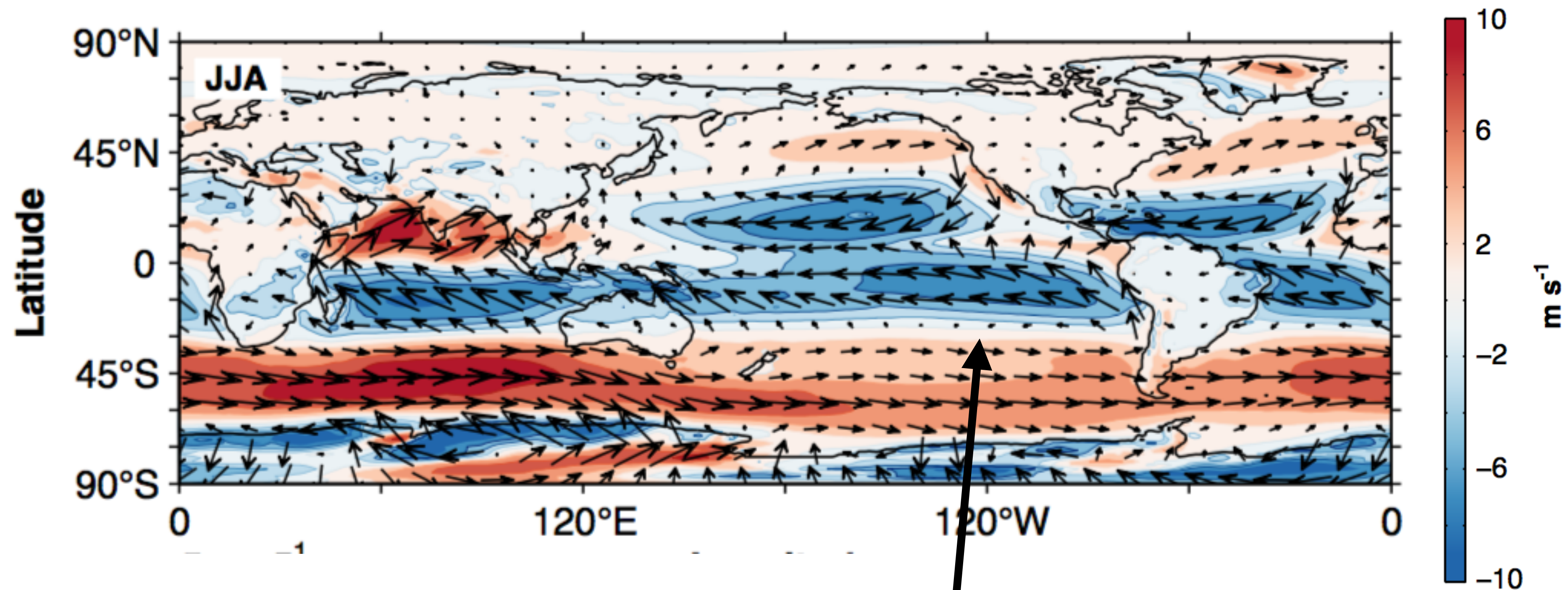


from Schneider's "Physics of Earth's Climate"

# Phenomena: NH summer (JJA) surface winds, winds vary with the seasons

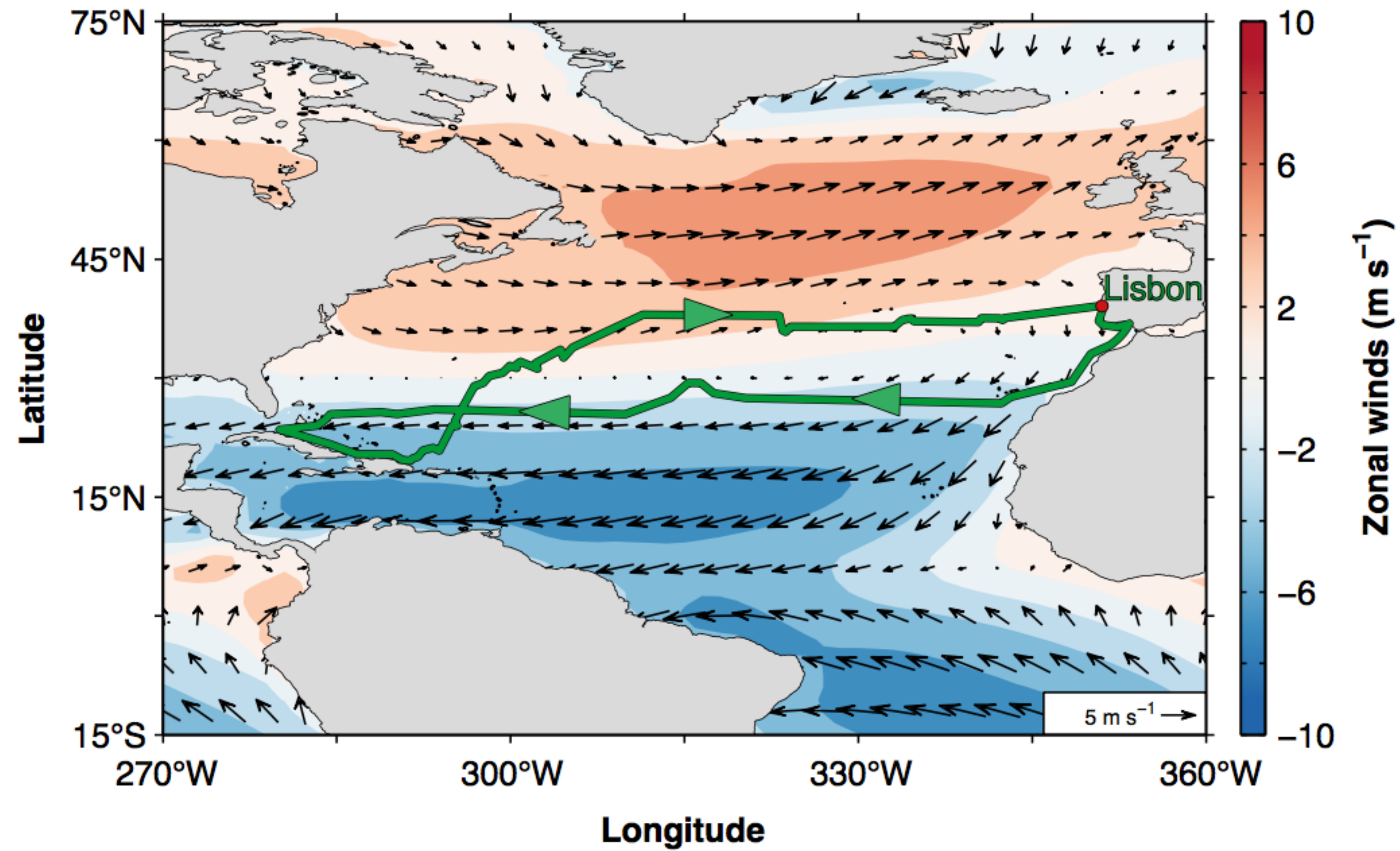


# Phenomena: NH summer (JJA) surface winds, winds vary with the seasons



“horse latitudes”

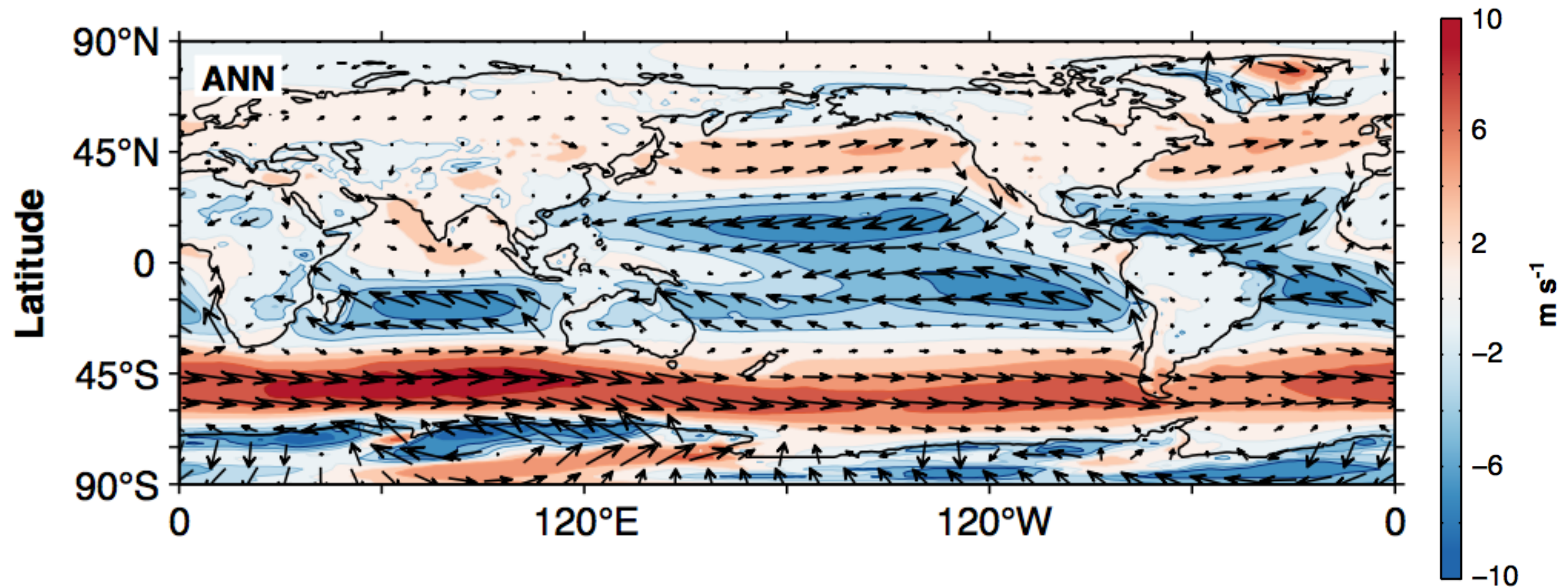
# Columbus knew about the surface-wind pattern



from Schneider's "Physics of Earth's Climate"

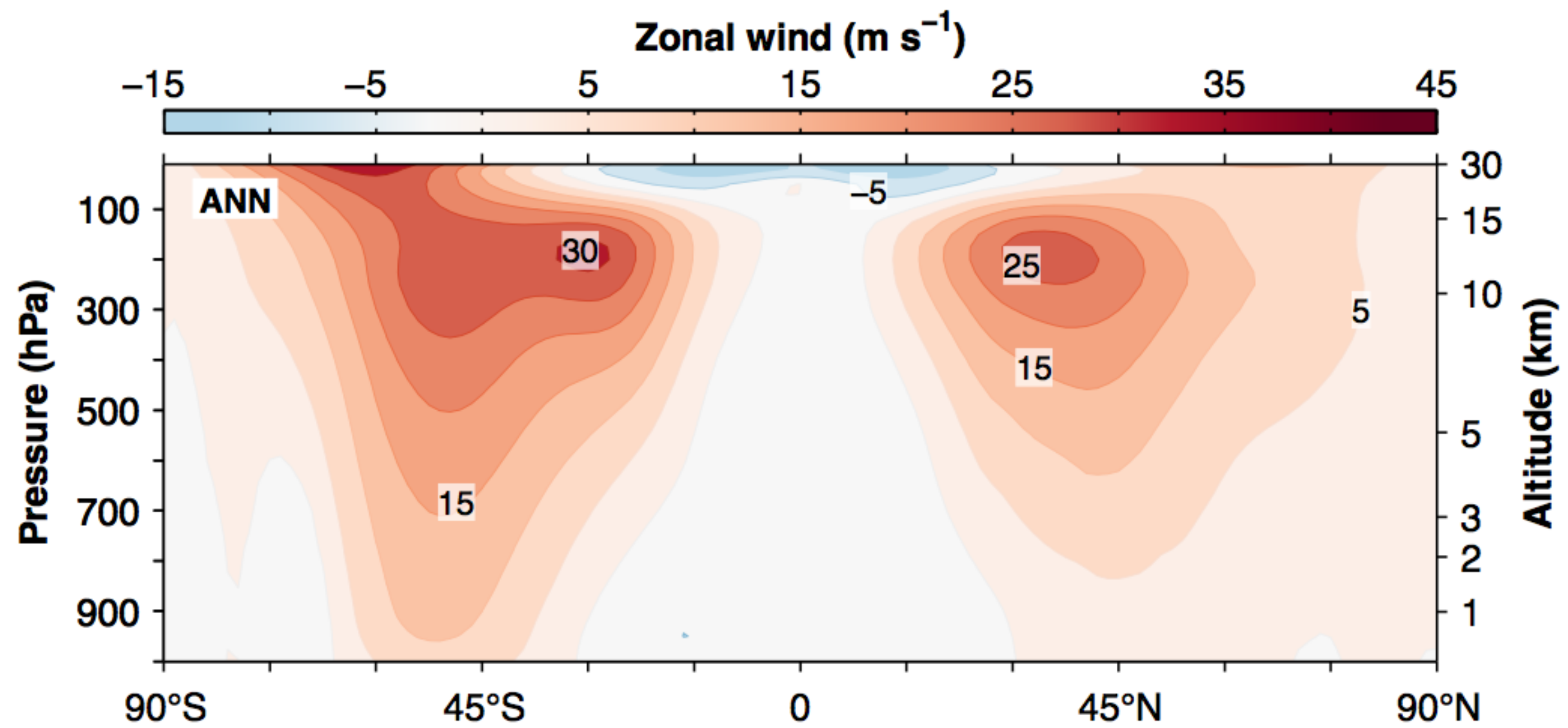


Phenomena: Meridional (north-south) winds are much weaker



from Schneider's "Physics of Earth's Climate"

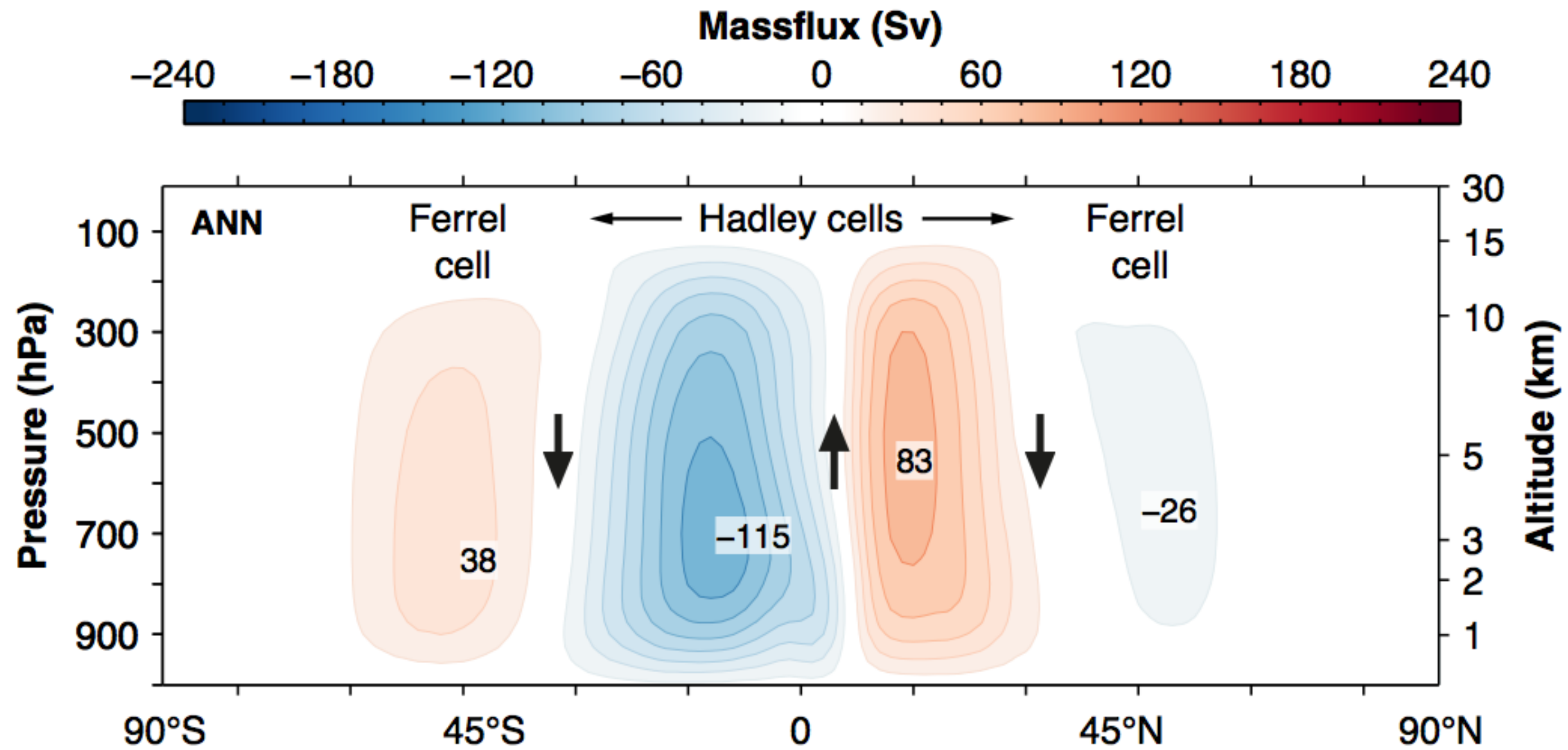
# Phenomena: Vertical structure of zonal winds



from Schneider's "Physics of Earth's Climate"

Phenomena: Vertical structure of meridional mass circulation  
— by mass balance, Hadley and Ferrel cells must exist!

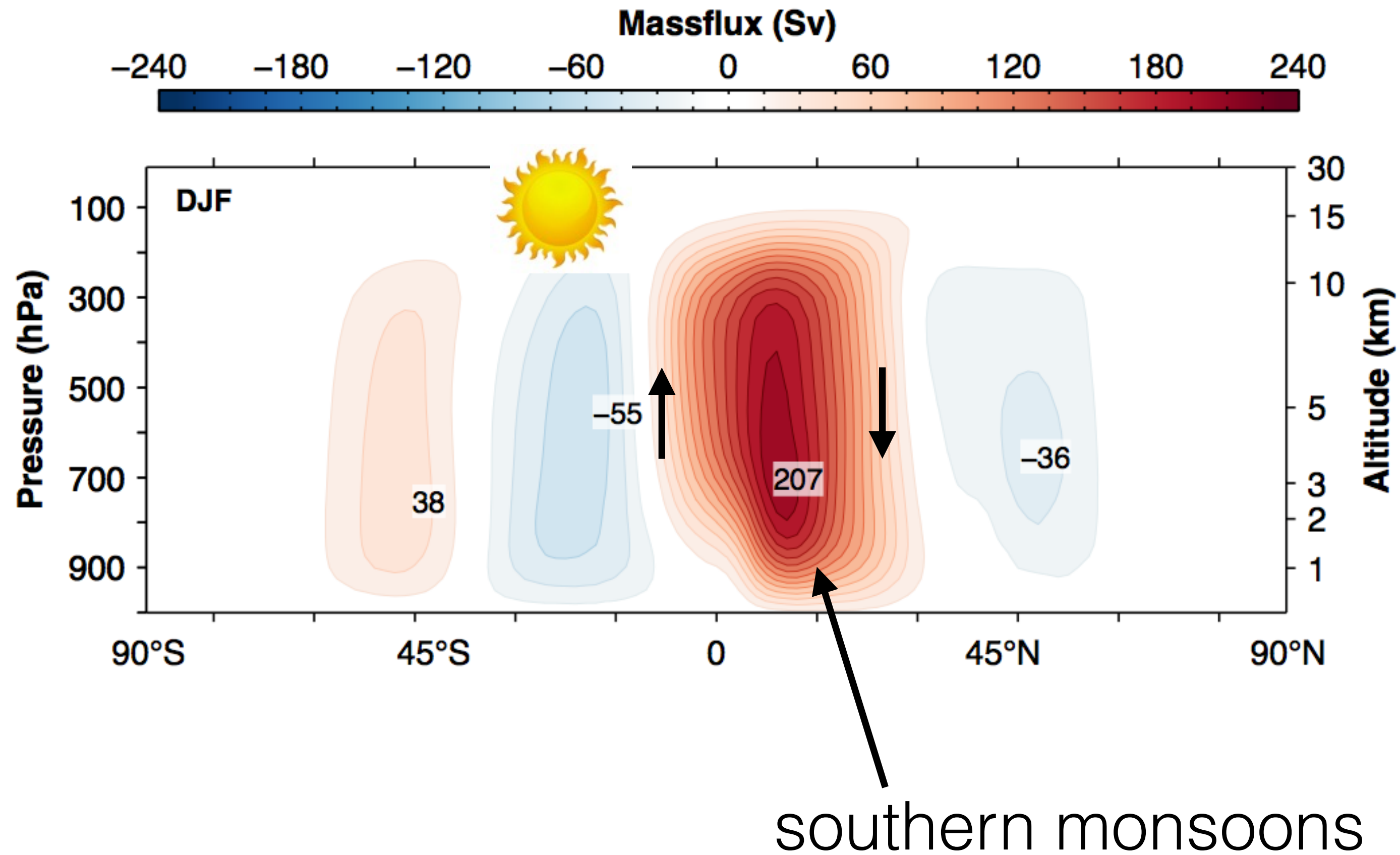
annual average



from Schneider's "Physics of Earth's Climate"

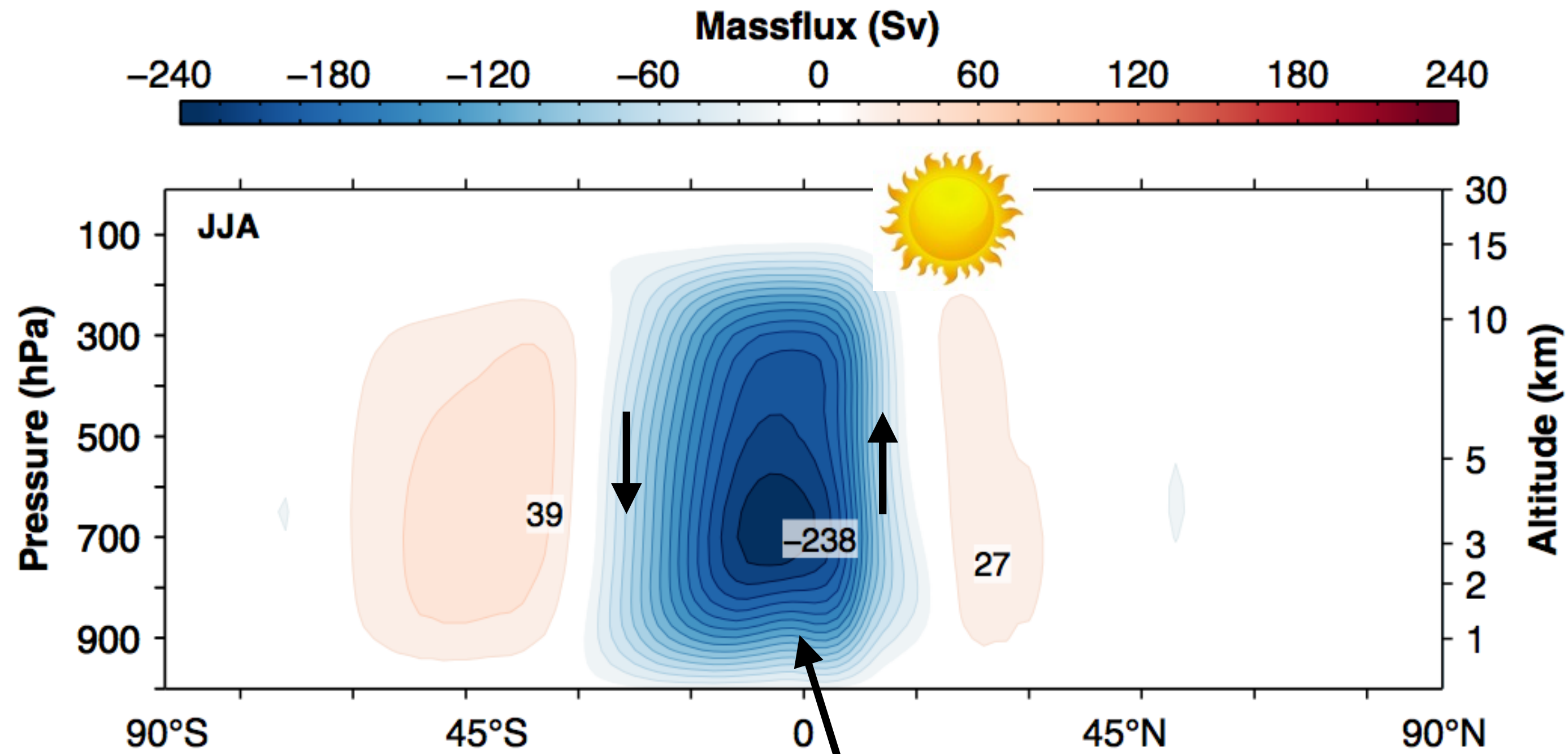
# Phenomena: Atmospheric meridional mass circulation — monsoons

**Dec-Jan-Feb**



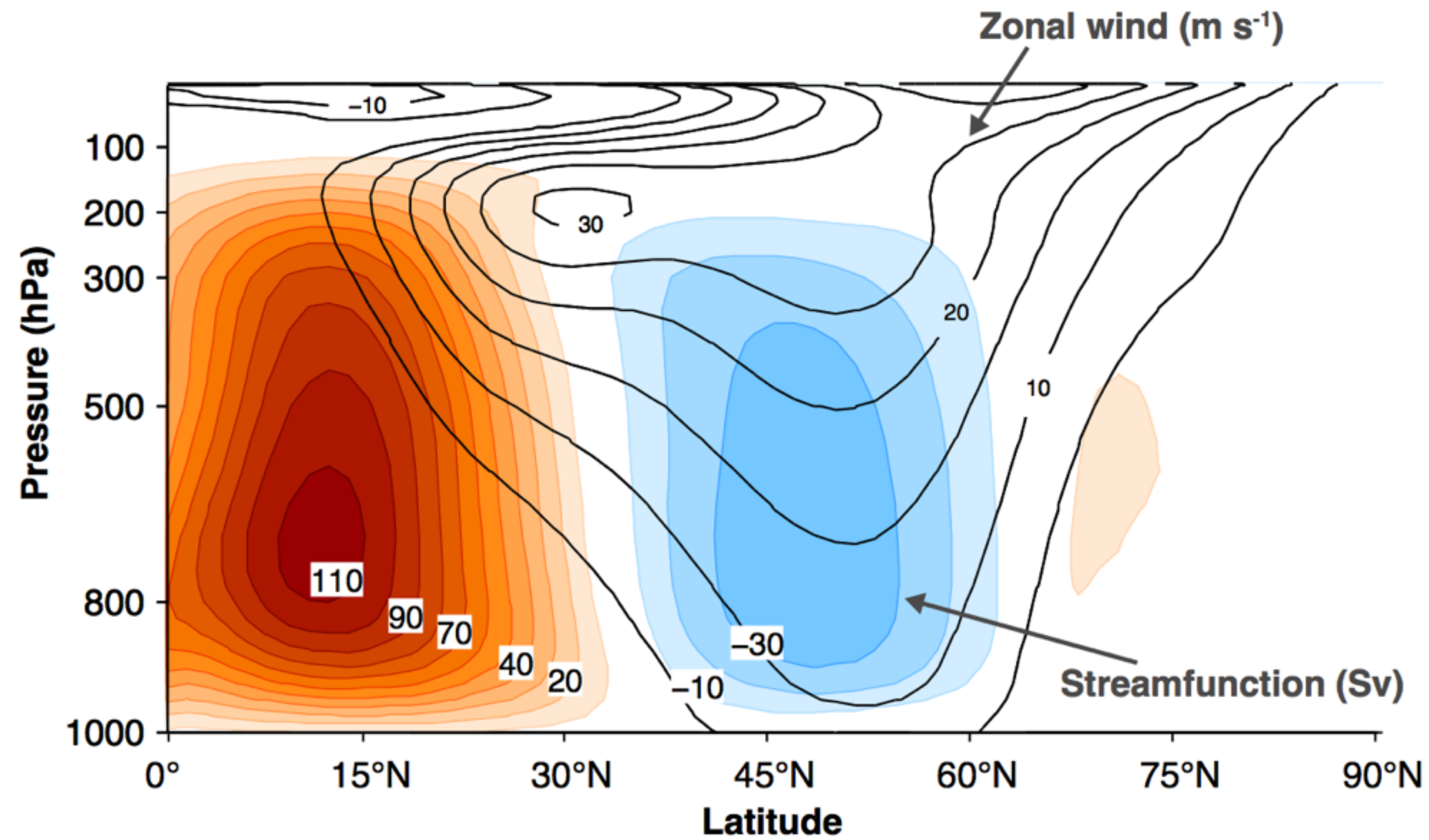
# Phenomena: Atmospheric meridional mass circulation — monsoons

**Jun-Jul-Aug**



northern monsoons (e.g. in India)

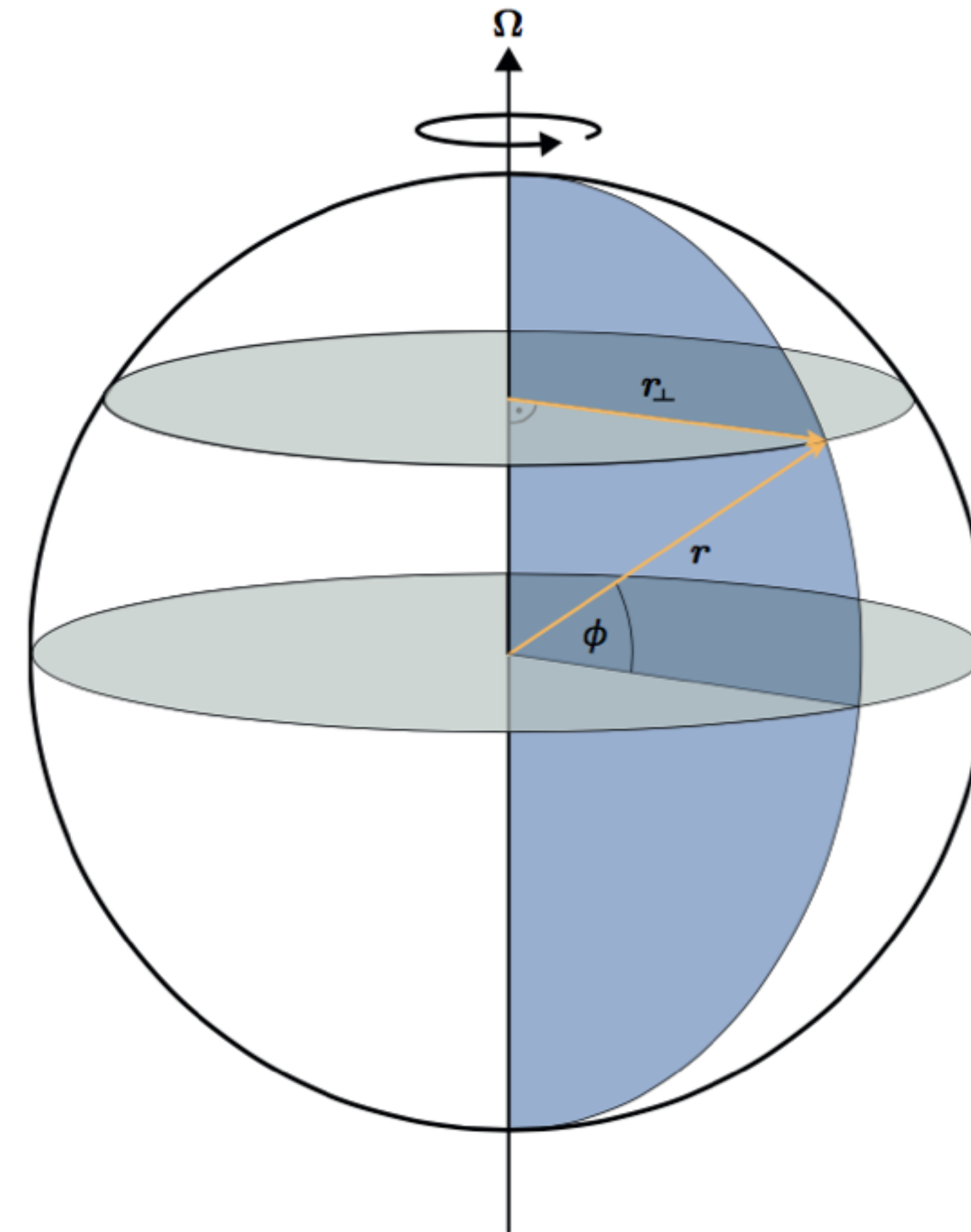
Why are there strong winds in the upper atmosphere? Why are these winds increasingly westerly as you move poleward? Angular momentum and Earth's rotation...



# Understanding winds and the Hadley circulation using angular momentum conservation

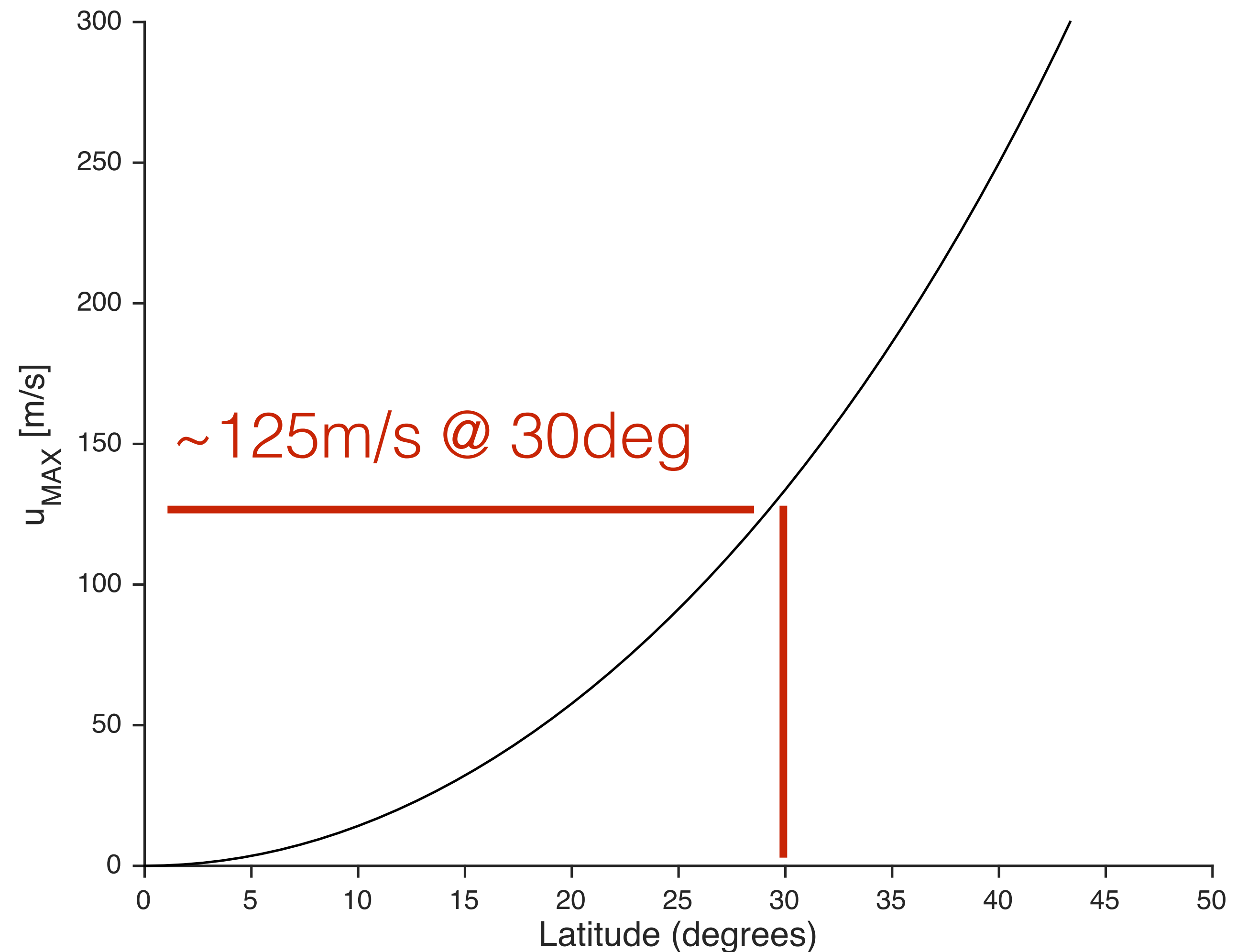
What is the angular momentum?  
“velocity times distance to rotation axis”

What does it imply for upper-tropospheric winds in Hadley cell?



Conservation of AM implies upper-level winds become stronger (more westerly) as air moves towards pole (opposite for surface winds)

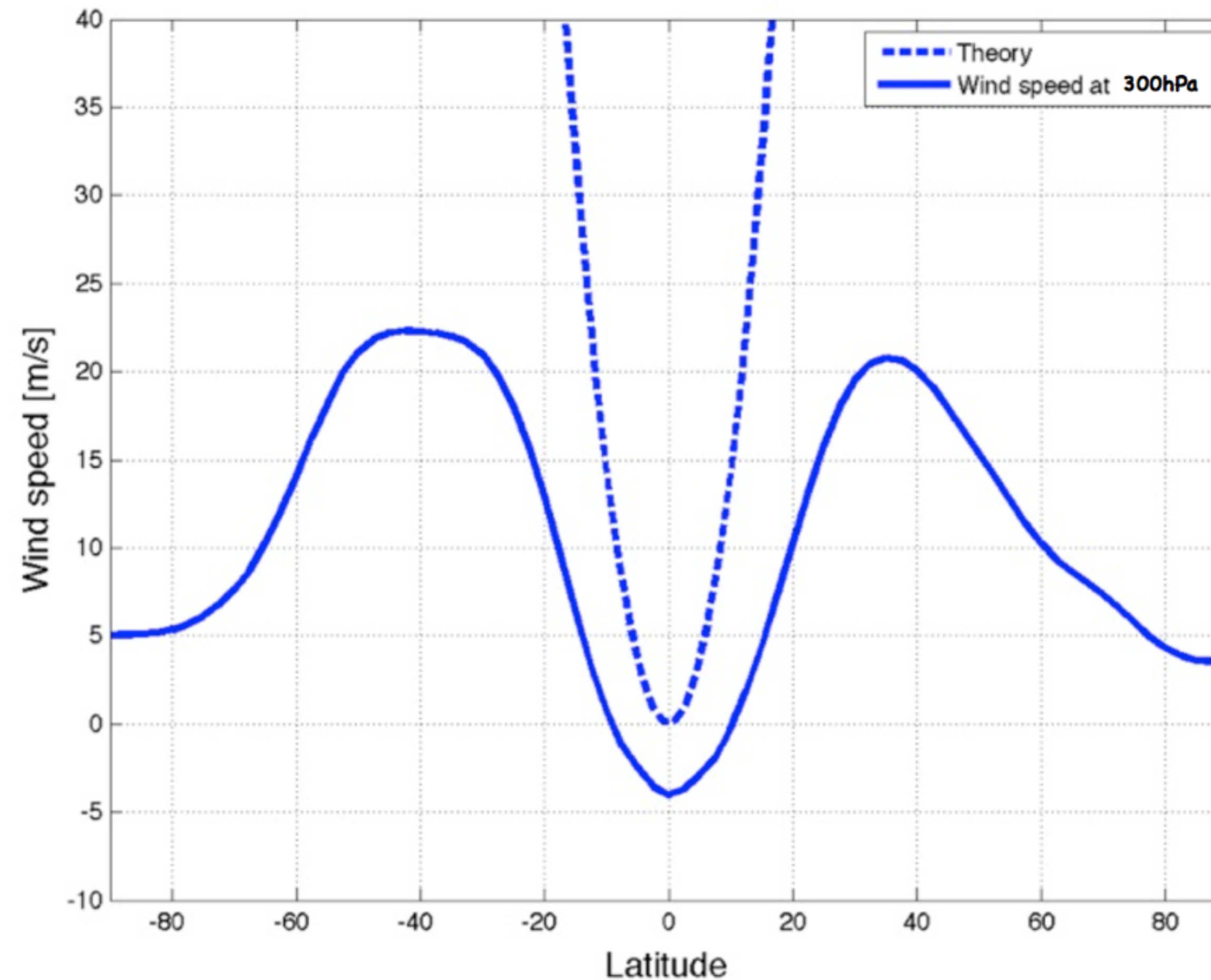
$$u_{\max} = \Omega a \frac{\sin^2 \phi}{\cos \phi}$$



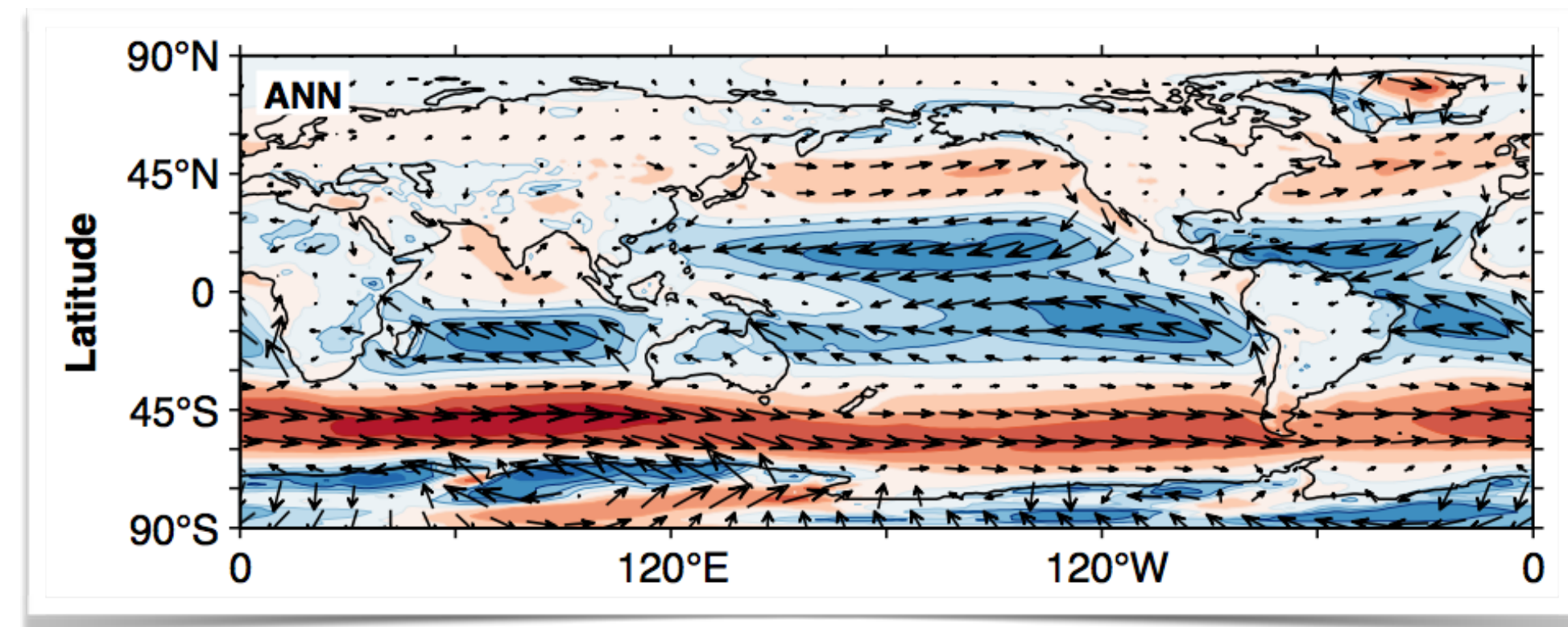
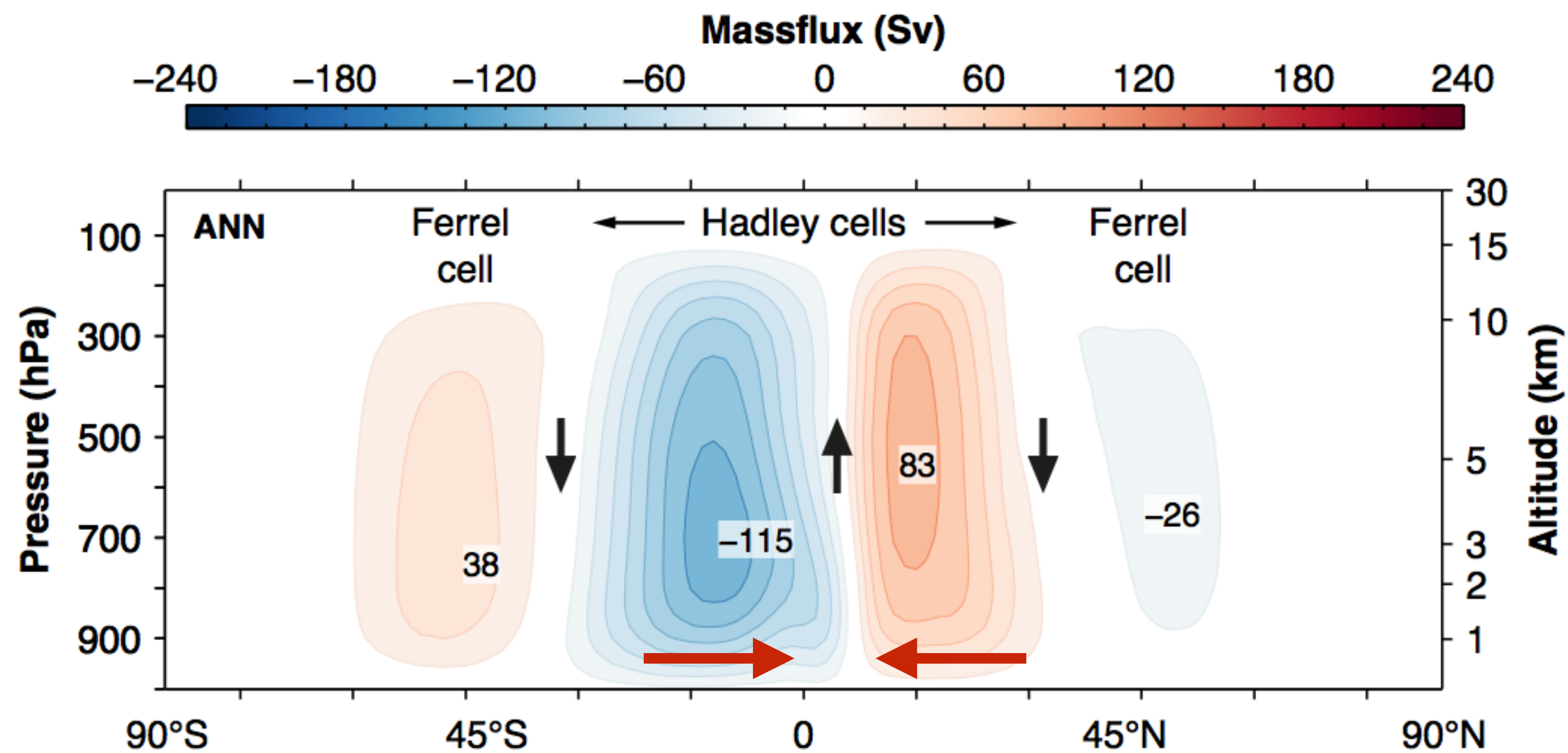


Implies infinite winds at the poles! AM conservation breaks down and Hadley circulation stops at ~30deg because of baroclinic instability and turbulence (see tomorrow's experiment)

$$u_{\max} = \Omega a \frac{\sin^2 \phi}{\cos \phi}$$



In surface branch AM is not conserved because of friction. Easterly winds transfer momentum to ocean and drive oceanic circulations -> Ekman layers



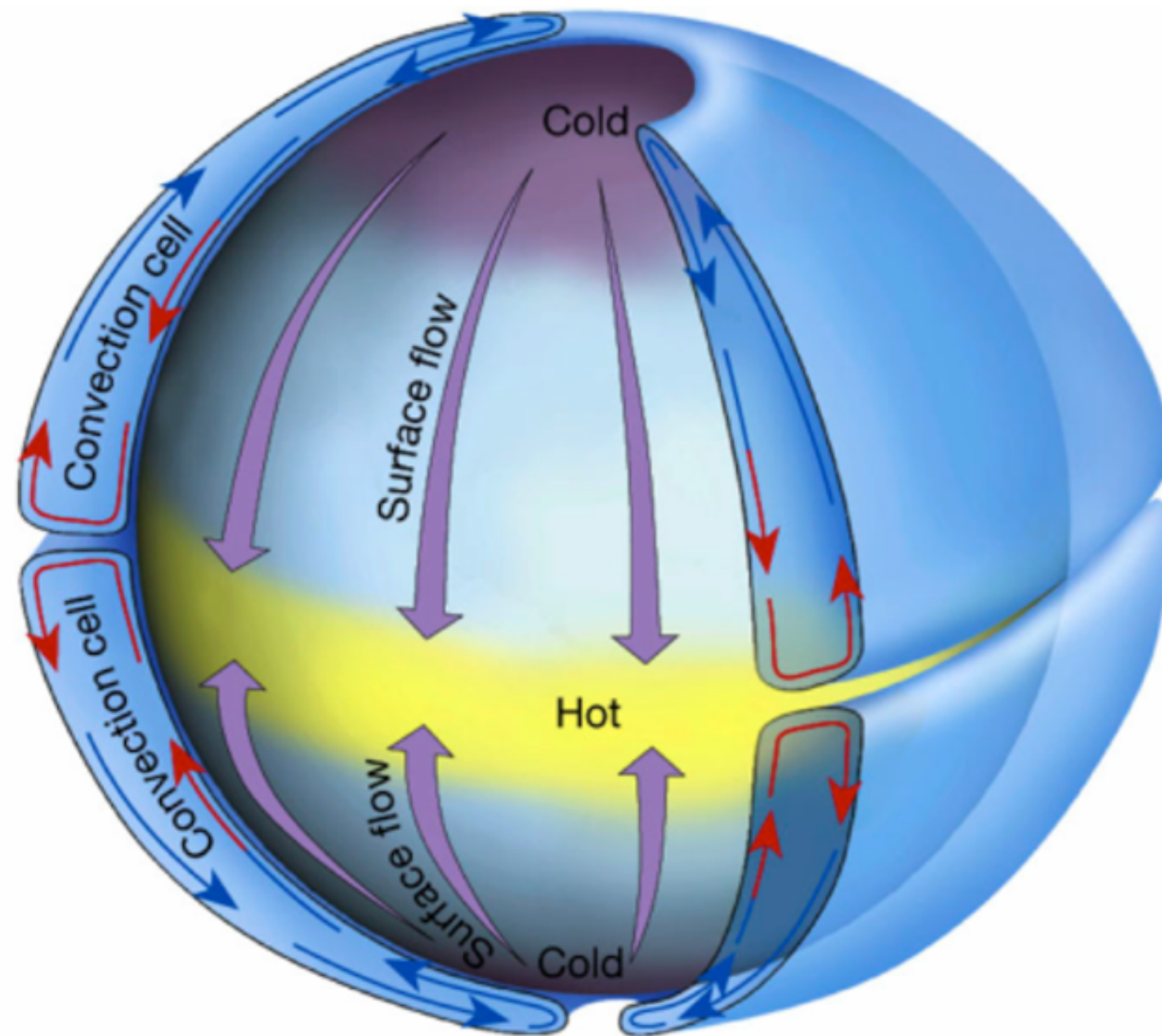
Ocean

# Ekman layers

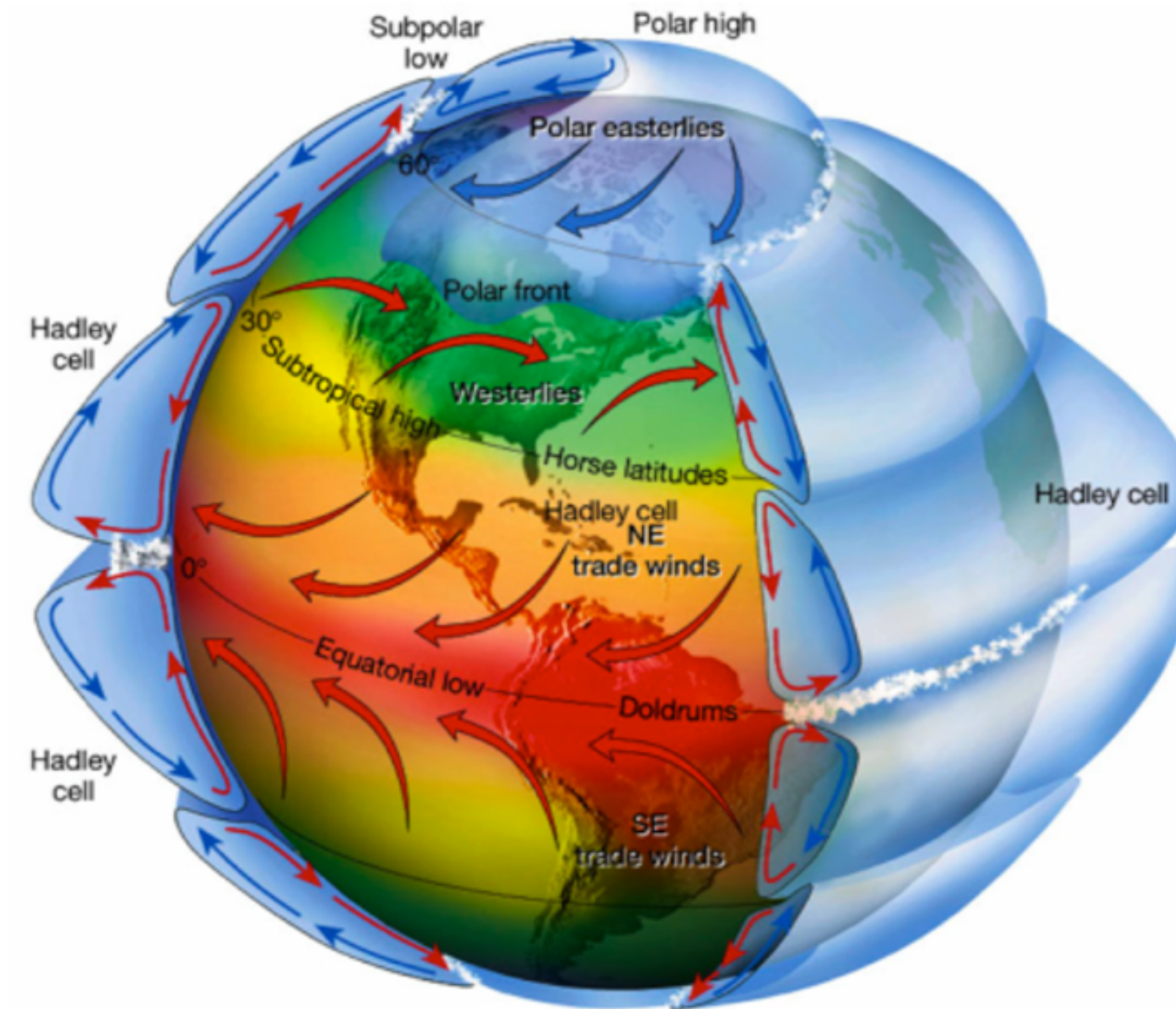
\*Arnaud's slides\*

# Breakdown of Hadley cell due to Earth's rotation

non-rotating



rotating



# Breakdown of Hadley cell due to Earth's rotation

Macroturbulence in an Earth-like simulation

Macroturbulence in a more realistic more

# Effect of Earth's rotation on atmosphere/ocean dynamics: The Rossby number

Can begin to understand the influence of rotation on circulation by doing a scale analysis of the momentum equation...

$$\frac{Du}{Dt} + \frac{1}{\rho} \frac{\partial p}{\partial x} - fv = \text{friction} \quad (\text{east} - \text{westdir.})$$

$$\frac{Dv}{Dt} + \frac{1}{\rho} \frac{\partial p}{\partial y} + fu = \text{friction} \quad (\text{north} - \text{southdir.})$$

acceleration

pressure-gradient  
force

Coriolis force

# Effect of Earth's rotation on atmosphere/ocean dynamics: The Rossby number

Can begin to understand the influence of rotation on circulation by doing a scale analysis of the momentum equation...

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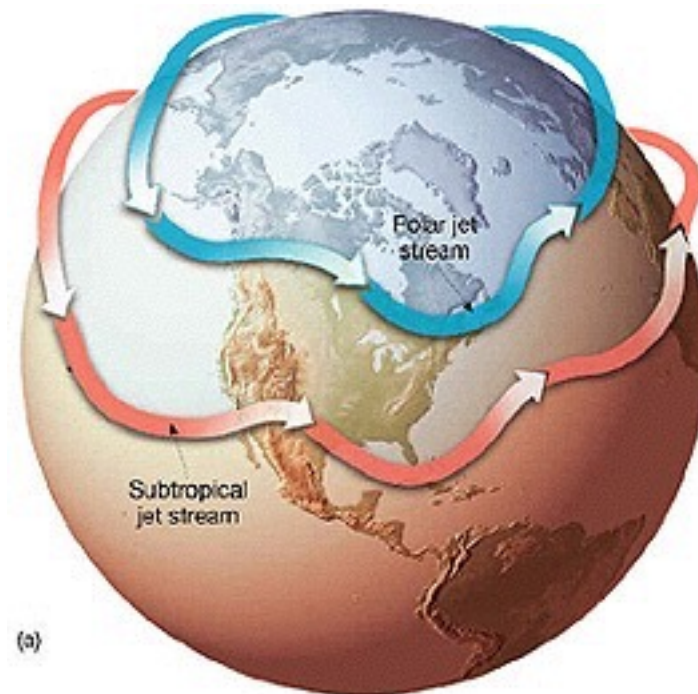
$$\sim V / T = V^2/L$$


$$\sim fV$$

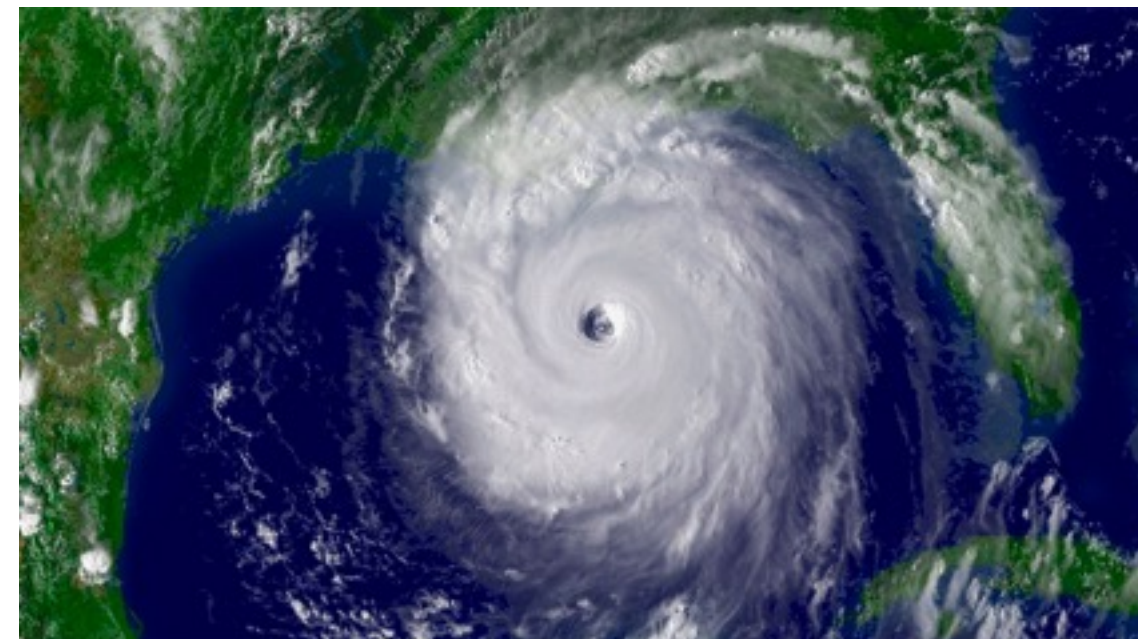

# Effect of Earth's rotation on atmosphere/ocean dynamics: The Rossby number

$$Ro = \frac{\text{acceleration}}{\text{Coriolis}} \sim \frac{V}{fL}$$

geostrophic  
balance (jet  
stream)



gradient balance  
(hurricanes)



cyclostrophic  
balance (tornados)



Ro = 0.1

1

10



# Geostrophic balance in Earth's atmosphere: Mid-latitude weather systems

$$Ro = \frac{\text{acceleration}}{\text{Coriolis}} \sim \frac{V}{fL} \approx 0.1$$

$$\Rightarrow f\hat{\mathbf{z}} \times \mathbf{u} + \frac{1}{\rho}\nabla p = 0$$

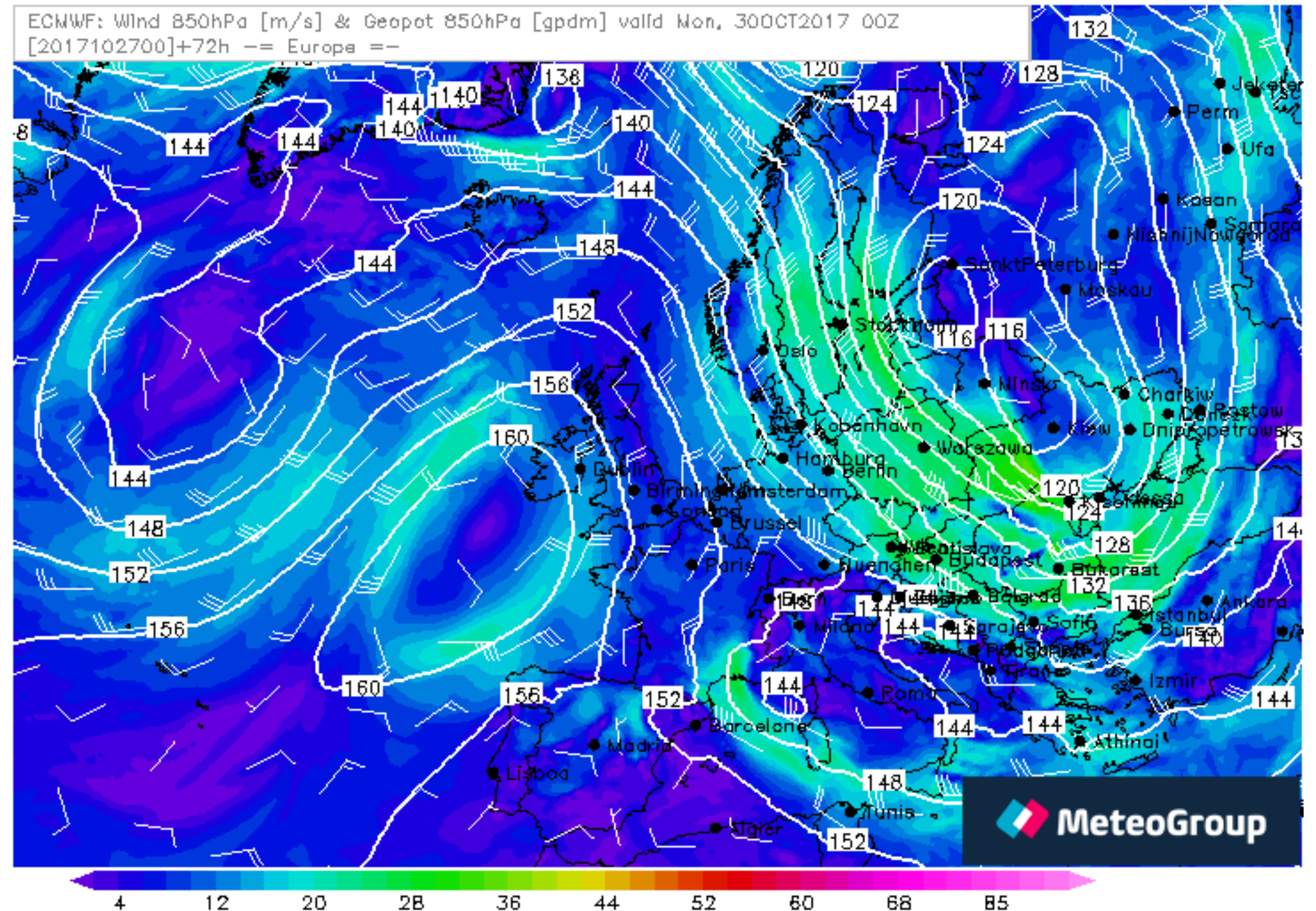
Geostrophic balance:  
“Pressure-gradient and  
Coriolis forces balance” ->  
flow along isobars

# Geostrophic balance in Earth's atmosphere: Mid-latitude weather systems

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Geostrophic balance:  
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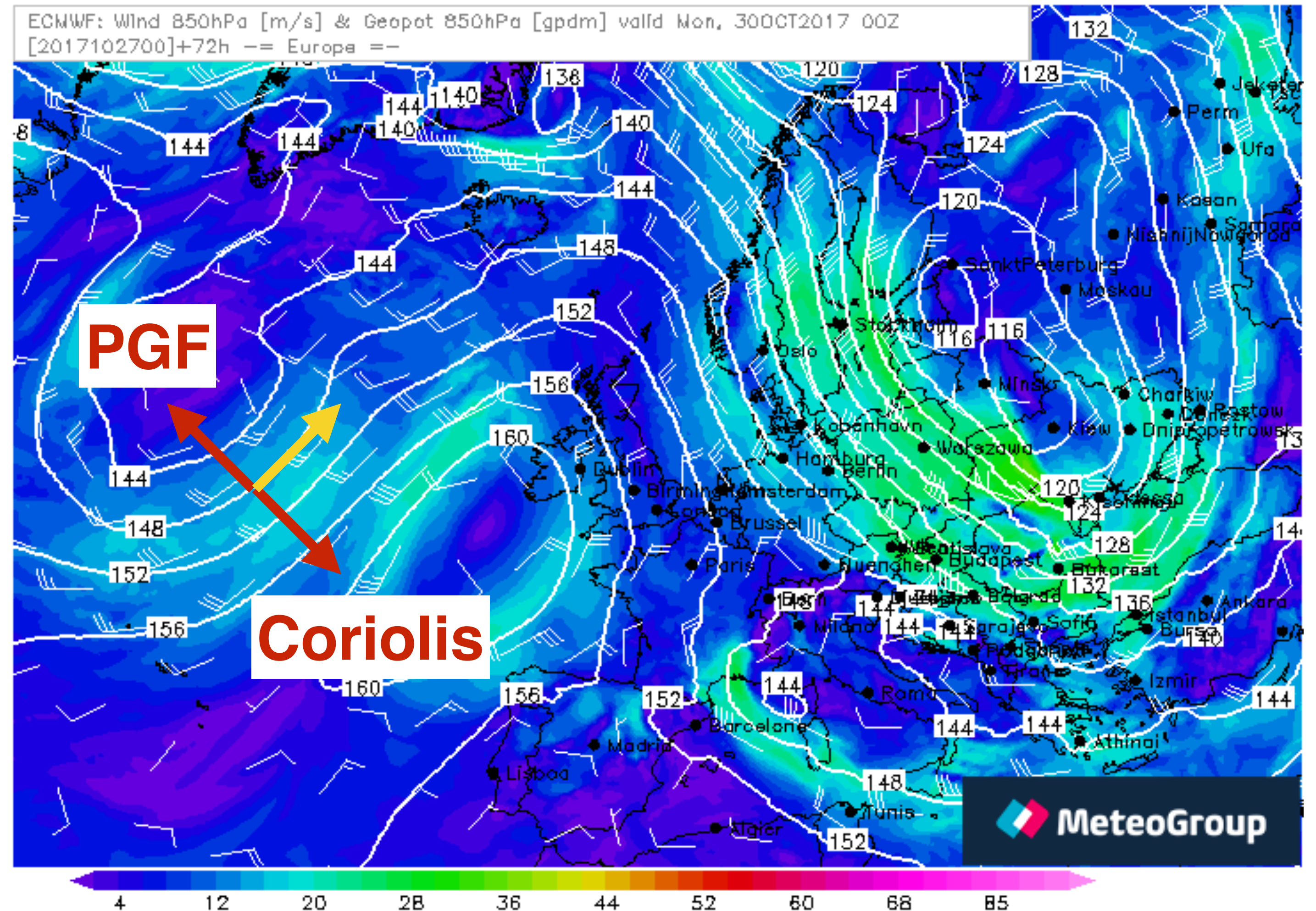


# Geostrophic balance in Earth's atmosphere: Mid-latitude weather systems

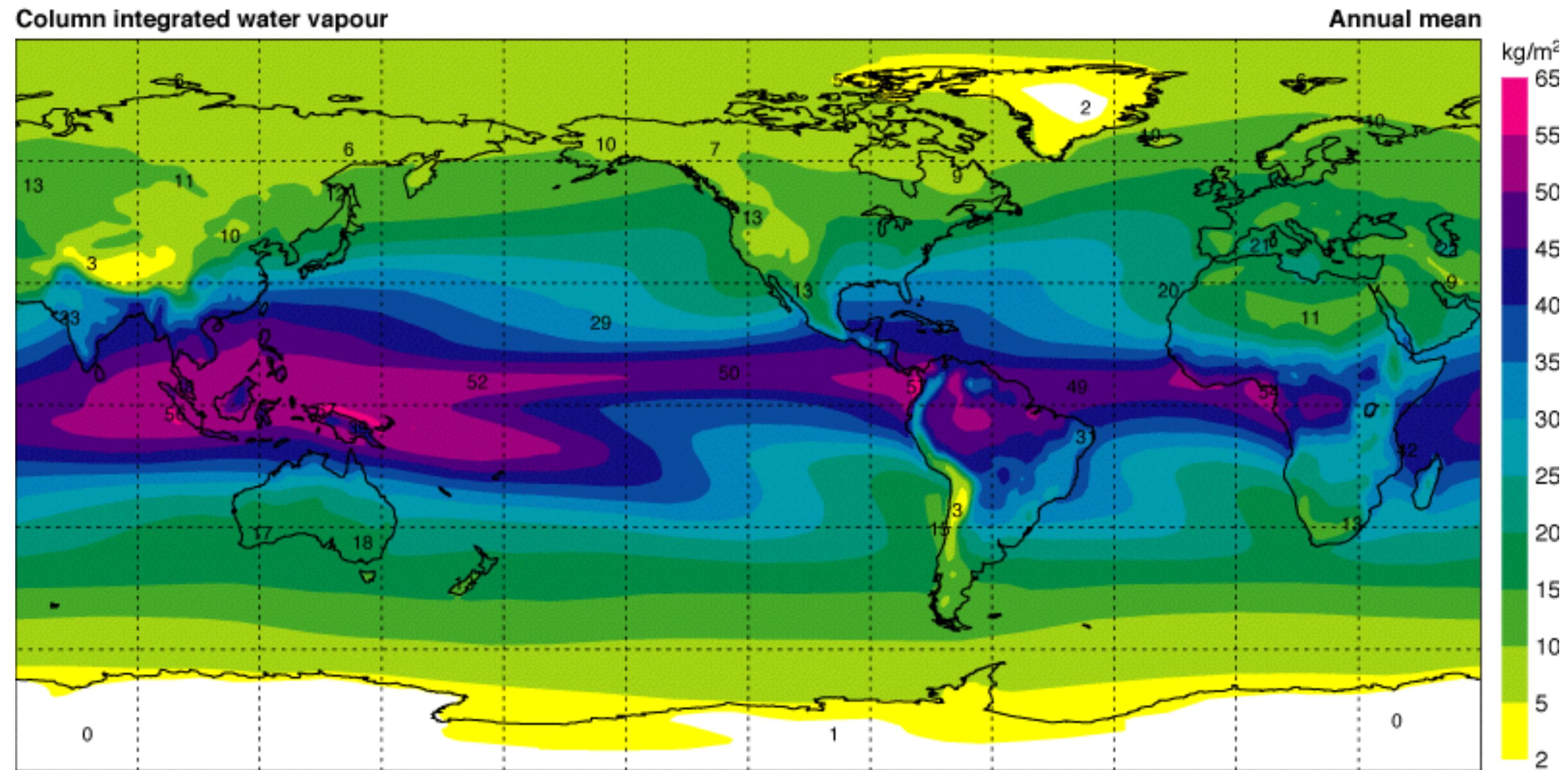
$$Ro = \frac{\text{acceleration}}{\text{Coriolis}} \sim \frac{V}{fL} \approx 0.1$$

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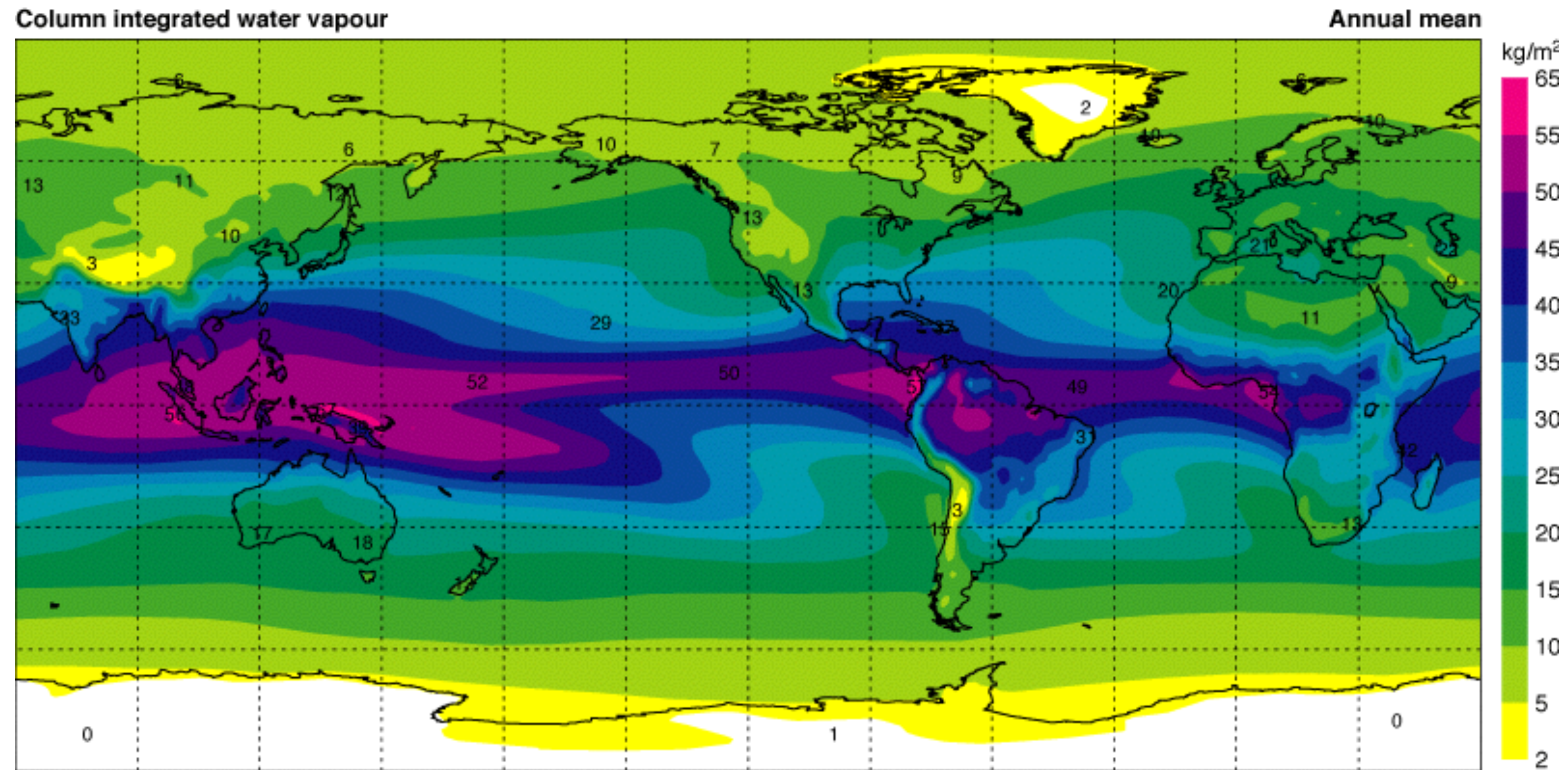
Geostrophic balance:  
“Pressure-gradient and  
Coriolis forces balance”



# Earth's water cycle: atmospheric water vapour



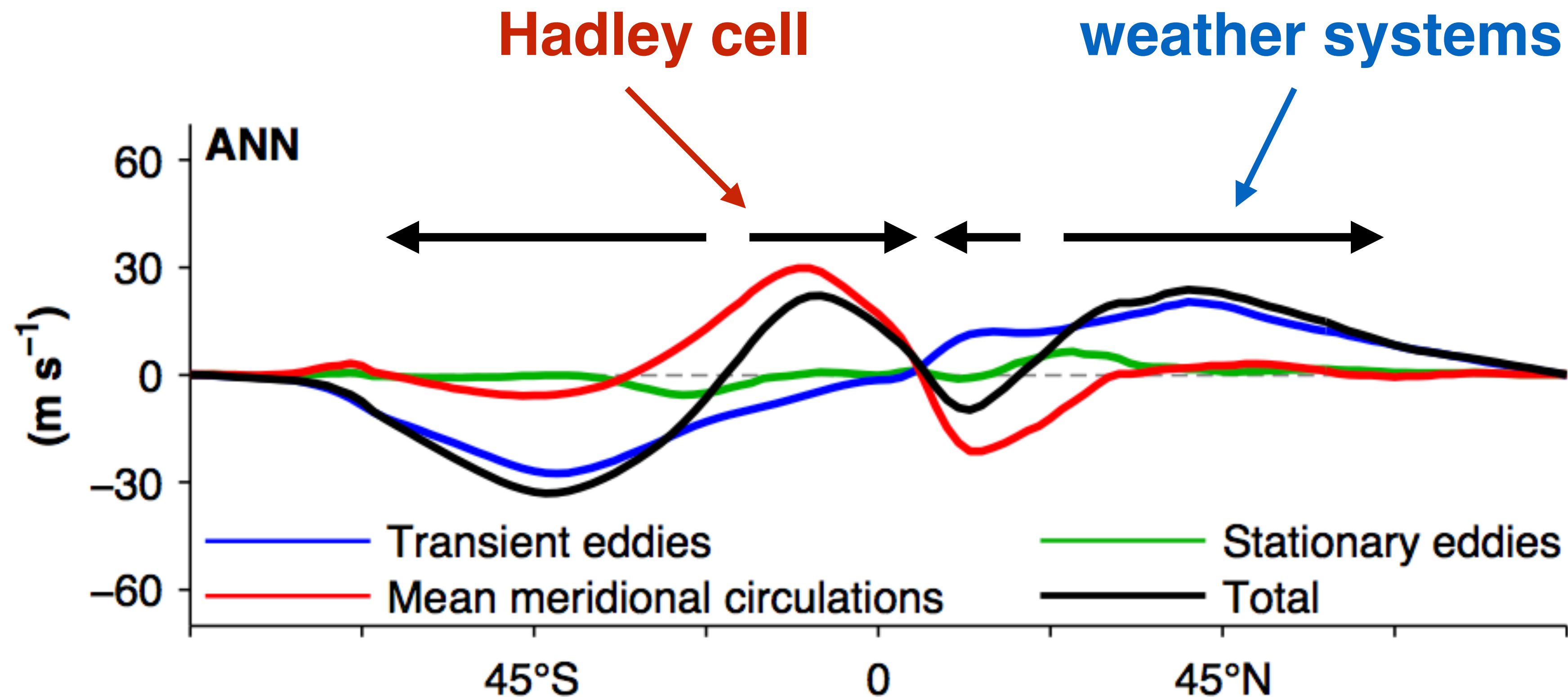
# Earth's water cycle: atmospheric water vapour



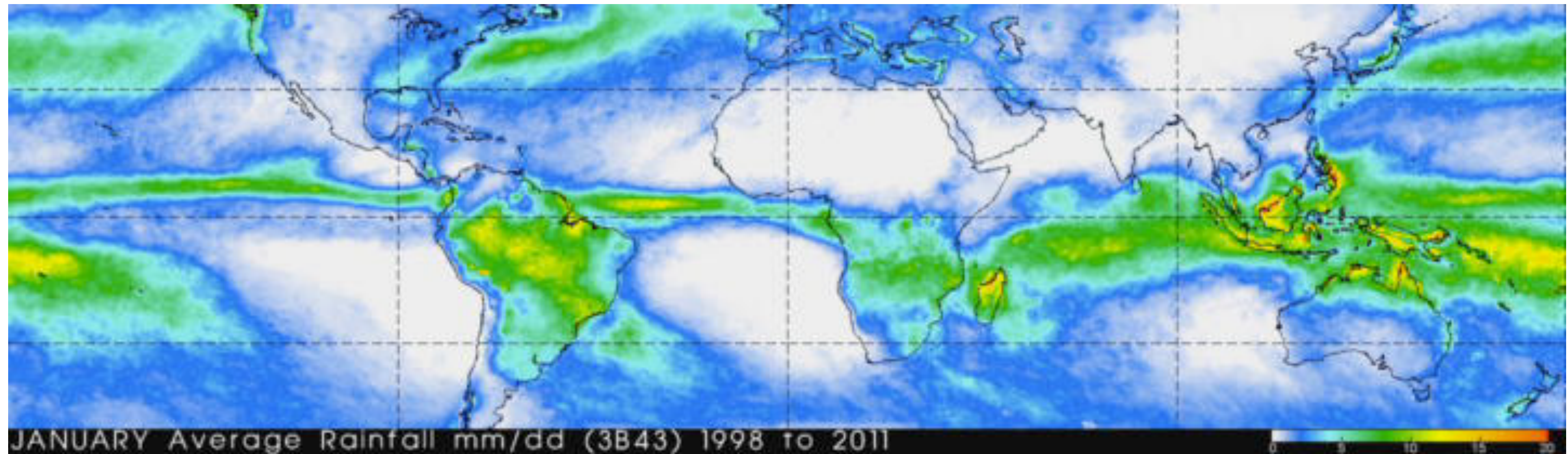
Clausius-Clapeyron:  $\frac{\delta q^*}{q^*} \approx \frac{L}{RT^2} \delta T$

← 7%/K

# Earth's water cycle: moisture transport

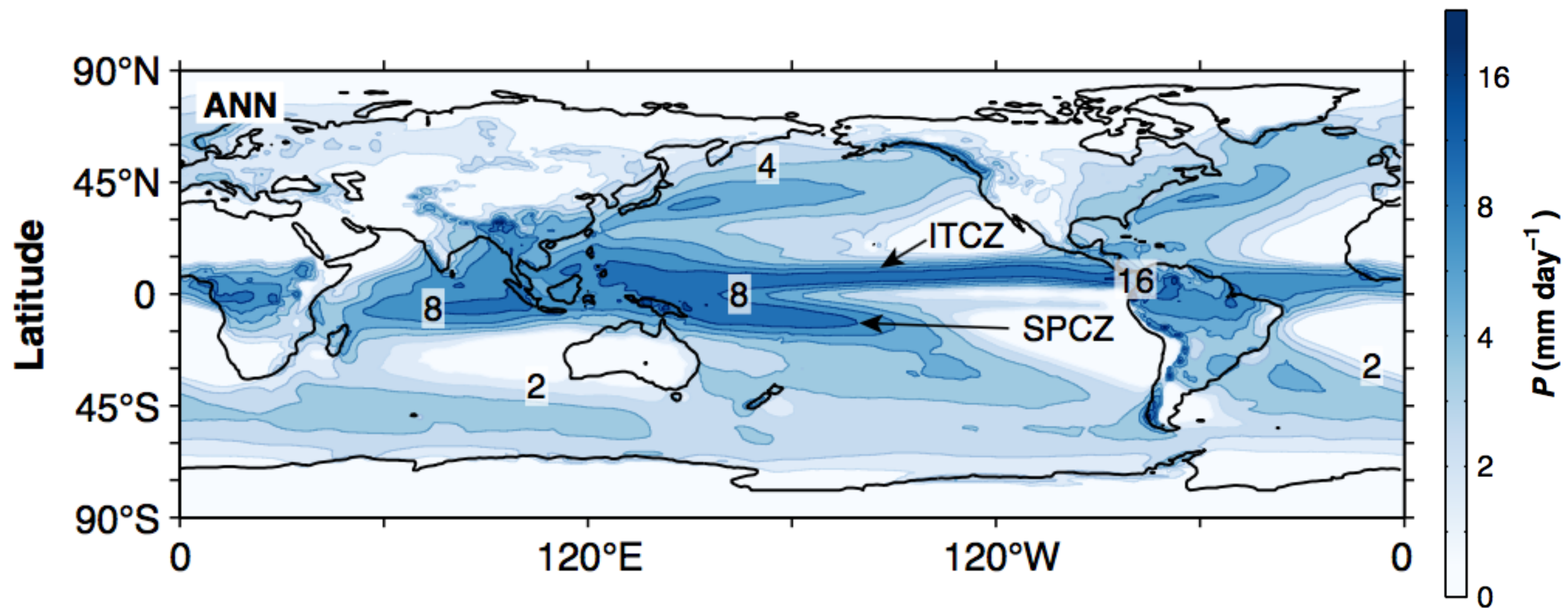


# Earth's water cycle: precipitation



*Tropical Rainfall Measuring Mission (TRMM)*

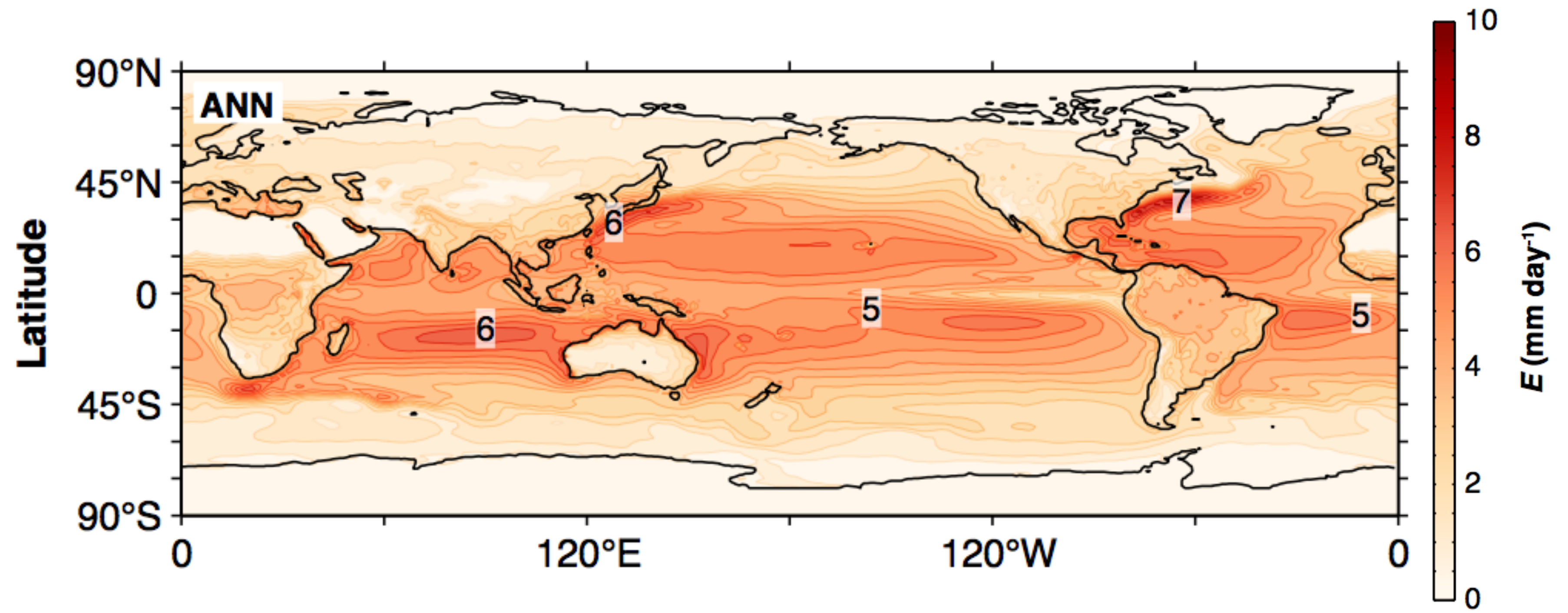
# Earth's water cycle: precipitation



from Schneider's "Physics of Earth's Climate"

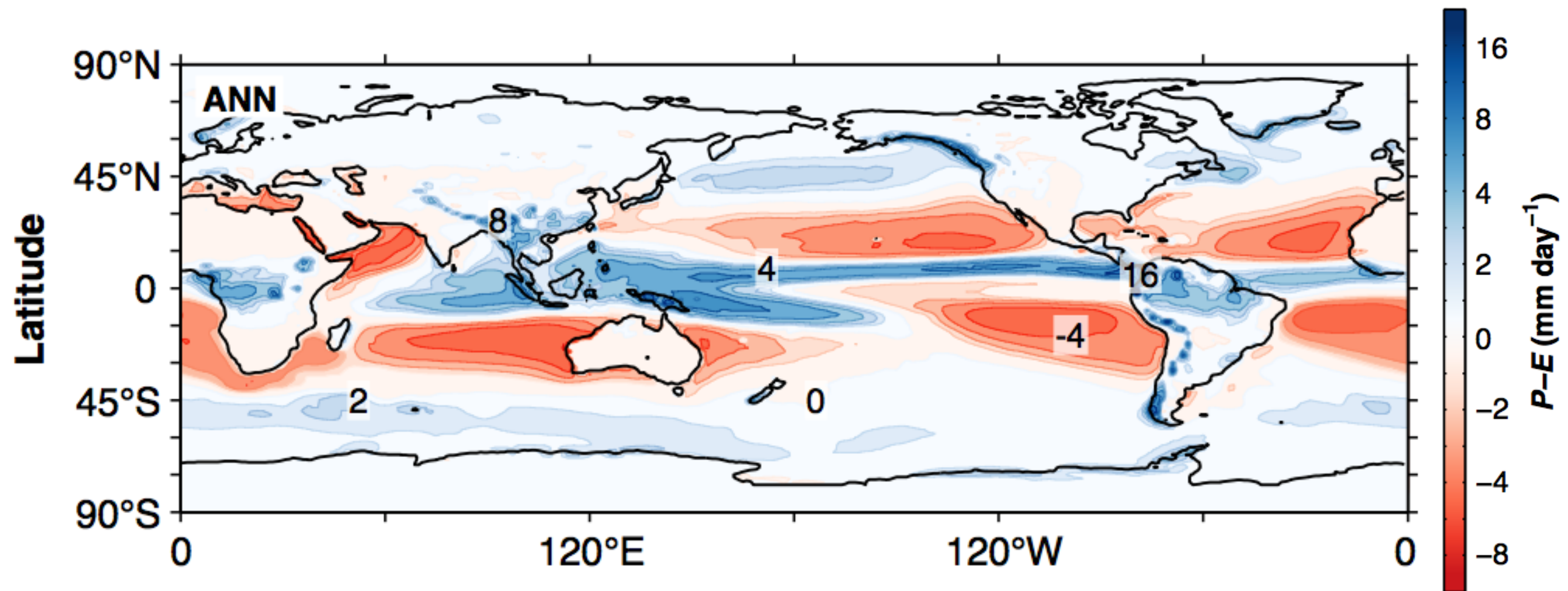


# Earth's water cycle: evaporation



from Schneider's "Physics of Earth's Climate"

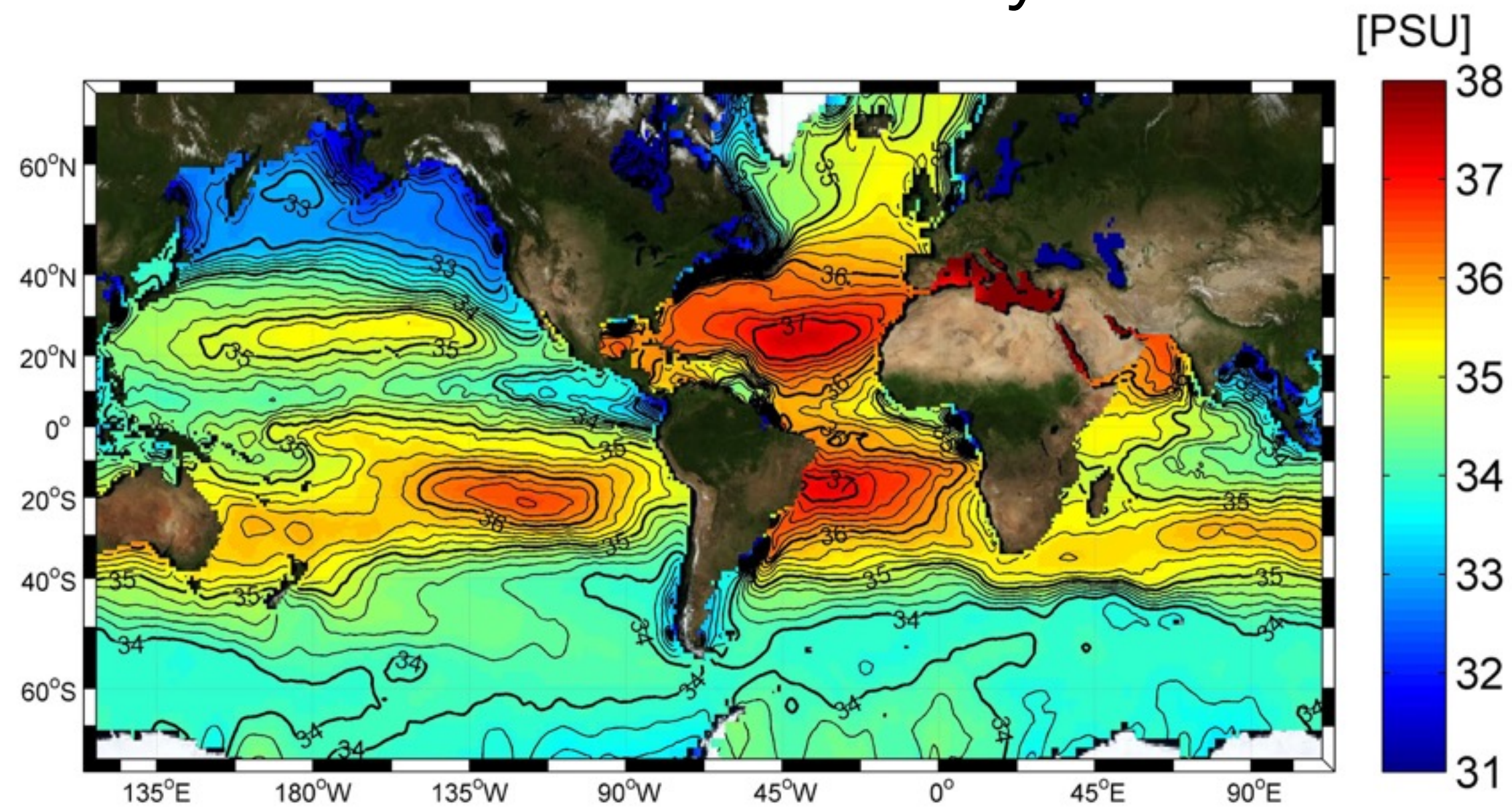
# Earth's water cycle: *net* precipitation (P-E)



from Schneider's "Physics of Earth's Climate"

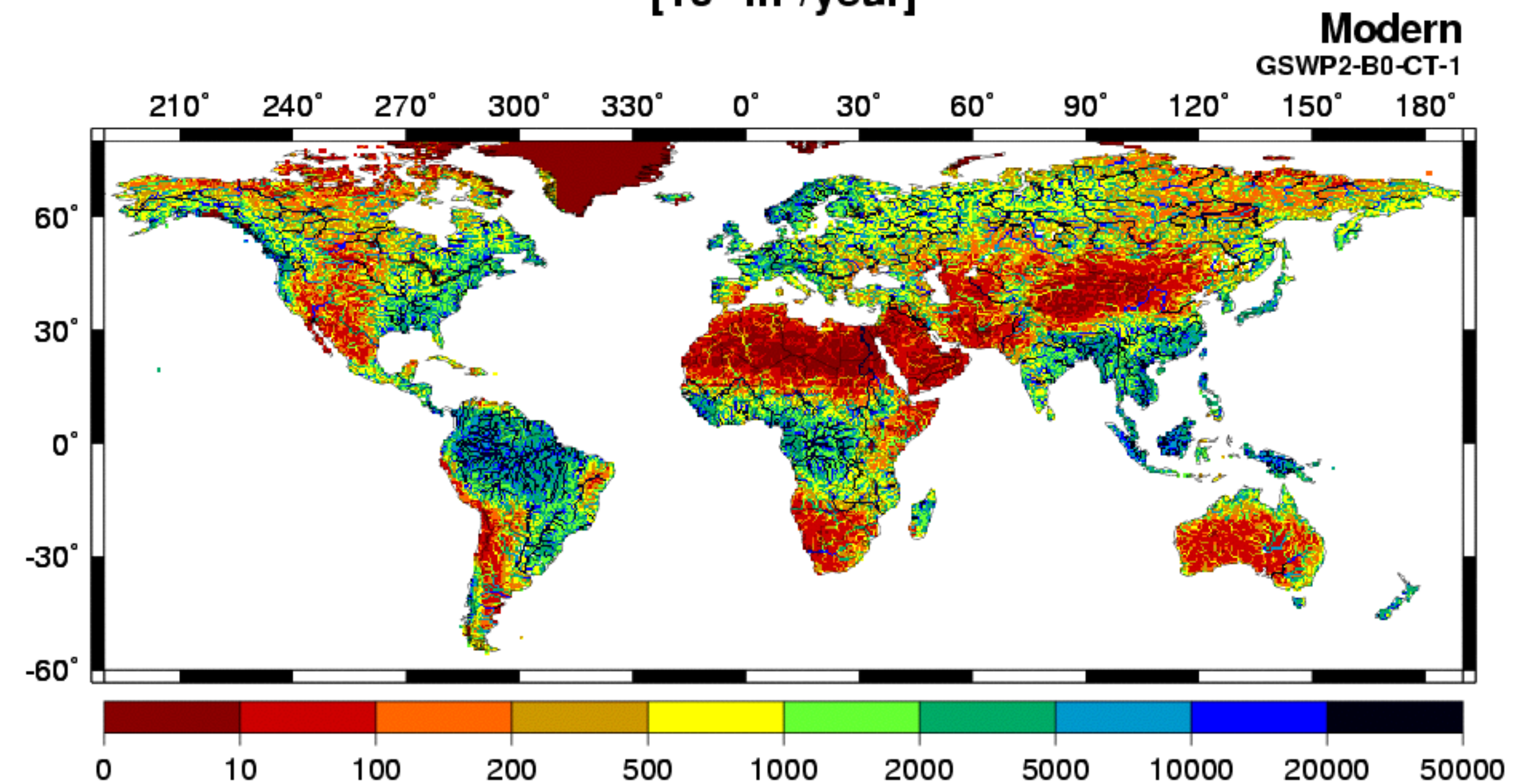
# Earth's water cycle: Impact of $P-E$ on oceans and continents

ocean salinity



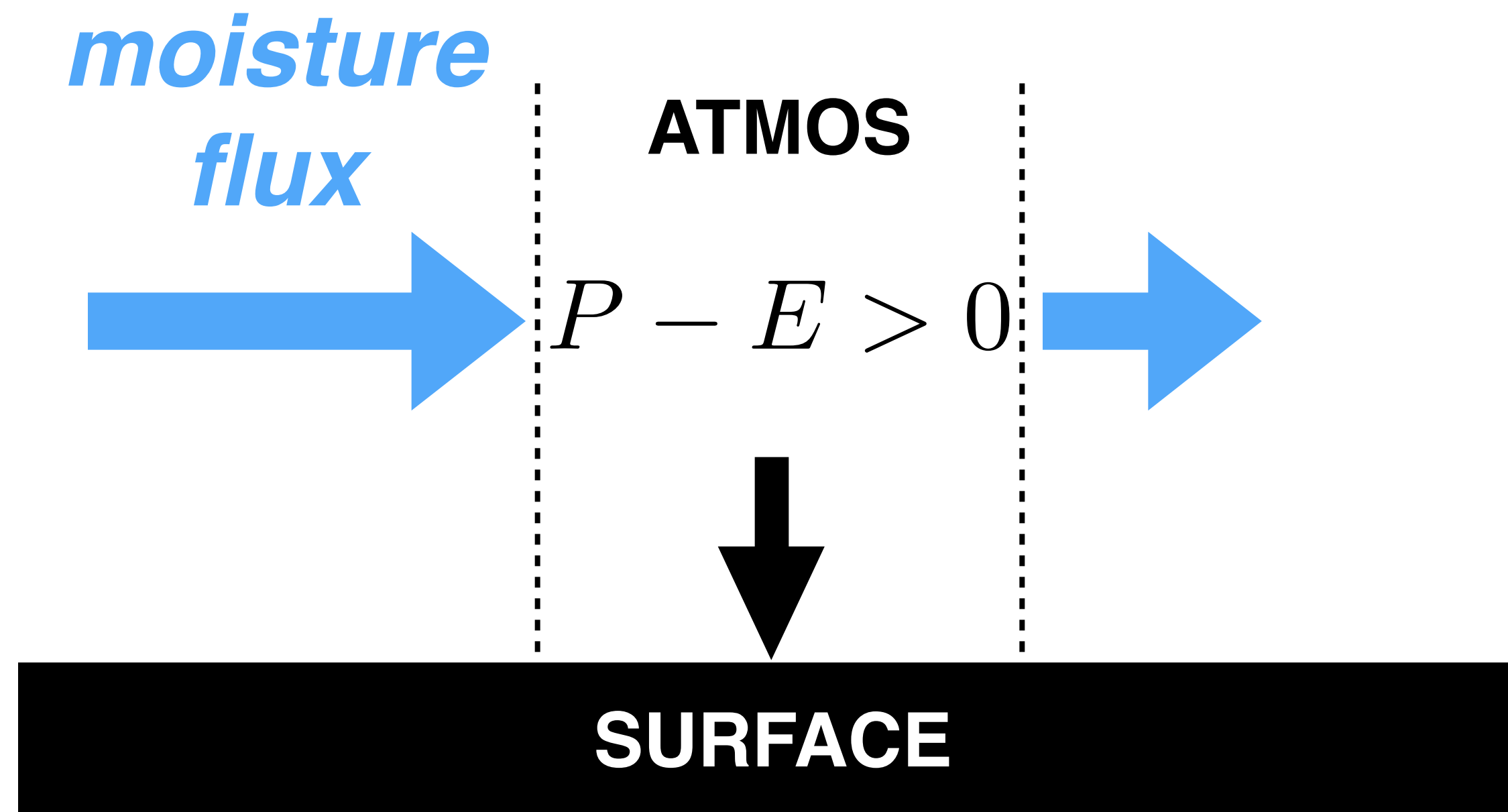
World Ocean Atlas (2005)

Annual River Discharge  
[ $10^6 \text{ m}^3/\text{year}$ ]



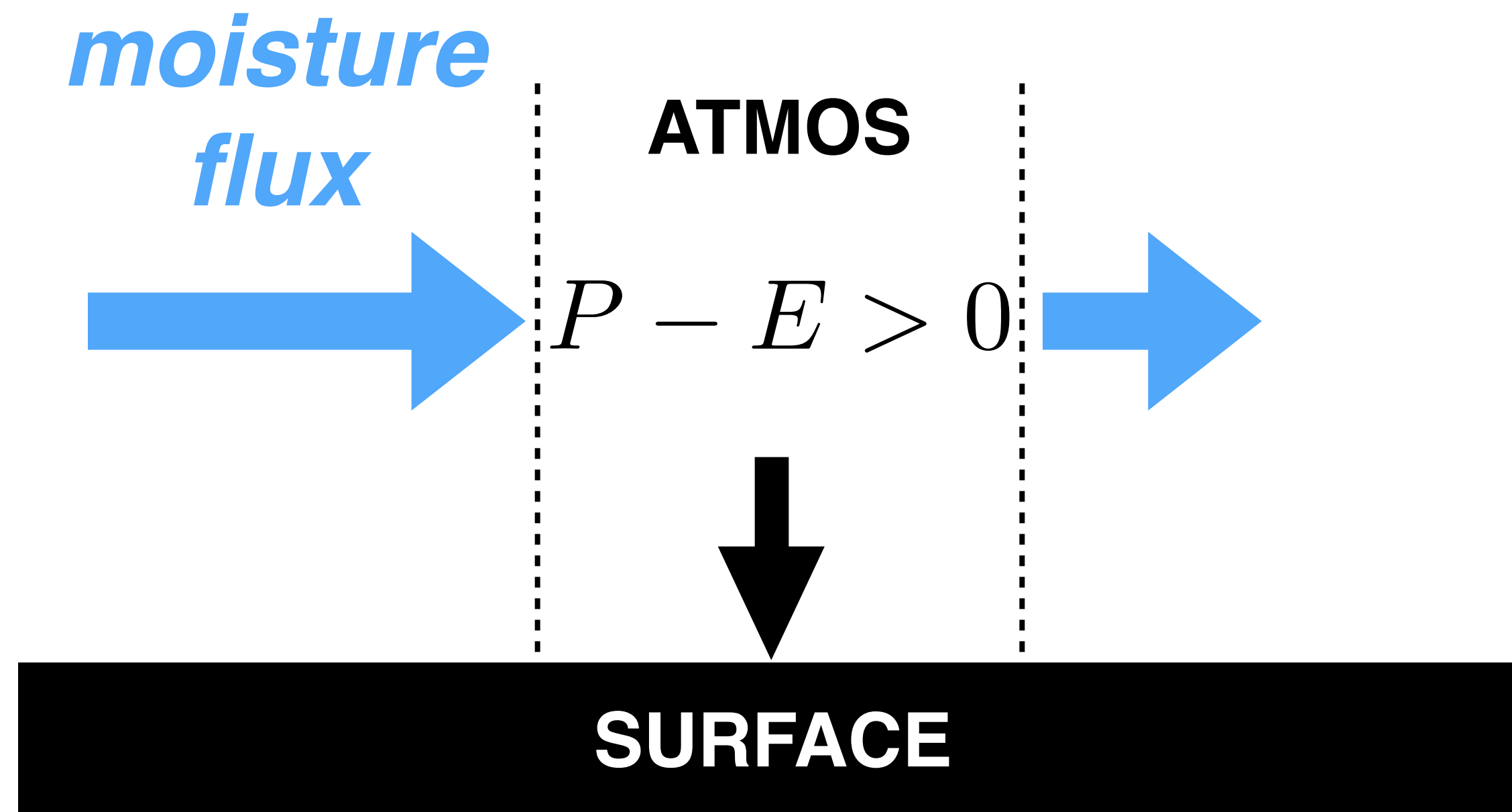
Global Water Resource Archive

# Earth's water cycle: P-E and the atmospheric circulation

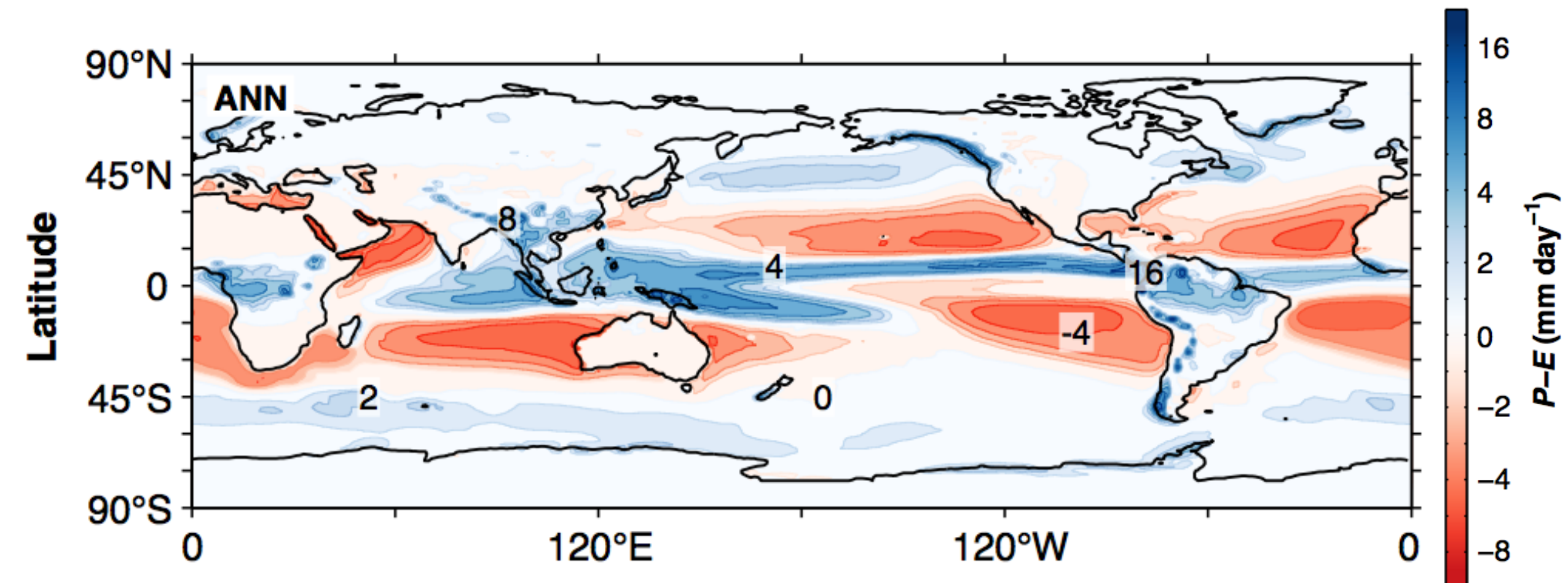


$$P - E = -\nabla \cdot \mathbf{F} = -\nabla \cdot [q\mathbf{u}] \\ \approx -[q\nabla \cdot \mathbf{u}]$$

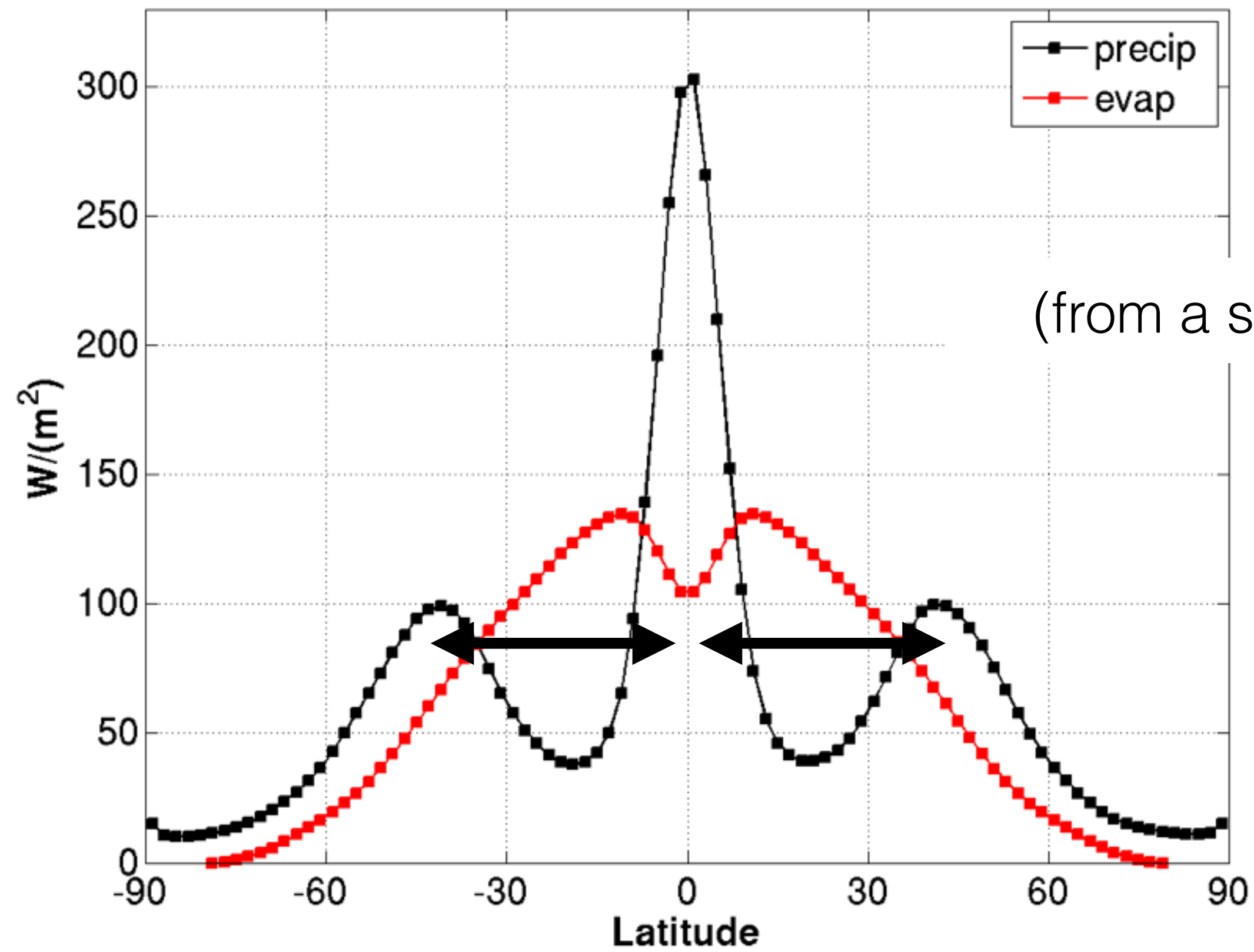
# Earth's water cycle: P-E and the atmospheric circulation



$$P - E = -\nabla \cdot \mathbf{F} = -\nabla \cdot [q\mathbf{u}]$$
$$\approx -[q\nabla \cdot \mathbf{u}]$$



Atmosphere moves moisture from dry subtropics ( $P-E < 0$ ) to moist tropics & extratropics ( $P-E > 0$ )



$$P - E = -\nabla \cdot \mathbf{F} = -\nabla \cdot [q\mathbf{u}]$$

$$\approx -[q\nabla \cdot \mathbf{u}]$$

